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**WBJEE 2022 Question Paper** 

West Bengal Joint Entrance Examinations

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### **WBJEE 2022 Solved Paper**

### **Mathematics**

### **Question 1**

The values of a, b, c for which the function  $f(x) = \begin{cases} \frac{\sin(a+1)x + \sin x}{x}, & x < 0 \\ c, x = 0 \\ \frac{(x+bx^2)^{\frac{1}{2}} - x^{\frac{1}{2}}}{bx^{\frac{1}{2}}}, & x > 0 \end{cases}$ is continuous at x = 0, are

**Options:** 

A.

 $a=rac{3}{2}, b=-rac{3}{2}, c=rac{1}{2}$ 

Β.

 $a = -\frac{3}{2}, c = \frac{3}{2}, b$  is arbitrary non-zero real number.

C.

$$a=-rac{5}{2},b=-rac{3}{2},c=rac{3}{2}$$

D.

 $a=-2, b\in R-\{0\}, c=0$ 

#### Answer: D

#### Solution:

For continuous at x = 0,

$$egin{aligned} &\lim_{x o 0} f(x) = f(0) \ &RHL = \lim_{x o 0^+} rac{(x+bx^2)^{rac{1}{2}}-x^{rac{1}{2}}}{bx^{rac{1}{2}}} \ &= \lim_{x o 0^+} rac{x^{rac{1}{2}}igl\{(1+bx)^{rac{1}{2}}-1igr\}}{bx^{rac{1}{2}}} \end{aligned}$$

$$= \lim_{x \to 0^+} \frac{(1+bx)^{\frac{1}{2}} - 1}{b}$$
  
= 0 (when b \neq 0)  
$$LHL = \lim_{x \to 0^-} \frac{\sin(a+1)x + \sin x}{x} \left(\frac{0}{0}\right)$$
  
$$= \lim_{x \to 0^-} \frac{(\cos(a+1)x)(a+1) + \cos x}{1}$$
  
$$= a + 1 + 1$$
  
$$= a + 2$$
  
And  $f(0) = c$  (given)  
We know, for continuous function  
$$LHL = RHL = f(0)$$
  
$$\therefore a + 2 = 0 (b \neq 0) = c$$

 $\therefore c = 0, a = -2$ 

and  $b = R - \{0\}$ 

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### **Question 2**

Domain of 
$$y = \sqrt{\log_{10} rac{3x-x^2}{2}}$$
 is

**Options:** 

A.

x < 1

В.

2 < x

C.

 $1 \le x \le 2$ 

D.

2 < x < 3

#### Answer: C

#### Solution:

 $\log_{10}\left(\frac{3x-x^{2}}{2}\right) \geq 0$   $\Rightarrow \frac{3x-x^{2}}{2} \geq 10^{0}$   $\Rightarrow \frac{3x-x^{2}}{2} \geq 1$   $\Rightarrow 3x - x^{2} \geq 2$   $\Rightarrow x^{2} - 3x + 2 \leq 0$   $\Rightarrow (x - 2)(x - 1) \leq 0$   $\therefore x \in [1, 2] \dots (1)$ Also,  $\frac{3x-x^{2}}{2} > 0$   $\Rightarrow x^{2} - 3x < 0$   $\Rightarrow x(x - 3) < 0$   $\Rightarrow x \in (0, 3) \dots (2)$   $\therefore \text{ Intersection of (1) and (2) is } x \in [1, 2]$ 

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### **Question 3**

Let  $f(x) = a_0 + a_1|x| + a_2|x|^2 + a_3|x|^3$ , where  $a_0, a_1, a_2, a_3$  are real constants. Then f(x) is differentiable at x = 0

#### **Options:**

A.

whatever be  $a_0, a_1, a_2, a_3$ .

#### В.

for no values of  $a_0, a_1, a_2, a_3$ .

C.

only if  $a_1 = 0$ 

D.

only if  $a_1 = 0, a_3 = 0$ 

#### Answer: C

#### Solution:

Given,

 $f(x) = a_0 + a_1 |x| + a_2 |x|^2 + a_3 |x|^3$   $\therefore f(x) = \begin{cases} a_0 + a_1 x + a_2 x^2 + a_3 x^3, & x \ge 0 \\ a_0 - a_1 x + a_2 x^2 - a_3 x^3, & x < 0 \end{cases}$   $\Rightarrow f(x) = \begin{cases} a_1 + 2a_2 x + 3a_3 x^2, & x \ge 0 \\ -a_1 + 2a_2 x - 3a_3 x^2, & x < 0 \end{cases}$  f(x) is differentiable at x = 0  $\therefore \text{ L. H. D = R. H. D}$   $\Rightarrow -a_1 + 0 + 0 = a_1 + 0 + 0$   $\Rightarrow 2a_1 = 0$  $\Rightarrow a_1 = 0$ 

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### **Question 4**

If  $y = e^{\tan^{-1}x}$ , then

**Options:** 

A.

 $(1+x^2)y_2+(2x-1)y_1=0$ 

В.

 $(1+x^2)y_2+2xy=0$ 

C.

 $(1-x^2)y_2-y_1=0$ 

D.

 $(1+x^2)y_2 + 3xy_1 + 4y = 0$ 

**Answer:** A

#### Solution:

 $y=e^{ an^{-1}x}$ 

Differentiating both sides with respect to x, we get

$$egin{aligned} &\Rightarrow rac{dy}{dx} = e^{ an^{-1}(x)} imes rac{1}{1+x^2} \ &\Rightarrow y_1(1+x^2) = e^{ an^{-1}x} \ &\Rightarrow y_1(1+x^2) = y \end{aligned}$$

Differentiating both side with respect to x, we get

$$egin{aligned} &\Rightarrow y_2(1+x^2)+y_1(2x)=y_1 \ &\Rightarrow y_2(1+x^2)+y_1(2x-1)=0 \end{aligned}$$

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### **Question 5**

$$\lim_{x\to 0} \left(\frac{1}{x} \ln \sqrt{\frac{1+x}{1-x}}\right) \text{ is }$$

#### **Options:**

A.

 $\frac{1}{2}$ 

B.

0

C.

1

#### D.

does not exist

#### Answer: C

$$\lim_{x \to 0} \left( \frac{1}{x} \ln \sqrt{\frac{1+x}{1-x}} \right)$$
  
Put  $x = \cos 2\theta$   
 $\Rightarrow 2\theta = \cos^{-1}(x)$   
 $\Rightarrow \theta = \frac{1}{2}\cos^{-1}(x)$   
when  $x \to 0$  then  $\theta \to \frac{\pi}{4}$   
 $\therefore \lim_{\theta \to \frac{\pi}{4}} \left( \frac{\ln \sqrt{\frac{1+\cos 2\theta}{1-\cos 2\theta}}}{\cos 2\theta} \right)$   
 $= \lim_{\theta \to \frac{\pi}{4}} \left( \frac{\ln \sqrt{\frac{2\cos^2\theta}{2\sin^2\theta}}}{\cos 2\theta} \right)$ 

$$= \lim_{\theta \to \frac{\pi}{4}} \left( \frac{\ln (\cot^2 \theta)^{\frac{1}{2}}}{\cos 2\theta} \right)$$
$$= \lim_{\theta \to \frac{\pi}{4}} \left( \frac{\ln |\cot \theta|}{\cos 2\theta} \right)$$

when  $\theta \to \frac{\pi}{4}$  then  $\cot \theta > 0$ 

 $\therefore |\!\cot\theta| = \cot\theta$ 

$$= \lim_{\theta \to \frac{\pi}{4}} \frac{\ln(\cot \theta)}{\cos 2\theta} \left( \frac{0}{0} \text{ form} \right)$$

Applying L' Hospital Rule,

$$= \lim_{\theta \to \frac{\pi}{4}} \frac{\frac{1}{\cot \theta} \times (-\cos ec^2 \theta)}{-\sin 2\theta \times 2}$$
$$= \frac{\frac{1}{\cot \frac{\pi}{4}} \times -\cos ec^2 \frac{\pi}{4}}{-\sin \frac{\pi}{2} \times 2}$$
$$= \frac{\frac{1}{1} \times -(\sqrt{2})^2}{-1 \times 2} = 0$$
$$= \frac{2}{2} = 1$$

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### **Question 6**

Let  $f : [a, b] \rightarrow R$  be continuous in [a, b], differentiable in (a, b) and f(a) = 0 = f(b). Then

#### **Options:**

there exists at least one point  $c \in (a, b)$  for which f'(c) = f(c)

#### B.

$$f'(x) = f(x)$$
 does not hold at any point of (a, b)

at every point of (a, b), f'(x) > f(x)

#### D.

at every point of (a, b), f'(x) < f(x)

#### Answer: A

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### **Question 7**

$$I = \int \cos(\ln x) dx$$
. Then I =

#### **Options:**

A.

 $\frac{x}{2} \{ \cos(\ln x) + \sin(\ln x) \} + c \text{ (c denotes constant of integration)}$ 

B.

 $x^{2} \{ \cos(\ln x) - \sin(\ln x) \} + c$  (c denotes constant of integration)

C.

 $x^2 \sin(\ln x) + c$  (c denotes constant of integration)

D.

 $x \cos(\ln x) + c$  (c denotes constant of integration)

#### Answer: A

$$I = \int \cos(\ln x) dx$$
  
Let,  $\ln x = t$   
 $\Rightarrow x = e^t$ 

 $\Rightarrow dx = e^{t}dt$   $\therefore I = \int \cos(t) \cdot e^{t}dt$ Apply integration by parts theorem,  $= \cos t \cdot \int e^{t}dt - \int \left(\frac{d}{dt}(\cos t) \cdot \int e^{t}dt\right)dt$   $= \cos t \cdot e^{t} + \int \sin t \cdot e^{t}dt$   $I = \cos t \cdot e^{t} + \sin t \cdot e^{t} - \int (\cos t \cdot e^{t}) dt$   $\Rightarrow I = \cos t \cdot e^{t} + \sin t \cdot e^{t} - I$   $\Rightarrow 2I = \cos t \cdot e^{t} + \sin t \cdot e^{t} + C$   $\Rightarrow 2I = e^{t}(\cos t + \sin t) + C$   $\Rightarrow 2I = x (\cos(\ln x) + \sin(\ln x)) + C$  $\Rightarrow I = \frac{x}{2} [\cos(\ln x) + \sin(\ln x)] + C$ 

### **Question 8**

#### Let f be derivable in [0, 1], then

#### **Options:**

#### A.

there exists  $c \in (0,1)$  such that  $\int_{0}^{c} f(x) dx = (1-c)f(c)$ 

#### B.

there does not exist any point  $d \in (0,1)$  for which  $\int_0^d f(x) dx = (1-d)f(d)$ 

 $\int_{0}^{c} f(x) dx$  does not exist, for any  $c \in (0, 1)$ 

 $\int_{0}^{c} f(x) dx$  is independent of  $c, c \in (0, 1)$ 

#### Answer: A

#### Solution:

Let f(x) = x which is derivable in [0, 1]. Option A :  $\int_0^c f(x) dx = (1 - c) f(c)$   $\Rightarrow \int_0^c x dx = (1 - c) \cdot c$   $\Rightarrow \left[\frac{x^2}{2}\right]_0^c = (1 - c) c$   $\Rightarrow \frac{c^2}{2} = (1 - c) c$   $\therefore c = 0$ or  $\frac{c}{2} = 1 - c$   $\Rightarrow c = 2 - 2c$   $\Rightarrow 3c = 2$   $\Rightarrow c = \frac{2}{3}$ 

 $\therefore$  c = 0 does not belongs to (0, 1) but  $c = \frac{2}{3}$  belongs to (0, 1)

: Option A is correct.

Option B :

$$\int_0^d f(x) dx = (1-d)f(d)$$
  
 $\Rightarrow \int_0^d x \, dx = (1-d) \cdot d$   
 $\Rightarrow \frac{d^2}{2} = (1-d)d$   
 $\therefore d = 0$ 

or

$$\frac{d}{2} = 1 - d$$

 $\Rightarrow d = \frac{2}{3}$  (which belongs to in between (0, 1))

: Option B is incorrect.

Option C :

 $\int_0^c f(x) dx$  $= \int_0^c x dx$  $= \left[\frac{x^2}{2}\right]_0^c$ 

 $=\frac{c^2}{2}$ 

 $\frac{c^2}{2}$  exist all values of c between 0 and 1.

: Option C is incorrect.

Option D :

 $\int_0^c f(x) = dx$ 

 $=\int_0^c x\,dx$ 

$$=\left[\frac{x^2}{2}\right]_0^c$$

$$=\frac{c^2}{2}$$

 $\therefore \int_0^c f(x) \, dx$  is not independent of c.

: Option D is incorrect.

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### **Question 9**

Let 
$$\int rac{x^{rac{1}{2}}}{\sqrt{1-x^3}} dx = rac{2}{3}g(f(x))+c$$
 ; then

#### (c denotes constant of integration)

#### **Options:**

A.

$$f(x)=\sqrt{x},g(x)=x^{rac{3}{2}}$$

B.

$$f(x)=x^{\frac{3}{2}},g(x)=\sin^{-1}x$$

C.

$$f(x)=\sqrt{x},g(x)=\sin^{-1}x$$

D.

 $f(x)=\sin^{-1}x,g(x)=x^{\frac{3}{2}}$ 

#### Answer: B

$$I = \int \frac{x^{1/2}}{\sqrt{1-x^3}} dx$$
  
Let  $x^{3/2} = t$   
 $\Rightarrow \frac{3}{2}x^{1/2}dx = dt$   
 $\therefore I = \int \frac{2}{3} \cdot \frac{dt}{\sqrt{1-t^2}}$   
 $= \frac{2}{3}\sin^{-1}t + C$   
 $= \frac{2}{3}\sin^{-1}(x^{3/2}) + C$   
 $= \frac{2}{3}g(f(x)) + C$   
 $\therefore f(x) = x^{3/2} \text{ and } g(x) = \sin^{-1}(x)$ 

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### **Question 10**

The value of 
$$\int_{0}^{\frac{\pi}{2}} \frac{(\cos x)^{\sin x}}{(\cos x)^{\sin x} + (\sin x)^{\cos x}} dx$$
 is

#### **Options:**

A.
π/4
B.
0
C.
π/2
D.
1/2

#### Answer: A

$$I = \int_{0}^{\frac{\pi}{2}} \frac{(\cos x)^{\sin x}}{(\cos x)^{\sin x} + (\sin x)^{\cos x}} dx \dots (1)$$

Replace x with  $\left(\frac{\pi}{2} - x\right)$ ,

$$\therefore I = \int_{0}^{\frac{\pi}{2}} \frac{[\cos(\frac{\pi}{2}-x)]^{\sin(\frac{\pi}{2}-x)}}{[\cos(\frac{\pi}{2}-x)]^{\sin(\frac{\pi}{2}-x)} + [\sin(\frac{\pi}{2}-x)]^{\cos(\frac{\pi}{2}-x)}} dx$$
$$I = \int_{0}^{\frac{\pi}{2}} \frac{(\sin x)^{\cos x}}{(\sin x)^{\cos x} + (\cos x)^{\sin x}} dx \dots (2)$$

Adding 1 and 2 we get,

$$2I = \int_{0}^{\frac{\pi}{2}} \frac{(\sin x)^{\cos x} + (\cos x)^{\sin x}}{(\sin x)^{\cos x} + (\cos x)^{\sin x}} dx$$
$$= \int_{0}^{\frac{\pi}{2}} 1 dx$$
$$= \frac{\pi}{2}$$
$$\Rightarrow I = \frac{\pi}{4}$$

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### **Question 11**

Let  $\lim_{\epsilon \to 0+} \int_{\epsilon}^{x} \frac{bt \cos 4t - a \sin 4t}{t^2} dt = \frac{a \sin 4x}{x} - 1$ ,  $(0 < x < \frac{\pi}{4})$ . Then a and b are given by

#### **Options:**

A.

a=2,b=2

B.

 $a=rac{1}{4},b=1$ 

C.

a=-1,b=4

D.

a=2,b=4

Answer: B

$$egin{aligned} &\lim_{\epsilon o 0^+}\int_{\epsilon}^xrac{bt\cos 4t-a\sin 4t}{t^2}dt = rac{a\sin 4x}{x}-1 \ &\Rightarrow \int_{0^+}^xrac{bt\cos 4t-a\sin 4t}{t^2}dt = rac{a\sin 4x}{x}-1 \end{aligned}$$

Differentiating both sides we get,

 $\frac{bx\cos 4x - a\sin 4x}{x^2} = \frac{xa\cos 4x \times 4 - a\sin 4x}{x^2}$ 

 $\Rightarrow bx \cos 4x - a \sin 4x = 4ax \cos 4x - a \sin 4x$ 

Comparing coefficient of cos 4x and sin 4x both side we get,

b = 4a an -a = -a

$$\therefore \frac{b}{a} = 4$$

By checking options, when  $a = \frac{1}{4}$  and b = 1, then,

$$\frac{b}{a} = 4$$

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### **Question 12**

Let 
$$f(x) = \int_{\sin x}^{\cos x} e^{-t^2} dt$$
. Then  $f'\left(\frac{\pi}{4}\right)$  equals

**Options:** 

A.

 $\sqrt{\frac{1}{e}}$ 

B.

 $-\sqrt{\frac{2}{e}}$ 

C.

 $\sqrt{\frac{2}{e}}$ 

D.

$$-\sqrt{\frac{1}{e}}$$

Answer: B

#### Solution:

$$f(x) = \int\limits_{\sin x}^{\cos x} e^{-t^2} dt$$

Differentiating both sides using Newton Leibnitz formula,

$$f'(x) = e^{-\cos^2 x} \cdot (-\sin x) - e^{-\sin^2 x} \cdot (\cos x)$$
  
$$\therefore f'\left(\frac{\pi}{4}\right) = e^{-\frac{1}{2}} \cdot \left(-\frac{1}{\sqrt{2}}\right) - e^{-\frac{1}{2}} \cdot \left(\frac{1}{\sqrt{2}}\right)$$
  
$$= -\frac{2}{\sqrt{2}}e^{-\frac{1}{2}}$$
  
$$= -\sqrt{2}e^{-\frac{1}{2}}$$
  
$$= -\sqrt{\frac{2}{e}}$$

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### **Question 13**

If 
$$xrac{dy}{dx} + y = xrac{f(xy)}{f'(xy)},$$
 then  $|f(xy)|$  is equal to

#### **Options:**

A.

 $Ce^{\frac{x^2}{2}}$  (where C is the constant of integration)

В.

 $Ce^{x^2}$  (where C is the constant of integration)

C.

 $Ce^{2x^2}$  (where C is the constant of integration)

D.

 $Ce^{\frac{x^2}{3}}$  (where C is the constant of integration)

#### Answer: A

Given,  $x \frac{dy}{dx} + y = x \cdot \frac{f(xy)}{f'(xy)}$ Let, xy = t

Differentiating both sides with respect to x,

$$egin{aligned} y+xrac{dy}{dx}&=rac{dt}{dx}\ &\thereforerac{dt}{dx}&=x\,.rac{f(t)}{f'(t)}\ &\Rightarrowrac{f'(t)}{f(t)}dt&=x\,dx \end{aligned}$$

Integrating both sides, we get

 $\int \frac{f'(t)}{f(t)} dt = \int x \, dx$   $\Rightarrow \ln |f(t)| = \frac{x^2}{2} + C$   $\Rightarrow |f(t)| = e^{\frac{x^2}{2} + C}$   $\Rightarrow |f(xy)| = e^{\frac{x^2}{2}} \cdot e^2$  $\Rightarrow |f(xy)| = e^{\frac{x^2}{2}} \cdot C [e^c = \text{constant} = C]$ 

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### **Question 14**

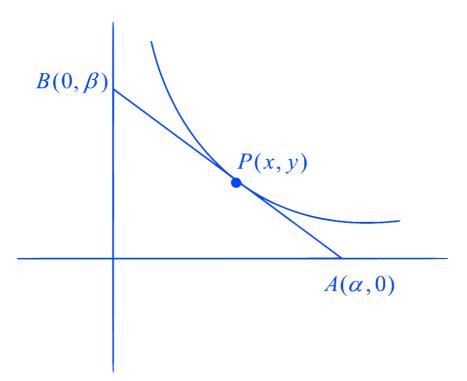
A curve passes through the point (3, 2) for which the segment of the tangent line contained between the co-ordinate axes is bisected at the point of contact. The equation of the curve is

**Options:** 

A.  $y = x^{2} - 7$ B.  $x = \frac{y^{2}}{2} + 2$ C. xy = 6D.  $x^{2} + y^{2} - 5x + 7y + 11 = 0$ 

#### Answer: C

#### Solution:



According to the question, p(x, y) is the midpoint of line AB.

 $\therefore \frac{\alpha+0}{2} = x \Rightarrow \alpha = 2x$  $\frac{\beta+0}{2} = y \Rightarrow \beta = 2y$  $\therefore \text{Point A} = (2x, 0)$ and Point B = (0, 2y) Slope of the tangent, $\frac{dy}{dx} = \frac{2y-0}{0-2x}$  $\Rightarrow \frac{dy}{dx} = -\frac{y}{x}$  $\Rightarrow x \, dy + y \, dx = 0$ 

 $\Rightarrow d(xy) = 0$ 

 $\Rightarrow xy = c$ 

This curve goes through point (3, 2). So this point satisfy the equation.

 $\therefore 3 \cdot 2 = c$  $\Rightarrow c = 6$ 

: Equation of the curve,

xy = 6

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### **Question 15**

#### The solution of

 $\cos y \frac{dy}{dx} = e^{x + \sin y} + x^2 e^{\sin y}$  is  $f(x) + e^{-\sin y} = C$  (C is arbitrary real constant) where f(x) is equal to

**Options:** 

A.  $e^{x} + \frac{1}{2}x^{3}$ B.  $e^{-x} + \frac{1}{3}x^{3}$ C.  $e^{-x} + \frac{1}{2}x^{3}$ D.  $e^{x} + \frac{1}{3}x^{3}$ 

#### Answer: D

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### **Question 16**

The point of contact of the tangent to the parabola  $y^2 = 9x$  which passes through the point (4, 10) and makes an angle  $\theta$  with the

#### positive side of the axis of the parabola where $tan\theta > 2$ , is

**Options:** 

А.	
$\left(\frac{4}{9},2\right)$	
В.	
(4, 6)	
С.	
(4, 5)	
D.	
$\left(rac{1}{4},rac{1}{6} ight)$	
Answer: A	

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### **Question 17**

### Let $f(x) = (x-2)^{17}(x+5)^{24}$ . Then

#### **Options:**

A.

f does not have a critical point at x = 2

#### B.

f has a minimum at x = 2

#### C.

f has neither a maximum nor a minimum at x = 2

#### D.

f has a minimum at x = 2

#### Answer: C

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### **Question 18**

If  $\overrightarrow{a} = \hat{i} + \hat{j} - \hat{k}$ ,  $\overrightarrow{b} = \hat{i} - \hat{j} + \hat{k}$  and  $\overrightarrow{c}$  is unit vector perpendicular to  $\overrightarrow{a}$  and coplanar with  $\overrightarrow{a}$  and  $\overrightarrow{b}$ , then unit vector  $\overrightarrow{d}$  perpendicular to both  $\overrightarrow{a}$  and  $\overrightarrow{c}$  is

**Options:** 

A.  $\pm \frac{1}{\sqrt{6}} \left( 2\hat{i} - \hat{j} + \hat{k} \right)$ B.  $\pm \frac{1}{\sqrt{2}} \left( \hat{j} + \hat{k} \right)$ C.  $\pm \frac{1}{\sqrt{6}} \left( \hat{i} - 2\hat{j} + \hat{k} \right)$ D.  $\pm \frac{1}{\sqrt{2}} \left( \hat{j} - \hat{k} \right)$ Answer: B

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### **Question 19**

If the equation of one tangent to the circle with centre at (2, -1) from the origin is 3x + y = 0, then the equation of the other tangent through the origin is

**Options:** 

A.3x - y = 0B.

x + 3y = 0

C. x - 3y = 0D. x + 2y = 0Answer: C

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### **Question 20**

Area of the figure bounded by the parabola  $y^2 + 8x = 16$  and  $y^2 - 24x = 48$  is

**Options:** 

A.  $\frac{11}{9}$  sq. unit B.  $\frac{32}{3}\sqrt{6}$  sq. unit C.  $\frac{16}{3}$  sq. unit D.  $\frac{24}{5}$  sq. unit Answer: B

### **Question 21**

A particle moving in a straight line starts from rest and the acceleration at any time t is  $a - kt^2$  where a and k are positive constants. The maximum velocity attained by the particle is

**Options:** 

A.
$\frac{2}{3}\sqrt{rac{a^3}{k}}$
B.
$rac{1}{3}\sqrt{rac{a^3}{k}}$
C.
$\sqrt{rac{a^3}{k}}$
D.
$2\sqrt{rac{a^3}{k}}$

Answer: A

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### **Question 22**

# If a, b, c are in G.P. and log $a - \log 2b$ , log $2b - \log 3c$ , log $3c - \log a$ are in A.P., then a, b, c are the lengths of the sides of a triangle which is

**Options:** 

A.

acute angled

B.

obtuse angled

C.

right angled

D.

equilateral

#### Answer: B

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### **Question 23**

```
Let a_n = (1^2 + 2^2 + \dots n^2)^n and b_n = n^n (n!). Then
```

#### **Options:**

A.

 $a_n < b_n orall n$ 

В.

 $a_n > b_n orall n$ 

C.

 $a_n = b_n$  for infinitely many n

D.

 $a_n < b_n$  if n be even and  $a_n > b_n$  if n be odd

#### Answer: B

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### **Question 24**

#### The number of zeros at the end of 100 is

**Options:** 

A.

21

B.

22

C.

23

D.

24

#### -----

### **Question 25**

If  $|z - 25i| \le 15$ , then Maximum  $\arg(z)$  – Minimum  $\arg(z)$  is equal to

(arg z is the principal value of argument of z)

#### **Options:**

```
A.

2\cos^{-1}\left(\frac{3}{5}\right)

B.

2\cos^{-1}\left(\frac{4}{5}\right)

C.

\frac{\pi}{2} + \cos^{-1}\left(\frac{3}{5}\right)

D.

\sin^{-1}\left(\frac{3}{5}\right) - \cos^{-1}\left(\frac{3}{5}\right)

Answer: B
```

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### **Question 26**

If z = x - iy and  $z^{\frac{1}{3}} = p + iq(x, y, p, q \in R)$ , then  $\frac{\left(\frac{x}{p} + \frac{y}{q}\right)}{(p^2 + q^2)}$  is equal to

#### **Options:**

A.

2

B.

-1

C.		
1		
D.		
-2		
Answer: D		

### **Question 27**

If a, b are odd integers, then the roots of the equation  $2ax^2 + (2a+b)x + b = 0, a \neq 0$  are

#### **Options:**

А.	
rational	
В.	
irrational	
С.	
non-real	
D.	
equal	
Answer: A	

### **Question 28**

There are n white and n black balls marked 1, 2, 3, ..... n. The number of ways in which we can arrange these balls in a row so that neighbouring balls are of different colours is

**Options:** 

А.	
(n!) <sup>2</sup>	
В.	
(2n)!	
C.	
2(n!) <sup>2</sup>	
D.	
$\frac{(2n)!}{(n!)^2}$	

Answer: C

-----

### **Question 29**

Let  $f(n)=2^{n+1},$   $g(n)=1+(n+1)2^n$  for all  $n\in N.$  Then

#### **Options:**

A.

f(n)>g(n)

B.

f(n) < g(n)

C.

f(n) and g(n) are not comparable.

#### D.

f(n) > g(n) if n be even and f(n) < g(n) if n be odd.

#### Answer: B

-----

### **Question 30**

#### A is a set containing n elements. P and Q are two subsets of A. Then the number of ways of choosing P and Q so that $P \cap Q = \varphi$ is

Options: A. $2^{2n-2n}C_n$ 

B.

 $2^n$ 

C.

 $3^n - 1$ 

D.

 $3^n$ 

#### Answer: D

\_\_\_\_\_

### **Question 31**

Under which of the following condition(s) does(do) the system of equations  $\begin{pmatrix} 1 & 2 & 4 \\ 2 & 1 & 2 \\ 1 & 2 & (a-4) \end{pmatrix} \begin{pmatrix} x \\ y \\ z \end{pmatrix} = \begin{pmatrix} 6 \\ 4 \\ a \end{pmatrix}$  possesses(possess) unique solution ?

**Options:** 

A.

 $\forall a \in R$ 

B.

a = 8

C.

for all integral values of a

D.

Answer: D

### **Question 32**

If 
$$\Delta(x) = egin{pmatrix} x-2 & (x-1)^2 & x^3 \ x-1 & x^2 & (x+1)^3 \ x & (x+1)^2 & (x+2)^3 \end{bmatrix}$$
, then coefficient of x in  $\Delta x$ 

\_\_\_\_\_

is

#### **Options:**

A. 2 B. -2 C. 3 D. -4 Answer: B

-----

\_\_\_\_\_

### **Question 33**

If  $p = \begin{bmatrix} 1 & \alpha & 3 \\ 1 & 3 & 3 \\ 2 & 4 & 4 \end{bmatrix}$  is the adjoint of the 3 × 3 matrix A and det A = 4, then  $\alpha$  is equal to

**Options:** 

A.			
4			
B.			
11			
C.			
5			
D.			
0			

#### Answer: B

\_\_\_\_\_

### **Question 34**

If 
$$A = \begin{pmatrix} 1 & 1 \\ 0 & i \end{pmatrix}$$
 and  $A^{2018} = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$ , then  $(a+d)$  equals

#### **Options:**

A. 1+i B. 0 C. 2 D. 2018 Answer: B

### **Question 35**

# Let S, T, U be three non-void sets and $f: S \to T, g: T \to U$ and composed mapping g. $f: S \to U$ be defined. Let g. f be injective mapping. Then

#### **Options:**

A.

f, g both are injective.

B.

neither f nor g is injective.

C.

f is obviously injective.

D.

g is obviously injective.

Answer: C

\_\_\_\_\_

### **Question 36**

For the mapping  $f: R - \{1\} \rightarrow R - \{2\}$ , given by  $f(x) = \frac{2x}{x-1}$ , which of the following is correct?

#### **Options:**

A.

f is one-one but not onto

B.

f is onto but not one-one

C.

f is neither one-one nor onto

D.

f is both one-one and onto

Answer: D

#### \_\_\_\_\_

### **Question 37**

A, B, C are mutually exclusive events such that  $P(A) = \frac{3x+1}{3}$ ,  $P(B) = \frac{1-x}{4}$  and  $P(C) = \frac{1-2x}{2}$ . Then the set of possible values of x are in

**Options:** 

А.		
[0, 1]		
В.		
$\left[rac{1}{3},rac{1}{2} ight]$		
C.		
$\left[\frac{1}{3},\frac{2}{3}\right]$		
D.		
$\left[rac{1}{3},rac{13}{3} ight]$		
Answer: B		

### **Question 38**

A determinant is chosen at random from the set of all determinants of order 2 with elements 0 or 1 only. The probability that the determinant chosen is non-zero is

**Options:** 

A.

 $\frac{3}{16}$ 

B.

<u>3</u> 8	
C.	
$\frac{1}{4}$	
D.	
<u>5</u> 8	
Answer: C	

\_\_\_\_\_

### **Question 39**

If  $(\cot \alpha_1)(\cot \alpha_2) \dots (\cot \alpha_n) = 1, 0 < \alpha_1, \alpha_2, \dots, \alpha_n < \pi/2$ , then the maximum value of  $(\cos \alpha_1)(\cos \alpha_2) \dots (\cos \alpha_n)$  is given by

**Options:** 

-----

### **Question 40**

If the algebraic sum of the distances from the points (2, 0), (0, 2) and (1, 1) to a variable straight line be zero, then the line passes through the fixed point

#### **Options:**

А.	
(-1, 1)	
B.	
(1, -1)	
C.	
(-1, -1)	
D.	
(1, 1)	
Answer: D	

\_\_\_\_\_

### **Question 41**

#### The side AB of $\triangle$ ABC is fixed and is of length 2a unit. The vertex moves in the plane such that the vertical angle is always constant and is $\alpha$ . Let x-axis be along AB and the origin be at A. Then the locus of the vertex is

**Options:** 

```
A.

x^{2} + y^{2} + 2ax \sin \alpha + a^{2} \cos \alpha = 0
B.

x^{2} + y^{2} - 2ax - 2ay \cot \alpha = 0
C.

x^{2} + y^{2} - 2ax \cos \alpha - a^{2} = 0
D.

x^{2} + y^{2} - ax \sin \alpha - ay \cos \alpha = 0
Answer: B
```

### **Question 42**

## If the sum of the distances of a point from two perpendicular lines in a plane is 1 unit, then its locus is

#### **Options:**

A.

a square

B.

a circle

C.

a straight line

D.

two intersecting lines

Answer: A

-----

### **Question 43**

A line passes through the point (-1, 1) and makes an angle  $\sin^{-1}\left(\frac{3}{5}\right)$  in the positive direction of x-axis. If this line meets the curve  $x^2 = 4y - 9$  at A and B, then |AB| is equal to

**Options:** 

A.

 $\frac{4}{5}$  unit

B.

 $\frac{5}{4}$  unit

C.

 $\frac{3}{5}$  unit

D.

 $\frac{5}{3}$  unit

Answer: B

\_\_\_\_\_

### **Question 44**

Two circles  $S_1 = px^2 + py^2 + 2g'x + 2f'y + d = 0$  and  $S_2 = x^2 + y^2 + 2gx + 2fy + d' = 0$  have a common chord PQ. The equation of PQ is

**Options:** 

A.  $S_1 - S_2 = 0$ B.  $S_1 + S_2 = 0$ C.  $S_1 - pS_2 = 0$ D.  $S_1 + pS_2 = 0$ Answer: C

### **Question 45**

Let  $P(3 \sec \theta, 2 \tan \theta)$  and  $Q(3 \sec \phi, 2 \tan \phi)$  be two points on  $\frac{x^2}{9} - \frac{y^2}{4} = 1$  such that  $\theta + \phi = \frac{\pi}{2}, 0 < \theta, \phi < \frac{\pi}{2}$ . Then the ordinate of the point of intersection of the normals at P and Q is

**Options:** 

$\frac{13}{2}$		
B.		
$-\frac{13}{2}$		
C.		
$\frac{5}{2}$		
D.		
$-\frac{5}{2}$		
Answer: A		

\_\_\_\_\_

### **Question 46**

Let P be a point on (2, 0) and Q be a variable point on  $(y - 6)^2 = 2(x - 4)$ . Then the locus of mid-point of PQ is

**Options:** 

A.  $y^{2} + x + 6y + 12 = 0$ B.  $y^{2} - x + 6y + 12 = 0$ C.  $y^{2} + x - 6y + 12 = 0$ D.  $y^{2} - x - 6y + 12 = 0$ Answer: D

-----

**Question 47** 

AB is a chord of a parabola  $y^2 = 4ax$ , (a > 0) with vertex A. BC is drawn perpendicular to AB meeting the axis at C. The projection of BC on the axis of the parabola is

Options:		
А.		
a unit		
B.		
2a unit		
C.		
8a unit		
D.		
4a unit		
Answer: D		

-----

# **Question 48**

AB is a variable chord of the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ . If AB subtends a right angle at the origin O, then  $\frac{1}{OA^2} + \frac{1}{OB^2}$  equals to

**Options:** 

 $\frac{1}{a^2} + \frac{1}{b^2}$ B.  $\frac{1}{a^2} - \frac{1}{b^2}$ C.  $a^2 + b^2$ 

A.

u +

D.

 $a^2 - b^2$ 

Answer: A

\_\_\_\_\_

# **Question 49**

# The equation of the plane through the intersection of the planes x + y + z = 1 and 2x + 3y - z + 4 = 0 and parallel to the x-axis is

**Options:** 

A. y + 3z + 6 = 0B. y + 3z - 6 = 0C. y - 3z + 6 = 0D. y - 3z - 6 = 0Answer: C

-----

# **Question 50**

The line x - 2y + 4z + 4 = 0, x + y + z - 8 = 0 intersect the plane x - y + 2z + 1 = 0 at the point

#### **Options:**

A.

 $\left(-2,5,1
ight)$ 

Β.

(2,-5,1)

\_\_\_\_\_

# **Question 51**

If I is the greatest of 
$$I_1 = \int_0^1 e^{-x} \cos^2 x \, dx, I_2 = \int_0^1 e^{-x^2} \cos^2 x \, dx,$$
 $I_3 = \int_0^1 e^{-x^2} dx, I_4 = \int_0^1 e^{-x^2/2} dx$ , then

#### **Options:**

A.

 $I = I_1$ 

B.

 $I = I_2$ 

C.

 $I = I_3$ 

D.

 $I = I_4$ 

#### Answer: D

-----

### **Question 52**

 $\lim_{x
ightarrow\infty}\Big(rac{x^2+1}{x+1}-ax-b\Big),(a,b\in R)$  = 0. Then

### **Options:**

A. a = 0, b = 1B. a = 1, b = -1C. a = -1, b = 1D. a = 0, b = 0Answer: B

\_\_\_\_\_

## **Question 53**

If the transformation  $z = \log \tan \frac{x}{2}$  reduces the differential equation

 $\frac{d^2y}{dx^2} + \cot x \frac{dy}{dx} + 4y \cos ec^2 x = 0$  into the form  $\frac{d^2y}{dz^2} + ky = 0$  then k is equal to

#### **Options:**

A. -4 B. 4 C. 2 D. -2

Answer: B

From the point (-1, -6), two tangents are drawn to  $y^2 = 4x$ . Then the angle between the two tangents is

**Options:** 

А.		
$\pi/3$		
В.		
$\pi/4$		
С.		
$\pi/6$		
D.		
$\pi/2$		
Answer: D		

-----

# **Question 55**

If  $\overrightarrow{\alpha}$  is a unit vector,  $\overrightarrow{\beta} = \hat{i} + \hat{j} - \hat{k}, \overrightarrow{\gamma} = \hat{i} + \hat{k}$  then the maximum value of  $\left[\overrightarrow{\alpha}\overrightarrow{\beta}\overrightarrow{\gamma}\right]$  is

**Options:** 

A.

3

B.

 $\sqrt{3}$ 

C.

2		
D.		
$\sqrt{6}$		
Answer: D		

```
_____
```

The maximum value of  $f(x) = e^{\sin x} + e^{\cos x}; x \in R$  is

### **Options:**

А.			
2e			
B.			
$2\sqrt{e}$			
C.			
$2e^{rac{1}{\sqrt{2}}}$			
D.			
$2e^{-rac{1}{\sqrt{2}}}$			
Answer: C			

# **Question 57**

A straight line meets the co-ordinate axes at A and B. A circle is circumscribed about the triangle OAB, O being the origin. If m and n are the distances of the tangent to the circle at the origin from the points A and B respectively, the diameter of the circle is

m(m + n)
В.
m + n
C.
n(m + n)
D.
$\frac{1}{2}(m+n)$
Answer: B

Let the tangent and normal at any point P(at<sup>2</sup>, 2at), (a > 0), on the parabola  $y^2 = 4ax$  meet the axis of the parabola at T and G respectively. Then the radius of the circle through P, T and G is

**Options:** 

A.  $a(1+t^2)$ B.  $(1+t)^2$ C.  $a(1-t^2)$ D.  $(1-t^2)$ Answer: A

# **Question 59**

The value of a for which the sum of the squares of the roots of the equation  $x^2 - (a - 2)x - a - 1 = 0$  assumes the least value is Options: A. 0 B. 1 C. 2 D. 3 Answer: B

-----

# **Question 60**

If x satisfies the inequality  $\log_{25} x^2 + (\log_5 x)^2 < 2$ , then x belongs to

### **Options:**

A.  $(\frac{1}{5}, 5)$ B.  $(\frac{1}{25}, 5)$ C.  $(\frac{1}{5}, 25)$ D.  $(\frac{1}{25}, 25)$ Answer: B

The solution of  $\det(A - \lambda I_2) = 0$  be 4 and 8 and  $A = \begin{pmatrix} 2 & 2 \\ x & y \end{pmatrix}$ . Then

### (I<sub>2</sub> is identity matrix of order 2)

### **Options:**

A. x = 4, y = 10B. x = 5, y = 8C. x = 3, y = 9D. x = -4, y = 10Answer: D

------

# **Question 62**

If  $P_1P_2$  and  $P_3P_4$  are two focal chords of the parabola  $y^2 = 4ax$  then the chords  $P_1P_3$  and  $P_2P_4$  intersect on the

### **Options:**

A.

directrix of the parabola

B.

axis of the parabola

C.

latus-rectum of the parabola

D.

y-axis

Answer: A

-----

# **Question 63**

 $f: X o R, X = \{x | 0 < x < 1\}$  is defined as  $f(x) = rac{2x-1}{1-|2x-1|}.$  Then

### **Options:**

### A.

f is only injective

#### B.

f is only surjective

#### C.

f is bijective

D.

f is neither injective nor surjective

Answer: A

\_\_\_\_\_

# **Question 64**

Let f be a non-negative function defined in  $[0, \pi/2]$ , f' exists and be continuous for all x and  $\int_{0}^{x} \sqrt{1 - (f'(t))^2} dt = \int_{0}^{x} f(t) dt$  and f (0) = 0. Then

A.  $f(\frac{1}{2}) < \frac{1}{2}$  and  $f(\frac{1}{3}) < \frac{1}{3}$ B.  $f(\frac{1}{2}) > \frac{1}{2}$  and  $f(\frac{1}{3}) < \frac{1}{3}$ C.  $f(\frac{4}{3}) < \frac{4}{3}$  and  $f(\frac{2}{3}) < \frac{2}{3}$ D.  $f(\frac{4}{3}) > \frac{4}{3}$  and  $f(\frac{2}{3}) > \frac{2}{3}$ Answer: C

# **Question 65**

PQ is a double ordinate of the hyperbola  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$  such that  $\Delta OPQ$  is an equilateral triangle, O being the centre of the hyperbola. Then the eccentricity e of the hyperbola satisfies

**Options:** 

A.  $1 < e < \frac{2}{\sqrt{3}}$ B.  $e = \frac{2}{\sqrt{3}}$ C.  $e = 2\sqrt{3}$ D.  $e > \frac{2}{\sqrt{3}}$ Answer: D

From a balloon rising vertically with uniform velocity v ft/sec a piece of stone is let go. The height of the balloon above the ground when the stone reaches the ground after 4 sec is  $[g = 32 \text{ ft/sec}^2]$ 

<b>Options:</b>
-----------------

А.
220 ft
В.
240 ft
С.
256 ft
D.
260 ft
Answer: C

# **Question 67**

Let  $f(x) = x^2 + x \sin x - \cos x$ . Then

### **Options:**

### A.

f(x) = 0 has at least one real root

#### B.

f(x) = 0 has no real root

C.

f(x) = 0 has at least one positive root

D.

#### Answer: D

-----

# **Question 68**

### Let $z_1$ and $z_2$ be two non-zero complex numbers. Then

#### **Options:**

A.

Principal value of  $arg(z_1z_2)$  may not be equal to Principal value of  $argz_1$  + Principal value of  $arg z_2$ 

#### B.

Principal value of  $arg(z_1z_2) = Principal value of arg z_1 + Principal value of arg z_2$ 

#### C.

Principal value of  $arg(z_1/z_2)$  = Principal value of  $argz_1$  – Principal value of  $arg z_2$ 

#### D.

Principal value of  $arg(z_1/z_2)$  may not be  $argz_1 - arg z_2$ 

#### Answer: D

\_\_\_\_\_

# **Question 69**

Let 
$$\Delta = \begin{vmatrix} \sin\theta\cos\phi & \sin\theta\sin\phi & \cos\theta \\ \cos\theta\cos\phi & \cos\theta\sin\phi & -\sin\theta \\ -\sin\theta\sin\phi & \sin\theta\cos\phi & 0 \end{vmatrix}$$
. Then

#### **Options:**

A.

 $\Delta$  is independent of  $\theta$ 

B.

 $\Delta$  is independent of arphi

C.

 $\Delta$  is a constant

D.

 $\left(\frac{d\Delta}{d\theta}\right)_{\theta=rac{\pi}{2}}=0$ 

Answer: D

\_\_\_\_\_

# **Question 70**

### Let R and S be two equivalence relations on a non-void set A. Then

### **Options:**

A.

 $R \cup S$  is equivalence relation

B.

 $R \cap S$  is equivalence relation

C.

 $R \cap S$  is not equivalence relation

D.

 $R \cup S$  is not equivalence relation

Answer: B

-----

# **Question 71**

# Chords of an ellipse are drawn through the positive end of the minor axis. Their midpoint lies on

a circle

B.

a parabola

C.

an ellipse

D.

a hyperbola

Answer: C

\_\_\_\_\_

# **Question 72**

### Consider the equation $y - y_1 = m(x - x_1)$ . If m and $x_1$ are fixed and different lines are drawn for different values of $y_1$ , then

### **Options:**

A.

the lines will pass through a fixed point

B.

there will be a set of parallel lines

C.

all lines intersect the line  $x = x_1$ 

### D.

all lines will be parallel to the line  $y = x_1$ 

### Answer: C

-----

# **Question 73**

# Let p(x) be a polynomial with real co-efficient, p(0) = 1 and p'(x) > 0 for all $x \in R$ . Then

### **Options:**

A.

p(x) has at least two real roots

B.

p(x) has only one positive real root

C.

p(x) may have negative real root

D.

p(x) has infinitely many real roots

Answer: C

-----

# **Question 74**

Twenty metres of wire is available to fence off a flower bed in the form of a circular sector. What must the radius of the circle be, if the area of the flower bed be greatest?

A.		
10 m		
B.		
4 m		
C.		
5 m		
D.		
6 m		

#### \_\_\_\_\_

# **Question 75**

### The line y = x + 5 touches

### **Options:**

A.

the parabola  $y^2 = 20 x$ 

B.

the ellipse  $9x^2 + 16y^2 = 144$ 

C.

the hyperbola  $\frac{x^2}{29} - \frac{y^2}{4} = 1$ 

D.

the circle  $x^2 + y^2 = 25$ 

#### Answer: C

# Chemistry

# **Question 76**

A sample of MgCO<sub>3</sub> is dissolved in dil. HCl and the solution is neutralized with ammonia and buffered with  $NH_4Cl / NH_4OH$ . Disodium hydrogen phosphate reagent is added to the resulting solution. A white precipitate is formed. What is the formula of the precipitate?

**Options:** 

A.

 $Mg_3(PO_4)_2$ 

B.

Mg(NH<sub>4</sub>)PO<sub>4</sub>

C.

MgHPO<sub>4</sub>

D.

 $Mg_2P_2O_7$ 

Answer: B

\_\_\_\_\_

# **Question 77**

### XeF<sub>2</sub>, NO<sub>2</sub>, HCN, ClO<sub>2</sub>, CO<sub>2</sub>.

# Identify the non-linear molecule-pair from the above mentioned molecules.

**Options:** 

A.

 $XeF_2$ ,  $ClO_2$ 

B.

 $CO_2$ ,  $NO_2$ 

C.

 $\mathrm{HCN},\mathrm{NO}_2$ 

D.

 $ClO_2$ ,  $NO_2$ 

Answer: D

\_\_\_\_\_

# The number of atoms in body centred and face centred cubic unit cell respectively are

Options:	
Α.	
2 and 4	
В.	
4 and 3	
C.	
1 and 2	
D.	
4 and 6	
Answer: A	

# **Question 79**

# The number of unpaired electron in Mn<sup>2+</sup> ion is

**Options:** 

A.
2
B.
3
C.
5
D.
6

Answer: C

#### \_\_\_\_\_

# **Question 80**

# The average speed of $H_2$ at $T_1K$ is equal to that of $O_2$ at $T_2K$ . The ratio $T_1: T_2$ is

#### **Options:**

А.		
1 : 16		
B.		
16 : 1		
C.		
1:4		
D.		
1:1		
Answer: A		

\_\_\_\_\_

# **Question 81**

### Sodium nitroprusside is :

### **Options:**

A.

```
Na_4[Fe(CN)_5NO_2]
```

B.

 $Na_2[Fe(CN)_5NO]$ 

C.

 $Na_3[Fe(CN)_5NO]$ 

 $Na_4[Fe(CN)_5NO_3]$ 

#### Answer: B

\_\_\_\_\_

# **Question 82**

Choose the correct statement for the  $[Ni(CN)_4]^{2-}$  complex ion (Atomic no. of Ni = 28)

### **Options:**

A.

The complex is square planar and paramagnetic.

B.

The complex is tetrahedral and diamagnetic.

C.

The complex is square planar and diamagnetic.

D.

The complex is tetrahedral and paramagnetic.

### Answer: C

\_\_\_\_\_

# **Question 83**

The boiling point of the water is higher than liquid HF. The reason is that

### **Options:**

A.

Hydrogen bonds are stronger in water.

B.

Hydrogen bonds are stronger in HF.

C.

Hydrogen bonds are larger in number in HF.

D.

Hydrogen bonds are larger in number in water.

### Answer: D

\_\_\_\_\_

# **Question 84**

# The metal-pair that can produce nascent hydrogen in alkaline medium is :

 Options:

 A.

 Zn, Al

 B.

 Fe, Ni

 C.

 Al, Mg

 D.

 Mg, Zn

 Answer: A

------

# **Question 85**

### The correct bond order of B-F bond in BF<sub>3</sub> molecule is :

1		
В.		
$1\frac{1}{2}$		
С.		
2		
D.		
$1\frac{1}{3}$		
Answer: D		

\_\_\_\_\_

# **Question 86**

### Which of the following is radioactive?

Options:
Α.
Hydrogen
В.
Deuterium
C.
Tritium
D.
none
Answer: C

# **Question 87**

The correct order of acidity of the following hydra acids is

### **Options:**

```
A.
HF > HCl > HBr > HI
B.
HF < HCl < HBr < HI
C.
HF < HCl > HBr > HI
D.
HF > HCl < HBr > HI
```

**Answer: B** 

# **Question 88**

To a solution of colourless sodium salt, a solution of lead nitrate was added to have a white precipitate which dissolves in warm water and reprecipitates on cooling. Which of the following acid radical is present in the salt?

А.	
Cl <sup>-</sup>	
B.	
$\mathrm{SO}_4^{2-}$	
C.	
s <sup>2–</sup>	
D.	
$NO_3^-$	
Answer: A	

### Oxidation states of Cr in K<sub>2</sub>Cr<sub>2</sub>O<sub>7</sub> and CrO<sub>5</sub> are respectively

### **Options:**

A. +6, +5 B. +6, +10 C. +6, +6 D.

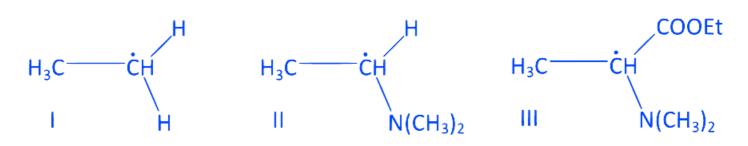
None of these

Answer: C

-----

# **Question 90**

### The correct order of relative stability for the given free radicals is :



### **Options:**

A.

II > I > III

I < III > III > I	
C.	
III > I > II	
D.	
II > II > I	
Answer: D	

\_\_\_\_\_

# **Question 91**

### Image

### Hybridisation of the negative carbons in (1) and (2) are

**Options:** 

A.

 $\mathrm{sp}^2$  and  $\mathrm{sp}^3$ 

B.

 ${\rm sp}^3$  and  ${\rm sp}^2$ 

C.

both  $\mathrm{sp}^2$ 

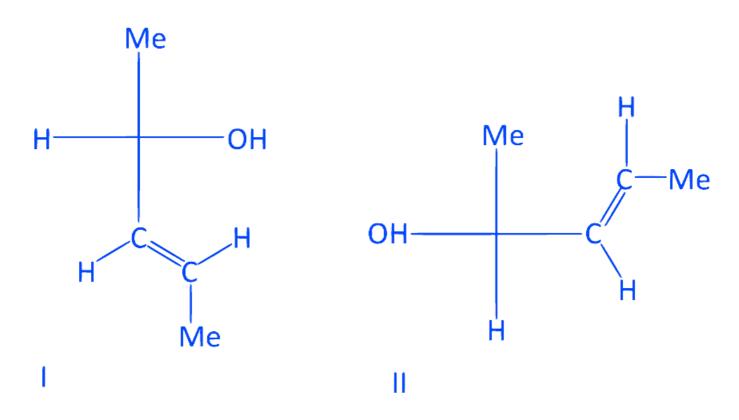
D.

both  $sp^3$ 

### Answer: B

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# **Question 92**



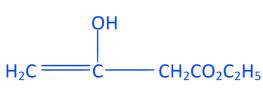
### The correct relationship between molecules I and II is

Options:
Α.
Enantiomer
В.
Homomer
C.
Diastereomer
D.
Constitutional isomer
Answer: B

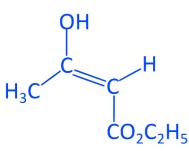
# **Question 93**

### The enol form in which ethyle-3-oxobutanoate exists is

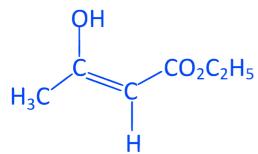




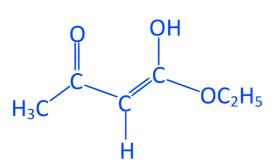




C.







### Answer: C

\_\_\_\_\_

# **Question 94**

# How many monobriminated product(s) (including stereoisomers) would form in the free radical bromination of n-butane?

**Options:** 

А.		
2		
B.		
1		
C.		
3		
D.		
4		
Answer: C		

\_\_\_\_\_

# **Question 95**

### What is the correct order of acidity of salicylic acid, 4hydroxybenzoic acid, and 2, 6-dihydroxybenzoic acid ?

### **Options:**

A.

2, 6-dihydroxybenzoic acid > salicylic acid > 4-hydroxybenzoic acid

B.

2, 6-dihydroxybenzoic acid > 4-hydroxybenzoic acid > salicylic acid

C.

salicylic acid > 2, 6-dihydroxybenzoic acid > 4-hydroxybenzoic acid

D.

salicylic acid > 4-hydroxybenzoic acid > 2, 6-dihydroxybenzoic acid

Answer: A

#### \_\_\_\_\_

# **Question 96**

### How much solid oxalic acid (Molecular weight 126) has to be weighed to prepare 100 ml. exactly 0.1 (N) oxalic acid solution in water?

 Options:

 A.

 1.26 g

 B.

 0.126 g

 C.

 0.63 g

 D.

 0.063 g

 Answer: C

## **Question 97**

### The major product of the following reaction is

\_\_\_\_\_

 $F_3C-CH=CH_2+HBr
ightarrow$ 

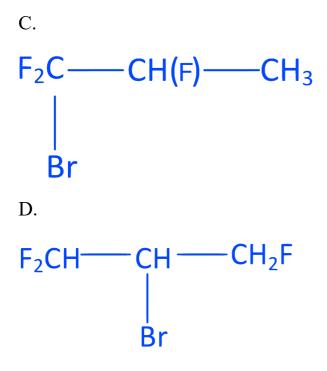
#### **Options:**

A.

 $F_3C - CH_2 - CH_2Br$ 

B.

 $F_3C - CH(Br) - CH_3$ 

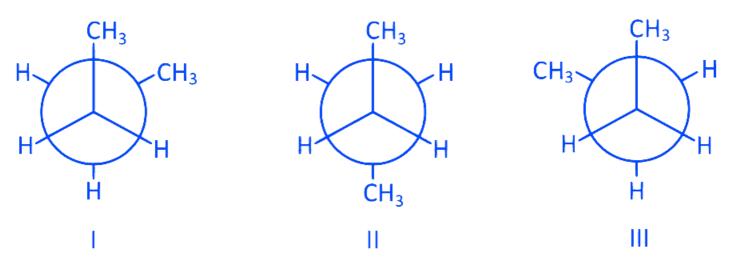


Answer: A

------

## **Question 98**

The correct order of relative stability of the given conformers of nbutane is



Options:
А.
II > I = III
В.
II > III > I
С.
II > I > III
D.
I = III > II
Answer: A

-----

# **Question 99**

### $C_6H_6(liq)+rac{15}{2}O_2(g) ightarrow 6CO_2(g)+3H_2O(liq)$

Benzene burns in oxygen according to the above equation. What is the volume of oxygen (at STP) needed for complete combustion of 39 gram of liquid benzene?

**Options:** 

A.

11.2 litre

B.

22.4 litre

C.

84 litre

D.

168 litre

Answer: C

\_\_\_\_\_

# **Question 100**

### Avogadro's law is valid for

### **Options:**

A.

all gases

Β.

ideal gas

C.

Van der Waals gas

D.

real gas

Answer: B

\_\_\_\_\_

# Question 101

A metal (M) forms two oxides. The ratio M:O (by weight) in the two oxides are 25:4 and 25:6. The minimum value of atomic mass of M is

А.		
50		
В.		
100		
С.		
150		
D.		
200		
Answer: B		

The de-Broglie wavelength ( $\lambda$ ) for electron (e), proton (p) and He<sup>2+</sup> ion ( $\alpha$ ) are in the following order. Speed of e, p and  $\alpha$  are the same

**Options:** 

A.  $\alpha > p > e$ B.  $e > p > \alpha$ C.  $e > \alpha > p$ D.  $\alpha e$ Answer: B

# **Question 103**

1 mL of water has 25 drops. Let  $N_0$  be the Avogadro number. What is the number of molecules present in 1 drop of water ? (Density of water = 1 g/mL)

**Options:** 

А.		
$\frac{0.02}{9}N_0$		
B.		
$\frac{18}{25}N_0$		
C.		
$\frac{25}{18}N_0$		
D.		
$\frac{0.04}{25}N_0$		
Answer: A		

\_\_\_\_\_

# **Question 104**

In Bohr model of atom, radius of hydrogen atom in ground state is  $r_1$  and radius of He<sup>+</sup> ion in ground state is  $r_2$ . Which of the following is correct?

**Options:** 

A. $\frac{r_1}{r_2} = 4$ B. $\frac{r_1}{r_2} = \frac{1}{2}$ C.

 $rac{r_1}{r_2} = rac{1}{4}$ 

D.

 $rac{r_2}{r_1}=rac{1}{2}$ 

Answer: D

-----

## **Question 105**

Which one of the following is the correct set of four quantum numbers (n, 1, m, s) ?

**Options:** 

A.  $(3, 0, -1, +\frac{1}{2})$ B.  $(4, 3, -2, -\frac{1}{2})$ C.  $(3, 1, -2, -\frac{1}{2})$ D.  $(4, 2, -3, +\frac{1}{2})$ Answer: B

\_\_\_\_\_

# **Question 106**

Let  $(C_{rms})_{H_2}$  is the r.m.s. speed of  $H_2$  at 150 K. At what temperature, the most probable speed of helium  $[C_{mp})_{He}$  will be half of  $(C_{rms})_{H_2}$ ?

**Options:** 

A.

75 K

В.
112.5 K
C.
225 K
D.
900 K
Answer: B

-----

## **Question 107**

#### The correct pair of electron affinity order is

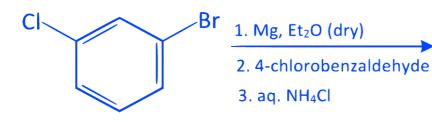
#### **Options:**

A. O > S, F > ClB. O < S, Cl > FC. S > O, F > ClD. S < O, Cl > FAnswer: B

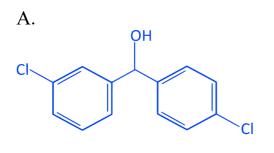
## **Question 108**

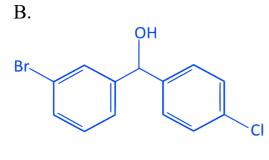
The product of the following reaction is :

\_\_\_\_\_

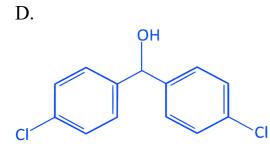


**Options:** 







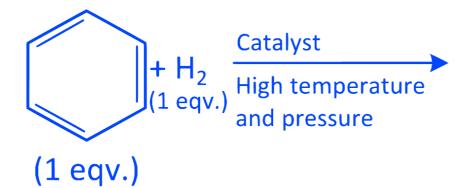


Answer: A

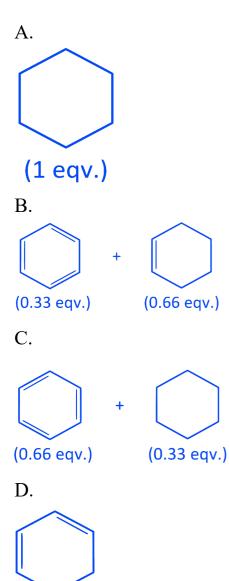
\_\_\_\_\_

## **Question 109**

The product of the following hydrogenation reaction is:



#### **Options:**



(1 eqv.)

## **Question 110**

#### Pick the correct statement.

#### **Options:**

A.

Relative lowering of vapour pressure is independent of T.

B.

Osmotic pressure always depends on the nature of solute.

C.

Elevation of boiling point is independent of nature of the solvent.

D.

Lowering of freezing point is proportional to the molar concentration of solute.

\_\_\_\_\_

#### Answer: A

\_\_\_\_\_

## **Question 111**

## During the preparation of NH<sub>3</sub> in Haber's process, the promoter(s) used is/are -

#### **Options:**

A.

 $PtO_2$ 

B.

Mo

C.

```
Mix of Al_2O_3 and K_2O
```

#### D.

Fe and Mn

Answer: C

\_\_\_\_\_

## **Question 112**

### The correct statement(s) about B<sub>2</sub>H<sub>6</sub> is /are :

#### **Options:**

A.

All B atoms are sp<sup>3</sup> hybridised.

B.

It is paramagnetic.

C.

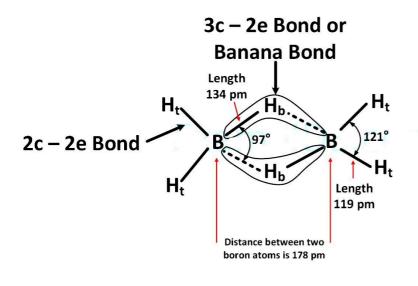
It contains 3C - 4C bonding.

D.

There are two types of H present.

Answer: D

Solution:



#### H<sub>t</sub> – Terminal Hydrogen H<sub>b</sub> – Bridge Hydrogen

It has two 3-centre-2-electron bonds and four 2-centre-2-electron bonds.

\_\_\_\_\_

## **Question 113**

## Which of the following would produce enantiomeric products when reacted with methyl magnesium iodide?

**Options:** 

A.

Benzaldehyde

В.

Propiophenone

C.

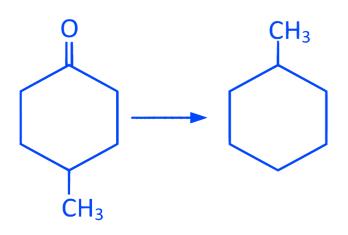
Acetone

D.

Acetaldehyde

Answer: B

## **Question 114**



#### The above conversion can be carried out by,

#### **Options:**

A.

Zn - Hg/Conc. HCl

B.

i. H<sub>2</sub>NNH<sub>2</sub> ii. NaOH in ethylene glycol,  $\Delta$ 

C.

i. HSCH<sub>2</sub>CH<sub>2</sub>SH/H<sup>⊕</sup> ii. H<sub>2</sub>/Ni

D.

Bromine water

Answer: C

## **Question 115**

#### Which of the statements are incorrect?

#### **Options:**

A.

pH of a solution of salt of strong acid and weak base is less than 7.

#### B.

pH of a solution of a weak acid and weak base is basic if  $K_b < K_a$ .

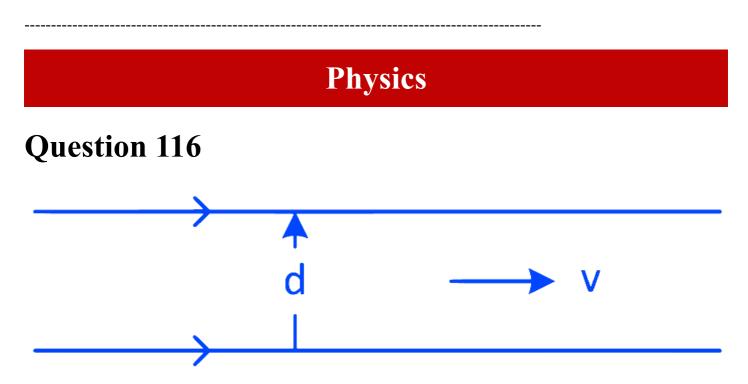
#### C.

pH of an aqueous solution of  $10^{-8}$  (M) HCl is 8.

#### D.

Conjugate acid of  $NH_2^-$  is  $NH_3$ .

#### Answer: C



Two infinite line-charges parallel to each other are moving with a constant velocity v in the same direction as shown in the figure. The separation between two line-charges is d. The magnetic attraction

## balances the electric repulsion when, [ c = speed of light in free space ]

**Options:** 

A.  $v = \sqrt{2}c$ B.  $v = \frac{c}{\sqrt{2}}$ C. v = cD.  $v = \frac{c}{2}$ 

#### Answer: C

#### Solution:

Electric field due to line charge is given by

$$E=rac{\lambda}{2\piarepsilon_0 d}$$

where,  $\lambda$  = linear charge density.

$$\lambda = rac{q}{l} \Rightarrow q = \lambda l$$

Electric force due to one wire on another wire,

$$egin{aligned} F_E &= q \,.\, E \ &= \lambda l \,.\, rac{\lambda}{2\piarepsilon_0 d} \ &\Rightarrow F_E &= rac{\lambda^2 l}{2\piarepsilon_0 d} \end{aligned}$$

Now, current due to moving charged wire is given as

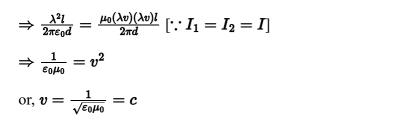
$$egin{aligned} I &= rac{dq}{dt} = rac{d}{dt} (\lambda dl) \left[\because v = rac{dl}{dt}
ight] \ &= \lambda v \end{aligned}$$

Magnetic force on one wire due to another wire,

$$F_B = rac{\mu_0 I_1 I_2 l}{2\pi d}$$

Since, both forces balance each other, thus

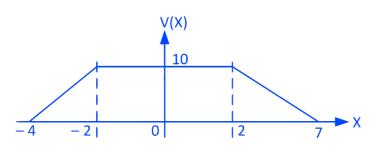
 $F_E = F_B$ 



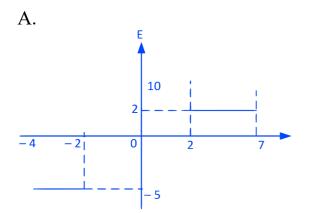
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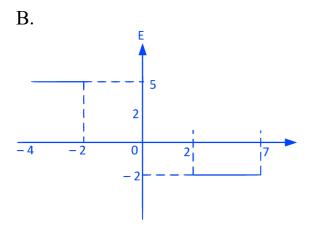
## **Question 117**

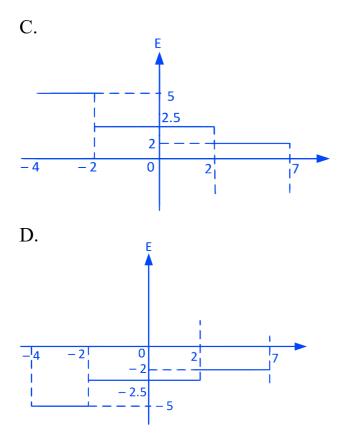
The electric potential for an electric field directed parallel to X-axis is shown in the figure. Choose the correct plot of electric field strength.



```
Options:
```







#### Answer: A

#### Solution:

We know that,  $E = -\frac{dV}{dr}$ 

Thus, electric field from (-4 to -2),

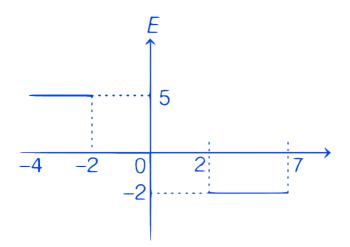
$$E = -\left(rac{10-0}{4-(-2)}
ight) = rac{10}{2} = 5$$
 N/C

Electric field from (-2 to 2),

$$E=-\left(rac{10-10}{2-(-2)}
ight)=0$$

Electric field from (2 to 7),

$$E = -\left(\frac{10-0}{2-7}\right) = -2$$
 N/C



## **Question 118**

An electron revolves around the nucleus in a circular path with angular momentum  $\overrightarrow{L}$ . A uniform magnetic field  $\overrightarrow{B}$  is applied perpendicular to the plane of its orbit. If the electron experiences a torque  $\overrightarrow{T}$ , then

**Options:** 

A.

 $\overrightarrow{T}||\overrightarrow{L}$ 

B.

 $\overrightarrow{T}$  is anti-parallel to  $\overrightarrow{L}$ 

C.

 $\overrightarrow{T}$ .  $\overrightarrow{L} = 0$ 

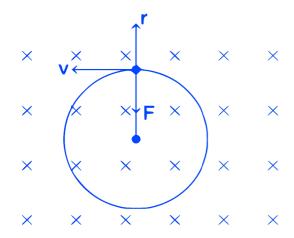
D.

Angle between  $\overrightarrow{T}$  and  $\overrightarrow{L}$  is  $45^{\circ}$ 

Answer: C

#### Solution:

According to the question, given situation can be represented by the figure below.



From the Lorentz force, we have

$$F = q(v imes B)$$

Hence, force is acting directly towards the centre.

Thus, both angular momentum ( $\mathbf{L}$ ) and torque ( $\mathbf{T}$ ) will have the same direction. i.e.  $\mathbf{T} \parallel \mathbf{L}$ .

\_\_\_\_\_

### **Question 119**

A straight wire is placed in a magnetic field that varies with distance x from origin as  $\overrightarrow{B} = B_0 \left(2 - \frac{x}{a}\right) \widehat{k}$ . Ends of wire are at (a, 0) and (2a, 0) and it carries a current I. If force on wire is  $\overrightarrow{F} = IB_0 \left(\frac{ka}{2}\right) \widehat{j}$ , then value of k is

**Options:** 

A. 1 B. 5 C. -1 D.  $\frac{1}{2}$ 

Answer: A

#### Solution:

Given,  $B = B_0 \left(2 - \frac{x}{a}\right) \hat{k}$ Force on a current carrying wire is given as

 $dF = IB \cdot dl$   $\Rightarrow \int dF = \int IB_0 \left(2 - \frac{x}{a}\right) dx$   $\Rightarrow F = IB_0 \int_a^{2a} \left(2 - \frac{x}{a}\right) dx$   $= IB_0 \left|2x - \frac{x^2}{2a}\right|_a^{2a} = IB_0 \left(\frac{a}{2}\right)$ Therefore, the value of k is 1.

#### -----

## **Question 120**

In a closed circuit there is only a coil of inductance L and resistance 100  $\Omega$ . The coil is situated in a uniform magnetic field. All on a sudden, the magnetic flux linked with the circuit changes by 5 Weber. What amount of charge will flow in the circuit as a result?

**Options:** 

500 C

B.

0.05 C

C.

20 C

D.

Value of L is to be known to find the charge flown

#### Answer: B

#### Solution:

Given, change in flux,  $d\phi = 5$  Wb

Emf due to change in flux is given as

$$E=rac{d\phi}{dt}\Rightarrow E\,.\,dt=5$$

Now, it is given that,  $R = 100 \,\Omega$ 

Thus, current,  $I = \frac{V}{R} = \frac{E}{R}$  ..... (i)

Also,  $I = \frac{dq}{dt}$  ..... (ii)

where, *dq* is the charge flowing per unit time.

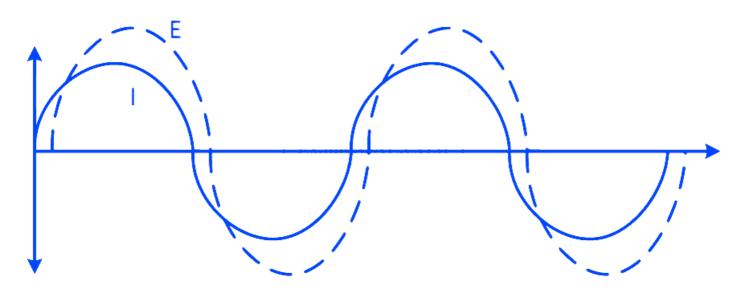
Thus, from Eqs. (i) and (ii), we have

$$rac{E}{R} = rac{dq}{dt} \Rightarrow rac{E \cdot dt}{R} = dq$$
 $\Rightarrow rac{5}{100} = dq \Rightarrow dq = 0.05 \, C$ 

\_\_\_\_\_

## **Question 121**

When an AC source of emf E with frequency  $\omega = 100$  Hz is connected across a circuit, the phase difference between E and current I in the circuit is observed to be  $\frac{\pi}{4}$  as shown in the figure. If the circuit consist of only RC or RL in series, then



#### **Options:**

A.

 $R = 1 k\Omega, C = 5 \mu F$ 

#### В.

 $R = 1 k \Omega$ , L = 10 H

C.

 $R = 1 k \Omega$ , L = 1 H

#### D.

 $R = 1 k\Omega, C = 10 \mu F$ 

#### Answer: D

#### Solution:

At any moment, the phase difference between current and voltage is given by

$$an \phi = rac{X_L}{R}$$

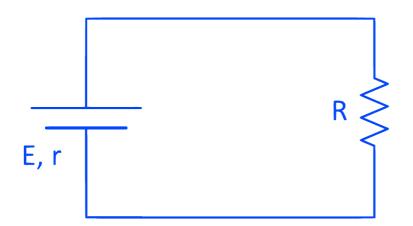
Since, voltage leads current by  $\frac{\pi}{4}$ , thus given circuit will be RL series circuit

$$\therefore \tan \frac{\pi}{4} = \frac{X_L}{R} \Rightarrow R = X_L = \omega L$$
  
From option (b),  $R = 1 k\Omega = 1000 \Omega$   
$$\therefore X_L = \omega L$$
  
$$= 100 \times 10 [\because \omega = 100 \text{ rad/s}]$$
  
$$= 1000 \Omega$$

Thus, the condition is satisfied. Hence, option (b) is correct.

\_\_\_\_\_

## **Question 122**



A battery of emf E and internal resistance r is connected with an external resistance R as shown in the figure. The battery will act as a constant voltage source if

**Options:** 

A. r << RB. r >> RC. r = RD.

It will never act as a constant voltage source.

#### Answer: A

#### Solution:

The constant voltage source provides a constant voltage to the load resistance regardless of variations or changes, in the load resistance. For this to happen, the source must have an internal resistance which is very low as compared to the resistance of the load.

i.e., **r** << **R** 

\_\_\_\_\_

## **Question 123**

# If the kinetic energies of an electron, an alpha particle and a proton having same de-Broglie wavelength are $\varepsilon_1, \varepsilon_2$ and $\varepsilon_3$ respectively, then

**Options:** 

A.  $\varepsilon_1 > \varepsilon_3 > \varepsilon_2$ B.  $\varepsilon_1 = \varepsilon_3 = \varepsilon_2$ C.  $\varepsilon_1 < \varepsilon_3 < \varepsilon_2$ D.  $\varepsilon_1 > \varepsilon_2 > \varepsilon_3$ Answer: A

#### Solution:

de-Broglie wavelength of a charged particle having energy  $\boldsymbol{\varepsilon}$  is given by

$$\lambda_p = rac{h}{\sqrt{2m_parepsilon_3}}$$

Since,  $\lambda_e = \lambda_{\alpha} = \lambda_p$  and  $m_{\alpha} = m_p = m_e$ 

Thus, we can say

 $\frac{1}{\sqrt{m_{\alpha}\varepsilon_2}} = \frac{1}{\sqrt{m_p\varepsilon_3}} = \frac{1}{\sqrt{m_e\varepsilon_1}}$  $\therefore \varepsilon_1 > \varepsilon_3 > \varepsilon_2$ 

\_\_\_\_\_

## **Question 124**

In a Young's double slit experiment, the intensity of light at a point on the screen where the path difference between the interfering waves is  $\lambda$ , ( $\lambda$  being the wavelength of light used) is I. The intensity at a point where the path difference is  $\frac{\lambda}{4}$  will be (assume two waves have same amplitude)

**Options:** 

A.		
zero		
B.		
Ι		
C.		
$\frac{I}{2}$		
D.		
$\frac{I}{4}$		
	C	

#### Answer: C

#### Solution:

Intensity at any point on the screen is given by

#### $I=4I_0\cos^2rac{\phi}{2}$

where,  $I_0$  is the intensity of either wave and  $\phi$  is the phase difference between two waves.

Phase difference  $(\phi) = \frac{2\pi}{\lambda} \times \text{path difference}$   $= \frac{2\pi}{\lambda} \times \lambda = 2\pi$   $\therefore I = 4I_0 \cos^2\left(\frac{2\pi}{2}\right)$   $= 4I_0 \cos^2(\pi) = 4I_0 = I$   $\Rightarrow I_0 = \frac{I}{4} \dots$  (i) When path difference is  $\frac{\lambda}{4}$ , then  $\phi = \frac{2\pi}{\lambda} \times \frac{\lambda}{4} = \frac{\pi}{2}$  $\therefore I = 4I_0 \cos^2\left(\frac{\pi}{4}\right) = 2I_0 = 2 \times \frac{I}{4} = \frac{I}{2}$ 

## **Question 125**

In Young's double slit experiment with a monochromatic light, maximum intensity is 4 times the minimum intensity in the interference pattern. What is the ratio of the intensities of the two interfering waves?

#### **Options:**

A.
1/9
B.
1/3
C.
1/16
D.
1/2
Answer: A

Solution:

Given,  $\frac{I_{\text{max}}}{I_{\text{min}}} = \frac{4}{1}$ 

Let  $I_1$  and  $I_2$  be the intensities of interfering waves,

then 
$$\frac{(\sqrt{I_2} + \sqrt{I_1})^2}{(\sqrt{I_2} - \sqrt{I_1})^2} = \frac{I_{\text{max}}}{I_{\text{min}}}$$
  
 $\Rightarrow \left(\frac{\sqrt{\frac{I_2}{I_1}} + 1}{\sqrt{\frac{I_2}{I_1}} - 1}\right)^2 = \frac{4}{1}$   
 $\Rightarrow \frac{\sqrt{\frac{I_2}{I_1}} + 1}{\sqrt{\frac{I_2}{I_1}} - 1} = \frac{2}{1} \Rightarrow \sqrt{\frac{I_2}{I_1}} = \frac{3}{1}$   
or,  $\frac{I_1}{I_2} = \frac{1}{9}$ 

-----

## **Question 126**

The human eye has an approximate angular resolution of  $\theta = 5.8 \times 10^{-4}$  rad and typical photo printer prints a minimum of 300 dpi (dots per inch, 1 inch = 2.54 cm). At what minimal distance d should a printed page be held so that one does not see the individual dots?

**Options:** 

A.

20.32 cm

B.

29.50 cm

C.

14.59 cm

D.

6.85 cm

Answer: C

#### Solution:

Given, angular resolution of human eye,

 $\theta = 5.8 imes 10^{-4}$  rad

The linear distance between two successive dots in a printer,

 $l = rac{2.54}{300} = 0.846 imes 10^{-2}$  cm

At a distance d cm, the gap l will subtend an angle which is given by

 $d = rac{l}{ heta} = rac{0.846 imes 10^{-2}}{5.8 imes 10^{-4}} = 14.59 ext{ cm}$ 

\_\_\_\_\_

## **Question 127**

Suppose in a hypothetical world the angular momentum is quantized to be even integral multiples of  $\frac{h}{2\pi}$ . The largest possible wavelength emitted by hydrogen atoms in visible range in a world according to Bohr's model will be,

(Consider hc = 1242 Mev-fm)

**Options:** 

A. 153 nm

B.

409 nm

C.

121 nm

```
D.
```

487 nm

#### Answer: D

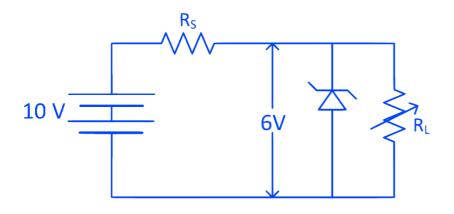
#### Solution:

$$E = 13.6 \left(rac{1}{n_1^2} - rac{1}{n_2^2}
ight)$$
 $= 13.6 \left(rac{1}{2^2} - rac{1}{4^2}
ight)$ 

= 13.6  $\left(\frac{1}{4} - \frac{1}{16}\right)$ = 2.55 eV Now, given that, hc = 1242 MeV-nm Hence,  $\lambda = \frac{hc}{2.55 \ eV} = \frac{1242 \ eV - nm}{2.55 \ eV}$ = 487 nm

## **Question 128**

A Zener diode having break down voltage Vz = 6V is used in a voltage regulator circuit as shown in the figure. The minimum current required to pass through the Zener to act as a voltage regulator is 10 mA and maximum allowed current through Zener is 40 mA. The maximum value of  $R_s$  for Zener to act as a voltage regulator is



**Options:** 

A.

100 **Ω** 

B.

400 **Ω** 

C.

0.4 **Ω** 

D.

950 **Ω** 

Answer: B

#### Solution:

Given,  $V_s = 10 V$  $V_z = 6 V$ Maximum current  $(I_{z \text{ max}}) = 40 \, mA = 40 \times 10^{-3} \, A$ 

Minimum current  $(I_{z \min}) = 10 \, mA = 10 \times 10^{-3} \, A$ 

Maximum value of series resistance  $R_S$  in the voltage regulator circuit is given as

$$egin{aligned} R_{ ext{max}} &= rac{V_s - V_z}{I_{z ext{ min}}} \ &= rac{10 - 6}{10 imes 10^{-3}} \ &= 400 \, \Omega \end{aligned}$$

\_\_\_\_\_

## **Question 129**

The expression  $\overline{A}(A+B) + (B+AA)(A+\overline{B})$  simplifies to

**Options:** 

A. A+B B. AB

C.

 $\overline{A+B}$ 

D.

#### $\overline{A} + \overline{B}$

#### Answer: A

#### Solution:

Given expression,  $\overline{A}(A + B) + (B + AA)(A + \overline{B})$  $= \overline{A}(A + B) + (B + A)(A + \overline{B})$   $= A\overline{A} + \overline{A}B + AB + B\overline{B} + AA + A\overline{B}$   $= A + A\overline{B} + B(\overline{A} + \overline{A}) [\because A\overline{A} = B\overline{B} = 0 \text{ and } A \cdot A = A]$   $= A + A\overline{B} + B(\overline{A} + A)$   $= A(1 + \overline{B}) + B(1) [\because = A + \overline{A} = 1]$   $= A + B [\because 1 + \overline{B} = 1]$ 

-----

## **Question 130**

## Given : The percentage error in the measurements of A, B, C and D are respectively, 4%, 2%, 3% and 1%. The relative error in

$$Z=rac{A^4B^{1\over 3}}{CD^{3\over 2}}$$
 is

**Options:** 

A.  $\frac{127}{2}\%$ B.  $\frac{127}{5}\%$ C.  $\frac{127}{6}\%$ D.  $\frac{127}{6}\%$ 

Answer: C

#### Solution:

The percentage error in Z is given as

 $\frac{\Delta Z}{Z}\% = 4\frac{\Delta A}{A} + \frac{1}{3}\frac{\Delta B}{B} + \frac{\Delta C}{C} + \frac{3}{2}\frac{\Delta D}{D}$  $= 4 \times 4 + \frac{1}{3} \times 2 + 3 + \frac{3}{2} \times 1$  $= 16 + \frac{2}{3} + 3 + \frac{3}{2}$  $= \frac{127}{6}\%$ 

\_\_\_\_\_

## **Question 131**

The Entropy (S) of a black hole can be written as  $S = \beta k_B A$ , where  $k_B$  is the Boltzmann constant and A is the area of the black hole. The  $\beta$  has dimension of

**Options:** 

A.  $L^{2}$ B.  $ML^{2}L^{-1}$ C.  $L^{-2}$ D.

dimensionless

Answer: C

#### Solution:

Given,  $S = \beta k_B A$ 

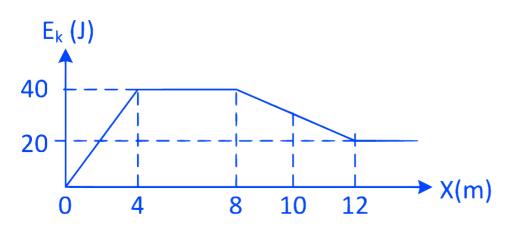
where, dimensional formula of  $S = [M^1 L^2 T^{-2} K^{-1}]$ 

Dimensional formula of  $k_B = [M^1 L^2 T^{-2} K^{-1}]$ Dimensional formula of  $A = [L^2]$ Thus,  $[M^1 L^2 T^{-2} K^{-1}] = \beta [M^1 L^2 T^{-2} K^{-1}] [L^2]$  $\Rightarrow \beta = [L^{-2}]$ 

-----

## **Question 132**

The kinetic energy  $(E_k)$  of a particle moving along X-axis varies with its position (X) as shown in the figure. The force acting on the particle at X = 10 m is



#### **Options:**

A.

5**î** N

Β.

0 N

C.

97.5**î** N

D.

 $-5\hat{i}$ N

#### Answer: D

#### Solution:

According to work-energy theorem,

change in kinetic energy = work done

= force  $\times$  distance

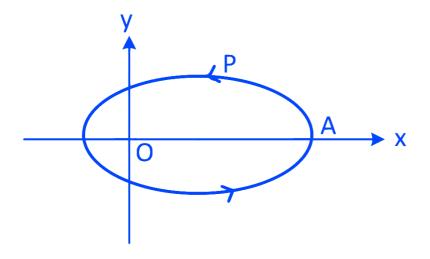
Thus,  $force = \frac{change in energy}{change in distance}$ 

At x = 10 m, we have

 $F = \frac{20-40}{12-8}\hat{i} = -5\hat{i}N$ 

\_\_\_\_\_

## **Question 133**



A particle is moving in an elliptical orbit as shown in figure. If  $\overrightarrow{p}, \overrightarrow{L}$ and  $\overrightarrow{r}$  denote the linear momentum, angular momentum and position vector of the particle (from focus O) respectively at a point A, then the direction of  $\overrightarrow{\alpha} = \overrightarrow{p} \times \overrightarrow{L}$  is along.

#### **Options:**

A.

+ve x axis

B.

-ve x axis

C.

+ve y axis

D.

-ve y axis

Answer: A

### Solution:

At position A, direction of  $\overrightarrow{p}$  is along + ve Y-axis.

At position A, direction of  $\overrightarrow{L}$  is along + ve Z-axis because  $\overrightarrow{L} = \overrightarrow{r} \times \overrightarrow{p}$  and  $\overrightarrow{r}$  is along + ve X-axsis.

Thus,  $\overrightarrow{\alpha} = \overrightarrow{p} \times \overrightarrow{L}$ 

## $= \widehat{i} imes \widehat{k}$

 $= -\hat{j}$  or -ve Y-axis.

------

## Question 134

A particle is subjected to two simple harmonic motions in the same direction having equal amplitudes and equal frequency. If the resultant amplitude is equal to the amplitude of the individual motion, the phase difference ( $\delta$ ) between the two motion is

**Options:** 

A.

 $\delta = \frac{\pi}{3}$ 

B.  $\delta = \frac{2\pi}{3}$ C.  $\delta = \pi$ D.  $\delta = \frac{\pi}{2}$ 

Answer: B

#### Solution:

According to the question,

 $A = \sqrt{A^2 + A^2 + 2AA\cos\delta}$  $\Rightarrow \cos\delta = -\frac{1}{2}$ or,  $\delta = 120^\circ$ or,  $= \frac{2\pi}{3}$ 

-----

## **Question 135**

A body of mass m is thrown with velocity u from the origin of a coordinate axes at an angle  $\theta$  with the horizon. The magnitude of the angular momentum of the particle about the origin at time t when it is at the maximum height of the trajectory is proportional to

**Options:** 

A. u B. u<sup>2</sup> C. u<sup>3</sup>

#### D.

independent of u

#### Answer: C

#### Solution:

Maximum height of projectile,

 $h = rac{u^2 \sin^2 \theta}{2g}$  ..... (i)

At maximum height velocity of projectile,

 $v = u \cos \theta$ 

 $\therefore$  Momentum at highest point =  $mu \cos \theta$ 

: Angular momentum about origin,

 $p = mu\cos heta imes h$ 

 $= mu\cos heta imes rac{u^2 \sin^2 heta}{2g}$ 

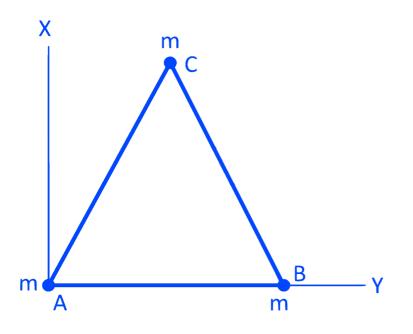
```
=rac{mu^3\cos	heta\sin^2	heta}{2g}
```

```
\Rightarrow p \propto u^3
```

-----

## **Question 136**

Three particles, each of mass 'm' grams situated at the vertices of an equilateral  $\triangle ABC$  of side 'a' cm (as shown in the figure). The moment of inertia of the system about a line AX perpendicular to AB and in the plane of ABC in g-cm<sup>2</sup> units will be



#### **Options:**

A.

 $2 \text{ ma}^2$ 

B.

 $\frac{\mathbf{3}}{\mathbf{2}}$  ma<sup>2</sup>

C.

 $\frac{\mathbf{3}}{\mathbf{4}}$  ma<sup>2</sup>

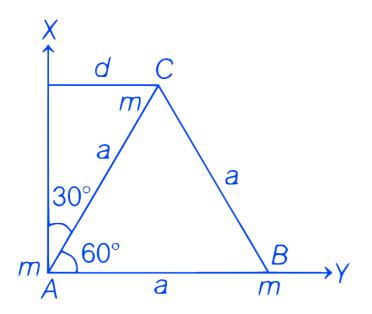
D.

 $\frac{\mathbf{5}}{\mathbf{4}}$  ma<sup>2</sup>

Answer: D

#### Solution:

Moment of inertia about line  $AX = ma^2 + md^2$ 



We know that,

 $\sin \theta = \frac{d}{a}$   $\Rightarrow \frac{1}{2} = \frac{d}{a} (\because \theta = 30^{\circ})$   $\Rightarrow d = \frac{a}{2}$   $\therefore I_{Ax} = ma^{2} + m\left(\frac{a}{2}\right)^{2}$   $= ma^{2} + \frac{ma^{2}}{4} = \frac{5}{4}ma^{2}$ 

\_\_\_\_\_

**Question 137** 

# A body of mass m is thrown vertically upward with speed $\sqrt{3}$ v<sub>e</sub>, where v<sub>e</sub> is the escape velocity of a body from earth surface. The final velocity of the body is

**Options:** 

A.		
0		
B.		
2 v <sub>e</sub>		
C.		
$\sqrt{3} v_e$		
D.		
$\sqrt{2} v_e$		

Answer: D

#### Solution:

Given, initial speed,  $v = \sqrt{3} v_e$ We know that,  $v_e = \sqrt{\frac{2GM}{R}}$ At the surface of earth, Total energy = PE + KE  $= -\frac{GMm}{R} + \frac{1}{2}mv^2$   $= -\frac{GMm}{R} + \frac{1}{2}m\left(\sqrt{3}\sqrt{\frac{2GM}{R}}\right)^2$   $= -\frac{GMm}{R} + \frac{1}{2}3m \times \frac{2GM}{R}$   $= -\frac{GMm}{R} + \frac{3GMm}{R} = \frac{2GMm}{R}$ At infinity, total energy = PE + KE  $= 0 + \frac{1}{2}mv^2$ From the principle of conservation of energy,

$$\frac{2GMm}{R} = \frac{1}{2}mv^2$$

$$\Rightarrow \frac{4GM}{R} = v^2$$

$$\Rightarrow v = \sqrt{\frac{4GM}{R}}$$

$$= \sqrt{2 \times \frac{2GM}{R}} = \sqrt{2} v_e$$

\_\_\_\_\_

## **Question 138**

If a string, suspended from the ceiling is given a downward force  $F_1$ , its length becomes  $L_1$ . Its length is  $L_2$ , if the downward force is  $F_2$ . What is its actual length?

**Options:** 

 $\frac{L_1+L_2}{2}$ B. $\sqrt{L_1L_2}$ 

A.

с. -

 $rac{F_2L_1+F_1L_2}{F_2+F_1}$ 

D.

 $rac{F_2L_1-F_1L_2}{F_2-F_1}$ 

Answer: D

#### Solution:

According to the Hooke's law, for deformation of string of length l,

$$\frac{F_1}{A} \propto \frac{\Delta l_1}{l}$$
 ...... (i)

and in second case,

$$\frac{F_2}{A} \propto \frac{\Delta l_2}{l}$$
 ..... (ii)

From Eqs. (i) and (ii), we have

$$egin{aligned} rac{F_1}{F_2} &= rac{\Delta l_1}{\Delta l_2} = rac{l_1 - l}{l_2 - l} \ &\Rightarrow (F_2 - F_1) l = F_2 l_1 - F_1 l_2 \ &\Rightarrow l = rac{F_2 l_1 - F_1 l_2}{F_2 - F_1} \end{aligned}$$

\_\_\_\_\_

## **Question 139**

27 drops of mercury coalesce to form a bigger drop. What is the relative increase in surface energy?

**Options:** 

A.  $\frac{3}{2}$ B.  $\frac{2}{3}$ C.  $-\frac{2}{3}$ D. 8

#### Answer: C

#### Solution:

Let r be the radius of small mercury drop. Thus, total volume of 27 drops =  $27 \times \frac{4}{3} \pi r^3$ Total volume of bigger drop =  $\frac{4}{3} \pi R^3$  $\therefore$  According to given situation,

$$rac{4}{3}\,\pi R^3 = 27 imes rac{4}{3}\,\pi r^3$$

 $\Rightarrow R = 3r$ 

Now, surface energy = surface tension  $\times$  area

 $= T \times A$ 

Surface energy of 27 drops =  $T \times 27 \times (4\pi r^2)$ 

 $=27 imes4\pi r^2T$ 

Surface energy of bigger drop  $= T \times 4\pi R^2$ 

$$T = T imes 4\pi (3r)^2$$
 $= 9 imes 4\pi r^2 T$ 

Increase in surface energy =  $9 \times 4\pi r^2 T - 27 \times 4\pi r^2 T$ 

 $= -18 imes 4 \pi r^2 T$ 

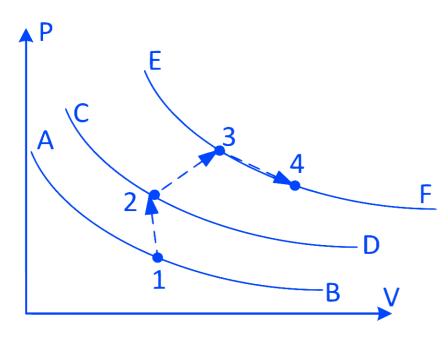
... Relative increase in surface energy

$$=rac{-18 imes 4\pi r^2T}{27 imes 4\pi r^2T}=-rac{2}{3}$$

-----

# **Question 140**

Certain amount of an ideal gas is taken from its initial state 1 to final state 4 through the paths  $1 \rightarrow 2 \rightarrow 3 \rightarrow 4$  as shown in figure. AB, CD, EF are all isotherms. If  $v_p$  is the most probable speed of the molecules, then



#### **Options:**

A.

 $v_p$  at 3 =  $v_p$  at 4 >  $v_p$  at 2 >  $v_p$  at 1

B.

 $v_p$  at  $3 > v_p$  at  $1 > v_p$  at  $2 > v_p$  at 4

C.

 $v_p$  at  $3 > v_p$  at  $2 > v_p$  at  $4 > v_p$  at 1

D.

 $v_p$  at 2 =  $v_p$  at 3 >  $v_p$  at 1 >  $v_p$  at 4

#### Answer: A

### Solution:

For the given isotherm, the temperature of the curve EF is greater than the curve CD and AB.

As we know that, most probable speed of the molecule is given as

$$v_p = \sqrt{rac{2RT}{M}}$$

Thus, the  $v_p$  at 3 and 4 will be same.

Hence,  $\boldsymbol{v_p}$  at  $3 = \boldsymbol{v_p}$  at  $4 > \boldsymbol{v_p}$  at  $2 > \boldsymbol{v_p}$  at 1.

\_\_\_\_\_

# **Question 141**

# Consider a thermodynamic process where integral energy $U = AP^2V$ (A = constant). If the process is performed adiabatically, then

#### **Options:**

#### A.

 $AP^2(V+1) = constant$ 

#### B.

 $(AP + 1)^2 V = constant$ 

#### C.

 $(AP + 1)V^2 = constant$ 

#### D.

 $\frac{V}{(AP+1)^2} = \text{constant}$ 

#### Answer: B

### Solution:

 $U = Ap^2 V, A = \text{constant}$ 

For adiabatic process, dQ = 0

. From first law of thermodynamics,

dQ = dU + dW

$$\therefore dU + dW = 0 (\because dQ = 0)$$

$$\Rightarrow d(Ap^{2}V) + pdV = 0$$

$$\Rightarrow A(2p \cdot Vdp + p^{2}dV) + pdV = 0$$

$$\Rightarrow (Ap^{2} + p)dV + 2ApVdp = 0$$

$$\Rightarrow (Ap^{2} + p)dV = -2ApVdp$$

$$\Rightarrow \frac{dV}{-2AV} = \frac{pdp}{p(Ap+1)}$$

$$\Rightarrow \frac{dp}{(Ap+1)} + \frac{1}{2A} \cdot \frac{dv}{v} = 0$$

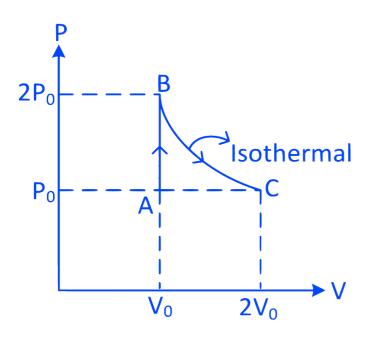
Integrating on both sides,

$$\Rightarrow \int \frac{dp}{(Ap+1)} + \frac{1}{2A} \int \frac{dV}{V} = \int 0$$
$$\Rightarrow \frac{\ln(Ap+1)}{A} + \frac{1}{2A} \ln V = \ln C$$
$$\Rightarrow \ln(Ap+1) + \ln V^{1/2} = \ln C$$
$$\Rightarrow \ln[V^{1/2}(Ap+1)] = \ln C$$
$$\Rightarrow V^{1/2}(Ap+1) = C$$
$$\Rightarrow V(Ap+1)^2 = C \text{ (constant)}$$

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# **Question 142**

One mole of a diatomic ideal gas undergoes a process shown in P-V diagram. The total heat given to the gas ( $\ln 2 = 0.7$ ) is



# **Options:**

A.

 $2.5 P_0 V_0$ 

B.

 $3.9 P_0 V_0$ 

C.

 $1.1 P_0 V_0$ 

D.

 $1.4 P_0 V_0$ 

#### Answer: B

### Solution:

The given process BC is isothermal and AB is isochoric.

From A to B, we have  $p_0 \rightarrow 2p_0$ as  $p \propto T$ Hence,  $T_B = 2T_A = 2T_0$   $Q_{AB} = \Delta U_{AB} = W_{AB} = C_V \Delta T + 0$   $\Rightarrow Q_{AB} = \frac{5}{2}R(2T_0 - T_0) = \frac{5}{2}p_0V_0$ ( $\because C_V = \frac{5}{2}R$  for diatomic gas and pV = RT) From B to C, we have,  $Q_{BC} = \Delta U_{BC} + W_{BC} = 0 + R(2T_0) \ln \frac{2V_0}{V_0}$   $= 2RT_0 \ln 2$   $= 2\ln 2p_0V_0$ Hence,  $Q_{total} = Q_{AB} + Q_{BC}$   $= (2.5 + 2\ln 2)p_0V_0$  $= 3.9 p_0V_0$ 

# **Question 143**

Two charges, each equal to -q are kept at (-a, 0) and (a, 0). A charge q is placed at the origin. If q is given a small displacement along y direction, the force acting on q is proportional to

\_\_\_\_\_

**Options:** 

А. у В.

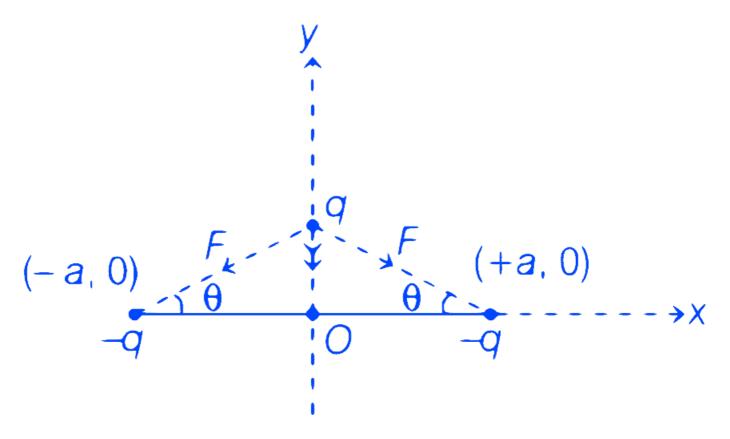
—у

C.	
$\frac{1}{y}$	
D.	
$-\frac{1}{y}$	

#### Answer: B

### Solution:

Consider the diagram given below.



When the charge q is displaced momentarily, it starts oscillating. The net force acting on q is given by  $F_{net} = 2F \sin \theta$ 

$$= -rac{2\,kq{ imes}q}{\left(\sqrt{y^2+a^2}
ight)^2} \, . \; rac{y}{\sqrt{y^2+a^2}} = -rac{2kq^2y}{\left(\sqrt{y^2+a^2}
ight)^{rac{3}{2}}}$$

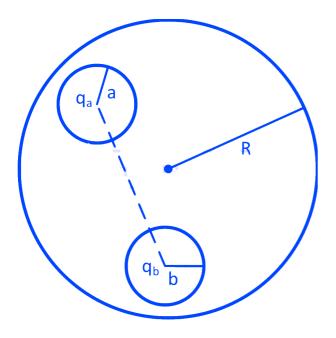
For *a* >> *y*, we have

$$F_{net} = -rac{2kq^2y}{a^3}$$

or,  $F_{net} \propto -y$ 

-----

# **Question 144**



A neutral conducting solid sphere of radius R has two spherical cavities of radius a and b as shown in the figure. Centre to centre distance between two cavities is c.  $q_a$  and  $q_b$  charges are placed at the centres of cavities respectively. The force between  $q_a$  and  $q_b$  is

**Options:** 

A.  $\frac{1}{4\pi\varepsilon_0} \frac{q_a q_b}{c^2}$ B.  $\frac{1}{4\pi\varepsilon_0} q_a q_b \left(\frac{1}{a^2} + \frac{1}{b^2}\right)$ C. zero D.

insufficient data

#### Answer: A

### Solution:

We can find the force between  $q_a$  and  $q_b$  by calculating electric field first.

From Gauss's law,

 $\oint E \,.\; ds = rac{Q_{enclosed}}{arepsilon_0} \Rightarrow E \,.\; 4\pi c^2 = rac{q_a}{arepsilon_0}$ 

(: For cavity of electric field is to be calculated upto  $q_b$  )

 $\Rightarrow E_a = rac{q_a}{4\piarepsilon_0 c^2}$ 

Now, force on  $q_b$  due to  $q_a$  is given by

 $F=E_a$  .  $q_b=rac{q_aq_b}{4\piarepsilon_0c^2}$ 

------

# **Question 145**

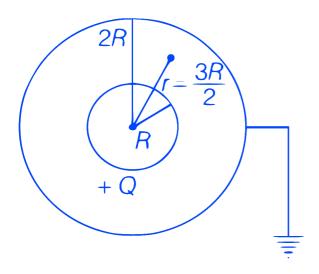
Consider two concentric conducting sphere of radii R and 2R respectively. The inner sphere is given a charge +Q. The other sphere is grounded. The potential at  $r = \frac{3R}{2}$  is

**Options:** 

A.  $\frac{1}{4\pi\varepsilon_{0}} \frac{Q}{6R}$ B. 0 C.  $\frac{1}{4\pi\varepsilon_{0}} \frac{2Q}{3R}$ D.  $\frac{1}{4\pi\varepsilon_{0}} \frac{Q}{R}$ Answer: A

### Solution:

Consider the figure given below.



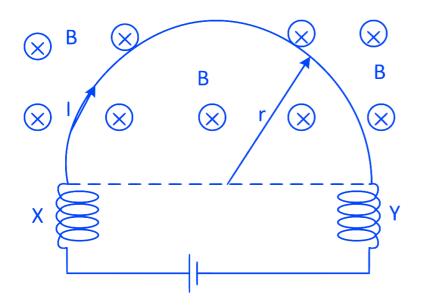
Due to grounding, charge on outer sphere = 0Now, potential due to inner sphere,

 $V = \frac{kQ}{r} = \frac{kQ}{\frac{3R}{2}}$  $= \frac{2kQ}{3R}$ or,  $\frac{1}{4\pi\varepsilon_0}\frac{2Q}{3R}$ 

\_\_\_\_\_

# **Question 146**

A horizontal semi-circular wire of radius r is connected to a battery through two similar springs X and Y to an electric cell, which sends current I through it. A vertically downward uniform magnetic field B is applied on the wire, as shown in the figure. What is the force acting on each spring?



### **Options:**

A.

 $2\pi rBI$ 

B.

 $\frac{1}{2}\pi rBI$ 

C.

BIr

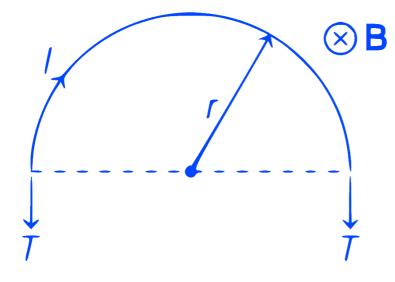
D.

2BIr

Answer: C

## Solution:

Considering the semi-circular wire of radius r. Force acting on it is shown below



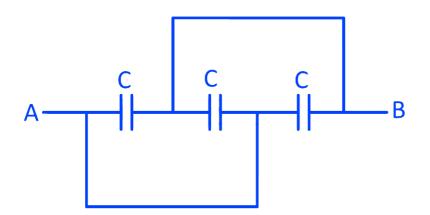
Let T be the force exerted by each spring.

 $\therefore T + T = IBl$  2T = IBl  $2T = IB \cdot \pi r (\because l = \pi r)$   $\therefore T = \frac{IB\pi r}{2}$ 

\_\_\_\_\_

# **Question 147**

Find the equivalent capacitance between A and B of the following arrangement :

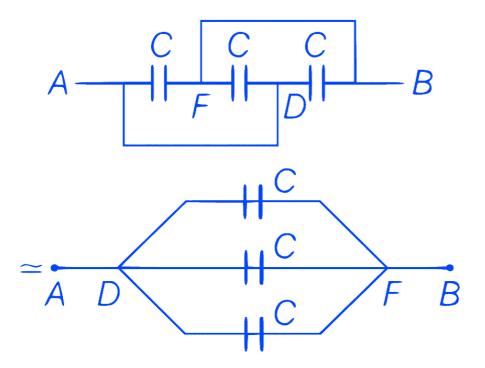


# **Options:**

A. C B. 3C C.  $\frac{2C}{3}$ D.  $\frac{3C}{2}$ 

# Answer: B

# Solution:



Here, all the three capacitors are connected in parallel. So, equivalent capacitance will be  $C_{eq} = C + C + C = 3C$ 

\_\_\_\_\_

# **Question 148**

A golf ball of mass 50 gm placed on a tee, is struck by a golf-club. The speed of the golf ball as it leaves the tee is 100 m/s, the time of contact on the ball is 0.02 s. If the force decreases to zero linearly with time, then the force at the beginning of the contact is

**Options:** 

A.

100 N

B.

200 N

C.

250 N

D.

500 N

#### Answer: D

### Solution:

Given, initial velocity,  $\boldsymbol{u} = \boldsymbol{0}$  m/s

Final velocity, v = 100 m/s

Mass of ball,  $m = 50 imes 10^{-3}$  kg

Time of contact = 0.02 s

Impulse,  $F = \frac{m(v-u)}{t}$ =  $\frac{50 \times 10^{-3}(100-0)}{0.02}$ 

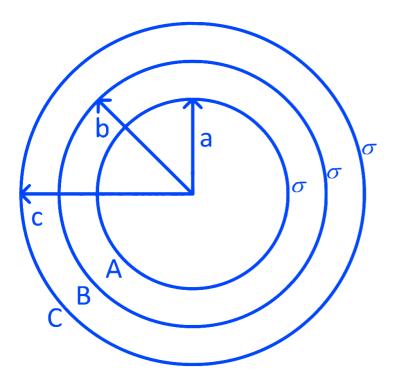
 $= \frac{1}{0.02}$  $= \frac{5 \times 100}{2}$ 

= 250 N

\_\_\_\_\_

# **Question 149**

Three concentric metallic shells A, B and C of radii a, b and c (a < b < c) have surface charge densities  $+\sigma$ ,  $-\sigma$  and  $+\sigma$  respectively. The potential of shell B is



# **Options:**

A.

 $(a+b+c)rac{\sigma}{arepsilon_0}$ 

B.

<u>σc</u> ε<sub>n</sub>

C.

 $\left(rac{a^2}{c}-rac{b^2}{c}+c
ight)rac{\sigma}{arepsilon_0}$ 

D.

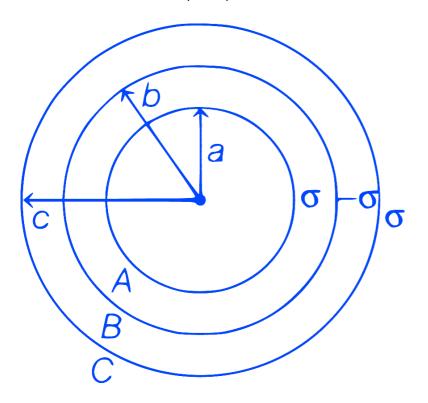
$$\left(rac{a^2}{c}-b+c
ight)rac{\sigma}{arepsilon_0}$$

#### Answer: D

### Solution:

\_

Net potential at any point (r = b) of shell B



= potential due to shell A + potential due to shell B + potential due to shell C.  $V = V_{A, out} + V_{B, surface} + V_{C, in}$   $= V_{A, out} + V_{B, surface} + V_{C, surface} \text{ (for shell, } V_{in} = V_{surface}\text{)}$   $V = \frac{1}{4\pi\varepsilon_0} \left[\frac{q_a}{b} + \frac{q_b}{b} + \frac{q_c}{c}\right]$ 

$$egin{aligned} &=rac{1}{4\piarepsilon_0}\left[rac{\sigma4\pi a^2}{b}+rac{(-\sigma)4\pi b^2}{b}+rac{(\sigma)4\pi c^2}{c}
ight]\ &=rac{\sigma}{arepsilon_0}\left[rac{a^2}{b}-b+c
ight] \end{aligned}$$

# **Question 150**

One mole of an ideal monoatomic gas expands along the polytrope  $PV^3 = constant$  from  $V_1$  to  $V_2$  at a constant pressure  $P_1$ . The temperature during the process is such that molar specific heat  $C_V = \frac{3R}{2}$ . The total heat absorbed during the process can be expressed as

**Options:** 

A.  $P_1 V_1 \left( \frac{V_1^2}{V_2^2} + 1 \right)$ 

B.

 $P_1V_1\left(rac{V_1^2}{V_2^2}-1
ight)$ 

$$P_1V_1\left(rac{V_1^3}{V_2^2}-1
ight)$$

D.

 $P_1V_1\left(rac{V_1}{V_2^2}-1
ight)$ 

Answer: B

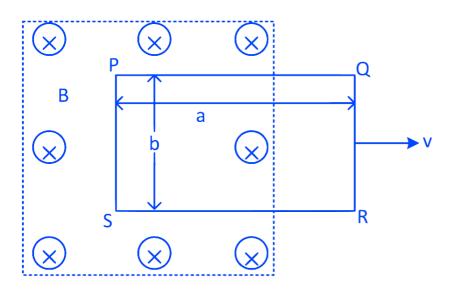
### Solution:

Given  $pV^3 = C$ ,  $C_V = \frac{3R}{2}$ , n = 1 mol

For polytropic process,

 $pV^x = C$  $\therefore x = 3$   $C = C_V + \frac{R}{1-x} = \frac{3R}{2} + \frac{R}{1-3} = R$ Heat supplied  $(Q) = nC\Delta T$   $= 1 \times R \times (T_2 - T_1) = R(T_2 - T_1)$ Now, As pV = nRT ..... (i)  $\therefore pV = RT$  ( $\because n = 1$ )  $\therefore R = \frac{pV}{T} = \frac{p_1T_1}{T_1}$ Also,  $pV^3 = C$   $\Rightarrow \left(\frac{RT}{V}\right)V^3 = C$  [from Eq. (i)]  $\Rightarrow TV^2 = C \Rightarrow T_1V_1^2 = T_2V_2^2$   $\therefore T_2 = \frac{T_1V_1^2}{V_2^2}$ Heat supplied  $(Q) = \frac{p_1V_1}{T_1} \left[\frac{T_1V_1^2}{V_2^2} - T_1\right] = p_1V_1 \left[\frac{V_1^2}{V_2^2} - 1\right]$ 

# **Question 151**



As shown in figure, a rectangular loop of length 'a' and width 'b' and made of a conducting material of uniform cross-section is kept

### in a horizontal plane where a uniform magnetic field of intensity B is acting vertically downward. Resistance per unit length of the loop is $\lambda \Omega/m$ . If the loop is pulled with uniform velocity 'v' in horizontal direction, which of the following statement is/are true?

#### **Options:**

A.

Current in the loop I =  $\frac{Bbv}{\lambda(2b+2a)}$ 

Β.

Current will be in clockwise direction, looking from the top.

C.

 $V_P - V_S = V_Q - V_R$ , where V is the potential.

#### D.

There cannot be any induction in part SR.

#### Answer: D

### Solution:

Given, resistance per unit length of loop

$$=\lambda\,\Omega/m$$

(a) Current in the loop,  $I = \frac{E}{R}$ 

$$I = \frac{Blv}{R}$$
 (:: emf  $E = Blv$ ) ......(i)

We know that,

$$\frac{R}{2(a+b)} = \lambda \Rightarrow R = \lambda (2a+2b) \dots \dots \dots \dots (ii)$$

Using Eqs. (i) and (ii), we get

$$I = rac{Bbv}{\lambda(2a+2b)}$$

So, option (a) is correct.

(b) Using right hand thumb rule, direction of current in the loop will be clockwise, looking from the top.

But as the flux is changing, so according to Lenz's law, direction of current will be anti-clockwise.

So, option (b) is incorrect.

(c) As the arm PS and QR has same potential, then  $V_P - V_S = V_Q - V_R$  is also same.

So, option (c) is correct.

(d) As the arm SR is parallel to the velocity. So, there will not be any current or induction.

So, option (d) is correct.

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# **Question 152**

A sample of hydrogen atom in its ground state is radiated with photons of 10.2 eV energies. The radiation from the sample is absorbed by excited ionized He<sup>+</sup>. Thenwhich of the following statement/s is/are true?

#### **Options:**

A.

 $He^+$  electron moves from n = 2 to n = 4.

Β.

In the  $He^+$  emission spectra, there will be 6 lines.

C.

Smallest wavelength of  $\text{He}^+$  spectrum is obtained when transition taken place from n = 4 to n = 3.

D.

He<sup>+</sup> electron moves from n = 2 to n = 3.

#### **Answer: B**

### Solution:

Given, energy of photons = 10.2 eV

Energy for nth state,

$$\begin{split} E_n &= -13.6 \, Z^2 \times \left( \frac{1}{n_i^2} - \frac{1}{n_f^2} \right) \\ &= -13.6 \times (2)^2 \left( \frac{1}{2^2} - \frac{1}{4^2} \right) (\because Z = 2) \end{split}$$

 $= -13.6 \times 4 \times \left(\frac{4-1}{16}\right)$   $= -3.4 \times \frac{3}{4}$  = -10.2 eVor, E = 10.2 eVSo, option (a) is correct. (b) Number of lines in emission spectra  $= \frac{n(n-1)}{2} = \frac{4 \times 3}{2} = 6 [\because n = 4]$ So, option (b) is correct. (c) For smallest wavelength of He<sup>+</sup> spectrum the final state should be  $n_f = \infty$ So, option (c) is incorrect. (d) He<sup>+</sup> electron cannot jump from n = 2 to n = 3 as the energy of photon is less than required. So, option (d) is incorrect.

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# **Question 153**

## A particle is moving in x-y plane according to $\overrightarrow{r} = b \cos \omega t \hat{i} + b \sin \omega t \hat{j}$ , where $\omega$ is constant. Which of the following statement(s) is/are true?

#### **Options:**

#### A.

 $\frac{E}{\omega}$  is a constant where E is the total energy of the particle.

#### B.

The trajectory of the particle in x-y plane is a circle.

C.

In  $a_x - a_y$  plane, trajectory of the particle is an ellipse ( $a_x$ ,  $a_y$  denotes the components of acceleration)

D.

 $\overrightarrow{a} = \omega^2 \overrightarrow{v}$ 

#### Answer: B

### Solution:

Given, trajectory of the particle,

#### $\overrightarrow{r} = b\cos\omega t\hat{i} + b\sin\omega t\hat{j}$

It's component can be written as

 $x = b \cos \omega t \dots$  (i)

 $y = b \sin \omega t$  ..... (ii)

Both Eqs. (i) and (ii) together represent the circle in x-y plane. Thus, the trajectory of the particle in x-y plane is circle.

Now,

$$egin{aligned} rac{dec{r}}{dt} &= \omega b (-\sin \omega t \hat{i} + \cos \omega t \hat{j}) \ &rac{d^2 ec{r}}{dt^2} &= -b \omega^2 (\cos \omega t \hat{i} + \sin \omega t \hat{j}) \ &= -\omega^2 (ec{r}) \end{aligned}$$

Therefore,  $\overrightarrow{a} = -\omega^2 \overrightarrow{r}$ 

Hence, option (c) and (d) are incorrect.

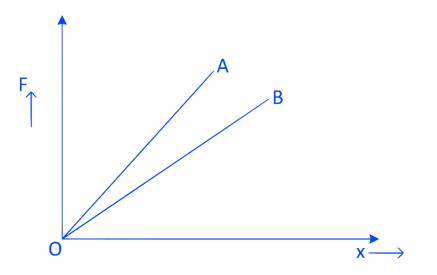
Energy of the particle in circular motion is given as  $\frac{1}{2}m\omega^2 A^2$  (where, A is the maximum displacement from the centre), which is constant.

Hence,  $\frac{E}{\omega}$  is also constant.

So, option (a) and (b) are correct.

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# **Question 154**



# Two wires A and B of same length are made of same material. Load (F) vs. elongation (x) graph for these two wires is shown in the figure. Then which of the following statement(s) is/are true?

#### **Options:**

A.

The cross-section area of A is greater than that of B.

B.

Young's modulus of A is greater than Young's modulus of B.

C.

The cross-sectional area of B is greater than that of A.

D.

Young's modulus of both A and B are same.

#### Answer: D

### Solution:

Load F can be given as

$$F = \left(\frac{AY}{L}\right)\Delta x$$

where, A = cross-sectional area

Y = Young's modulus

L = length

 $\Delta x =$  elongation in length.

i.e., F versus  $\Delta x$  graph is a straight line of slope  $\frac{YA}{L}$ .

 $(slope)_A > (slope)_B$ 

 $\left(\frac{YA}{L}\right)_A > \left(\frac{YA}{L}\right)_B$ 

or,  $(A)_A > (A)_B$ 

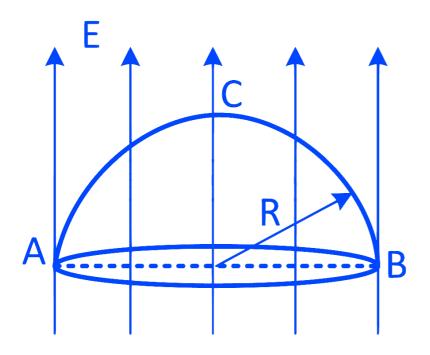
As we know that, they are of same material.

Hence,  $Y_B = Y_A$ 

So, option (a) and (d) are correct.

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# **Question 155**



### A hemisphere of radius R is placed in a uniform electric field E so that its axis is parallel to the field. Which of the following statement(s) is/are true?

#### **Options:**

A.

Flux through the curved surface of hemisphere is  $\pi R^2 E$ .

B.

Flux through the circular surface of hemisphere is  $\pi R^2 E$ .

C.

Total flux enclosed is zero.

D.

Work done in moving a point charge q from A to B via the path ACB depends upon R.

#### Answer: C

### Solution:

According to Gauss's theorem Net flux through the surface  $= \frac{q_{enclosed}}{\epsilon_0}$ Here,  $q_{enclosed} = 0$ So,  $\phi_{curved surface} + \phi_{circular surface} = 0$   $\phi_{curved surface} = -\phi_{circular surface}$   $= -E \cdot S = -ES \cos 180^{\circ}$   $= ES (\because \cos 180^{\circ} = -1)$   $= E \cdot \pi R^2 = \pi R^2 E$ As, electrostatic field is conservative in nature. So, work done is path independent. So, option (a) and (c) are correct.

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