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# **GUJCET 2018 Question Paper**

Gujarat Common Entrance Exam (GUJCET)

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# **Answers & Solutions**

Time: 2 hrs.



# **GUJCET-2018**

(Physics, Chemistry)

#### Important Instructions:

- The physics and Chemistry test consists of 80 question. Each question carries 1 marks. For correct response, the candidate will get 1 marks. For each incorrect response 1/4 mark will be deducted. The maximum marks are 80.
- 2. This test is of 2 hours duration.
- Use Black Ball Point Pen only for writing particulars on OMR Answer Sheet and marking answers by darkening the circle.
- 4. Rough work is to be done on the space provided for this purpose in the Test Booklet only.
- 5. On completion of the test, the candidate must handover the Answer Sheet to the Invigilator in the Room/Hall. The candidates are allowed to take away this Test Bookle with them.
- The Set No. for this Booklet is 01. Make sure that the Set No. Printed on the Answer Sheet is the same as that on this booklet. In case of discrepancy, the candidate should immediately report the matter to the Invigilator for replacement of both the Test Booklet and the Answer Sheet.
- 7. The candidate should ensure that the Answer Sheet is not folded. Do not make any stray marks on the Answer Sheet.
- 8. Do not write your Seat No. anywhere else, except in the specified space in the Test Booklet/Answer Sheet.
- 9. Use of White fluid for correction is not permissible on the Answer Sheet.
- 10. Each candidate must show on demand his/her Admission Card to the Invigilator.
- 11. No candidate, without special permission of the Superindent or Invigilator, should leave his/her seat.
- 12. Use of manual Calculator is permissible.
- 13. The candidate should not leave the Examination Hall without handing over their Answer Sheet to the Invigilator on duty and must sign the Attendance Sheet (Patrak-01). Cases where a candidate has not signed the Attendance Sheet (Patrak-01) will be deemed not to have handed over the Answer Sheet and will be dealt with as an unfair means case.
- 14. The candidates are governed by all Rules and Regulations of the Board with regards to their conduct in the Examination Hall. All cases of unfair means will be dealt with as per Rules and Regulations of the Board.
- 15. No part of the Test Booklet and Answer Sheet shall be detached under any circumstances.
- 16. The candidates will write the Correct Test Booklet Set No. as given in the Test Booklet/Answer Sheet in the Attendance Sheet. (Patrak-01)



M.M.: 80

# PART-A: PHYSICS

1. Three identical charges are placed on three vertices of a square. If the force acting between  $q_1$  and  $q_2$  is

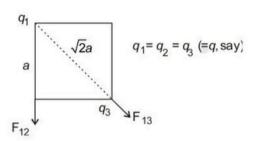
 $F_{12}$  and between  $q_1$  and  $q_3$  is  $F_{13}$  then  $\frac{F_{13}}{F_{12}}$  =

- (A)  $\frac{1}{\sqrt{2}}$
- (B) 2

(C)  $\frac{1}{2}$ 

(D)  $\sqrt{2}$ 

Answer (C)



Sol.

 $\mathsf{F}_{12} = \frac{kq_1q_2}{a^2} = \frac{kq^2}{a^2}$ 

$$\mathsf{F}_{13} = \frac{kq_1q_3}{(\sqrt{2}\mathsf{a})^2} = \frac{kq^2}{2\mathsf{a}^2}$$

$$\frac{F_{13}}{F_{12}} = \frac{1}{2}$$

- 2. When a  $10\mu C$  charge is enclosed by a closed surface, the flux passing through the surface is  $\phi$ . Now another 10  $\mu C$  charge is placed inside the closed surface, then the flux passing through the surface is
  - (A) 2¢

(B) ¢

(C) 46

(D) Zero

Answer (A)

Sol. 
$$\phi = \frac{q}{\epsilon_0}$$

$$\Rightarrow \phi \propto q$$

$$\therefore \quad \frac{\phi'}{\phi} = \frac{q'}{q} = \frac{20\mu C}{10\mu C}$$

$$=$$
  $\phi' = 2\phi$ 

- The electric force acting between two point charges kept at a certain distance in vacuum is 16N. If the same two charges are kept at the same distance in a medium of dielectric constant 8. The electric force acting between them is \_\_\_\_\_
  - (A) 16

- (B) 128
- (C) 1024
- (D) 2

Answer (D)

**Sol.** In medium 
$$F = \frac{F}{K} = \frac{16}{2}$$

- The unit of polarizabity of the molecule is
  - (B) C<sup>-2</sup>m<sup>1</sup>N<sup>1</sup>
  - (A) C<sup>-2</sup>m<sup>1</sup>N<sup>-1</sup> (C) C<sup>2</sup>m<sup>1</sup>N<sup>-1</sup>
- (D) C<sup>2</sup>m<sup>-1</sup>N<sup>-1</sup>

Answer (C)

- On the axis and on the equator of an electric dipole for all points
  - (A) On the axis V = 0 and on equator  $V \neq 0$
  - (B) On both of them V = 0
  - (C) On both of them  $V \neq 0$
  - (D) On the axis  $V \neq 0$  and on equator V = 0

Answer (D)

Sol. Potential due to dipole

$$V = \frac{kp \cos \theta}{r^2}$$

on axis.

$$\theta = 0$$

$$V = \frac{kp}{r^2} \neq 0$$
 on equator

$$\theta = 90^{\circ}$$

- When the temperature of a conductor increases the ratio of conductivity and resistivity \_\_\_\_
  - (A) decrease
- (B) increase

= 0

- (C) remain constant
- (D) increase or decrease

Answer (A)

Sol. 
$$\frac{\sigma}{\rho} = \frac{1}{\rho^2}$$

 $\boldsymbol{\rho}$  increases when temperature is increased. Thus, the given ratio decreases.

- 7. You are given 10 resistors each of resistance  $2\Omega$ . First they are connected to obtain possible minimum resistance. Then they are connected to obtain possible maximum resistance. The ratio of maximum and minimum resistance is
  - (A) 2.5

- (C) 100
- (D) 25

Sol. Minimum possible resistance is obtained when all resistors are connected in parallel

$$R_{min} = \frac{2}{10} = 0.2\Omega$$

Maximum possible resistance is obtained when all resistors are connected in series.

$$R_{\text{max}} = 2 \times 10 = 20\Omega$$

- The dimensional formula of mobility is
  - (A)  $M^1L^{-1}T^{-2}A^{-1}$
- (B) M1L0T-2A-1
- (C) M-1L1T2A1
- (D) M-1L0T2A1

# Answer (D)

Sol. 
$$\mu = \frac{V_d}{E}$$

$$[\mu] = \frac{[V_d]}{[E]} = \frac{[V_d][q]}{[F]}$$
$$= \frac{[LT^{-1}][AT]}{[MLT^{-2}]}$$

$$= [M^{-1}L^0T^2A]$$

- An electron having mass 9.1 × 10<sup>-31</sup> kg, charge  $1.6 \times 10^{-19}$  C and moving with the velocity of  $10^6$  m/ s enters a region where magnetic field exists. If it describes a circle of radius 0.2 m then intensity of magnetic field must be  $\times 10^{-5}$  T.
  - (A) 2.84
- (B) 5.65
- (C) 14.4
- (D) 1.32

#### Answer (A)

Sol. 
$$r = \frac{mv}{qB}$$

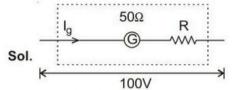
$$= B = \frac{mv}{qr} = \frac{9.1 \times 10^{-31} \times 10^{6}}{1.6 \times 10^{-19} \times 0.2}$$
$$= 2.84 \times 10^{-5} \text{ T}$$

10. A galvanometer of resistance 50Ω giving full scale deflection for a current of 10 milliampere is to be changed into a voltmeter of range 100V.

A resistance of  $\Omega$  has to be connected in series with the galvanometer.

- (A) 10000
- (B) 10025
- (C) 9950
- (D) 9975

#### Answer (C)



Using Ohm's law

$$100 = I_0(50 + R)$$

$$100 = 10 \times 10^{-3} (R + 50)$$

$$= R + 50 = 10000$$

$$= R = 9950\Omega$$

- 11. Two parallel very long straight wires carrying current of 5A each are kept at a separation of 1m. If the currents are in the same direction, the force per unit length between them is \_\_\_ N/m. ( $\mu_0 = 4\pi \times 10^{-7}$  SI)

  - (A)  $5 \times 10^{-5}$ , repulsive (B)  $5 \times 10^{-6}$ , attractive
  - (C)  $5 \times 10^{-5}$ , attractive (D)  $5 \times 10^{-6}$ , repulsive

## Answer (B)

Sol. Force per unit length is given by

$$F = \frac{\mu_0 I_1 I_2}{2\pi d}$$

$$= \frac{4\pi \times 10^{-7} \times 5 \times 5}{2\pi \times 1}$$

$$= 5 \times 10^{-6} \,\text{N}$$

$$I_1 \qquad I_2$$

12. A very long straight wire of radius r carries current I. Intensity of magnetic field B at a point, lying at a perpendicular distance 'a' from the axis is ∞ \_\_\_\_. (where a < r)

- (B) 1/2<sup>2</sup>
- (C) a2

(D) a

#### Answer (D)

Sol. Magnetic field inside a wire is given by

$$B = \frac{\mu_0 ia}{2\pi r^2}$$

- ⇒ B ∝ a
- 13. A substance is placed in a non uniform magnetic field. It experience weak force towards the strong field. The substance is type.
  - (A) Ferromagnetic
- (B) Diamagnetic
- (C) Paramagnetic
- (D) None of these

#### Answer (C)

Sol. Paramagnetic material is weakly attracted towards strong magnetic field.



The relation between B<sub>v</sub>, B<sub>h</sub> and B is \_\_\_\_\_

(A) 
$$B = \frac{B_v}{B_h}$$

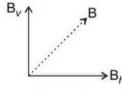
(B) 
$$B = B_h \cdot B_v$$

(C) 
$$B = \sqrt{B_h^2 + B_v^2}$$
 (D)  $B = \frac{B_h}{B_v}$ 

(D) 
$$B = \frac{B_h}{B_v}$$

Answer (C)

Sol. From the diagram



$$B = \sqrt{B_h^2 + B_v^2}$$

15. Two thin lenses of focal length  $f_1$  and  $f_2$  are in contact and coaxial. The power of the combination

(A) 
$$\frac{f_1f_2}{f_1+f_2}$$

(B) 
$$\frac{f_1 + f_2}{2}$$

(C) 
$$\frac{1}{\sqrt{f_1 f_2}}$$

(D) 
$$\frac{f_1 + f_2}{f_1 f_2}$$

Answer (D)

Sol. Power of combination of lenses is given by

$$P = P_1 + P_2 = \frac{1}{f_1} + \frac{1}{f_2}$$

$$= P = \frac{f_1 + f_2}{f_1 f_2}$$

On decreasing the wavelength of incident light from 8000 Å to 4000 Å. the intensity of the scattered light in Rayleih scattering will become \_\_\_\_ times the initial scattered intensity.

(A) 16

(B) 4

(C) 2

(D) 8

Answer (A)

Sol. Intensity in raylength scattering depends on wavelength as

$$I \propto \frac{1}{\lambda^4}$$

$$\frac{I'}{I} = \left(\frac{\lambda}{\lambda'}\right)^4$$

$$= \left(\frac{8000 \,\mathring{A}}{4000 \,\mathring{A}}\right)^4 = 16$$

17. A small angled prism of refractive index 1.6 gives a deviation of 3.6°. The angle of prism is

(A) 5°

(B) 6°

(C) 7°

(D) 8°

Answer (B)

Sol. 
$$\delta = (\mu - 1)A$$

$$\Rightarrow$$
 3.6 = (1.6 - 1)A

$$\Rightarrow$$
 A = 6°

18. A plano convex lens is made of material having refractive index 1.5. The radius of curvature of curved surface is 60 cm. The focal length of the lens is

- cm
- (A) 60
- (B) 120
- (C) -60
- (D) -120

Answer (B)

Sol. 
$$\frac{1}{f} = (\mu - 1) \left( \frac{1}{R_1} - \frac{1}{R_2} \right)$$
  
=  $\frac{1}{f} = (1.5 - 1) \left( \frac{1}{60} - \frac{1}{\infty} \right)$   
=  $f = 120 \text{ cm}$ 

19. If the uncertainty in the position of an electron is 10<sup>-10</sup> m, then the value of uncertainty in its momentum will be \_\_\_ kgms<sup>-1</sup>. ( $h = 6.62 \times 10^{-34} \text{ J}^{-8}$ )

- (B)  $1.03 \times 10^{-24}$
- (A)  $1.06 \times 10^{-24}$ (C)  $1.05 \times 10^{-24}$ 
  - (D)  $1.08 \times 10^{-24}$

Answer (C)

Sol. As per principle of uncertainty

$$\Delta p \cdot \Delta x \simeq \frac{h}{2\pi}$$

$$\Rightarrow \Delta p = \frac{h}{2\pi\Delta x} = \frac{6.626 \times 10^{-34}}{2 \times 3.14 \times 10^{-10}}$$

$$= 1.05 \times 10^{-24} \text{ kg-m/s}$$

20. If the energy of photons corresponding to wavelength of 6000 Å is  $3.2 \times 10^{-19}$  J. The photon energy for wavelength of 4000 Å will be

- (A)  $1.11 \times 10^{-19} \text{ J}$  (B)  $2.22 \times 10^{-19} \text{ J}$
- (C)  $4.44 \times 10^{-19} \text{ J}$  (D)  $4.80 \times 10^{-19} \text{ J}$

Answer (D)

Sol. E = 
$$\frac{hC}{\lambda}$$

$$E \propto \frac{1}{\lambda}$$

$$\therefore \frac{E_2}{E_1} = \frac{\lambda_1}{\lambda_2}$$

$$= \frac{E_2}{3.2 \times 10^{-19}} = \frac{6000 \text{Å}}{4000 \text{Å}}$$

$$= E_2 = \frac{3}{2} \times 3.2 \times 10^{-19}$$

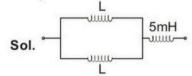
$$= 4.8 \times 10^{-19} \text{ J}$$

- Two inductors each of inductance L are connected in parallel. One more inductor of value 5 mH is connected in series of this configuration then the effective inductance is 15 mH. The value of L is \_\_\_\_ mH.
  - (A) 2.5
- (B) 5.0

(C) 10

(D) 20

Answer (D)



Equivalent inductance is given by

$$L_{eq} = \left(\frac{L \times L}{L + L}\right) + 5 = 15 \text{ (in mH)}$$
$$= \frac{L}{2} = 10$$
$$= L = 20 \text{ mH}$$

- 22. A lamp consumes only 50% of maximum power in an A.C. circuit. What is the phase difference between the applied voltage and the circuit current?
  - (A)  $\frac{\pi}{6}$

(B)  $\frac{\pi}{3}$ 

(C)  $\frac{\pi}{4}$ 

(D)  $\frac{\pi}{2}$ 

Answer (B)

Sol. P = VI coso

$$P_{max} = VI$$

Given

$$P = \frac{P_{max}}{2}$$

$$\Rightarrow$$
 VIcos $\phi = \frac{VI}{2}$ 

$$\Rightarrow \cos \phi = \frac{1}{2}$$

$$\Rightarrow \phi = \frac{\pi}{3}$$

- A capacitor 'C' is connected across a D.C. source, the reactance of capacitor will be
  - (A) LOW
- (B) HIGH
- (C) ZERO
- (D) INFINITE

Answer (D)

Sol. For D.C. source

$$\omega = 0$$
,

Capacitive reactance

$$X_C = \frac{1}{\omega C} = \infty$$

- 24. The dimensional formula of  $\mu_0 \in 0$  is \_\_\_\_
  - (A)  $M^0L^1T^{-1}$
- (B) M<sup>0</sup>L<sup>2</sup>T<sup>-2</sup>
- (C) M<sup>0</sup>L<sup>-2</sup>T<sup>2</sup>
- (D) M<sup>0</sup>L<sup>-1</sup>T<sup>1</sup>

Answer (C)

Sol. Speed of light

$$c = \frac{1}{\sqrt{\mu_0 \epsilon_0}}$$

$$c^2 = \frac{1}{\mu_0 \epsilon_0}$$

$$= \mu_0 \epsilon_0 = \frac{1}{c^2}$$

$$\mu_0 \varepsilon_0 = \frac{1}{[c]^2} = \frac{1}{[LT^{-1}]^2}$$
$$= [L^{-2}T^2] = [M^0L^{-2}T^2]$$

25. Match Column I and Column II

#### Column I

#### Column II

- (i) Interference
- (P) Coherent sources
- (ii) Brewster's Law
- (Q)  $\mu = \frac{1}{\sin C}$
- (iii) Malus Law
- (R)  $\mu = \tan \theta_p$
- (iv) Total Internal
- (S)  $I = I_0 \cos^2 \theta$

reflection

- (A)  $i\rightarrow Q$ ,  $ii\rightarrow S$ ,  $iii\rightarrow R$ ,  $iv\rightarrow P$
- (B)  $i\rightarrow P$ ,  $ii\rightarrow R$ ,  $iii\rightarrow S$ ,  $iv\rightarrow Q$
- (C)  $i\rightarrow P$ ,  $ii\rightarrow S$ ,  $iii\rightarrow R$ ,  $iv\rightarrow Q$
- (D)  $i\rightarrow R$ ,  $ii\rightarrow Q$ ,  $iii\rightarrow S$ ,  $iv\rightarrow P$

Answer (B)

- Sol. (i) Interference patterns can be observed only when coherent sources are used.
  - (ii) Brewster's Law gives angle of polarization  $tan\theta_p = \mu$



(iii) Malus law gives intensity of light after passing through polarizer

$$I = I_0 \cos^2\theta$$

(iv) Critical angle for total internal reflection is given by relation

$$sinC = \frac{1}{\mu}$$

Frequencies of various radiations are given as

 $f_{ij} \rightarrow \text{Visible light}$ 

f. → Radio waves

f<sub>IN</sub> → Ultra Violet waves

Then which of following is true?

- (A)  $f_{v} < f_{r} < f_{UV}$
- (B)  $f_r < f_V < f_{IJV}$
- (C)  $f_{UV} < f_v < f_r$  (D)  $f_{UV} < f_r < f_v$

# Answer (B)

Sol. -

- 27. Wavelength of characteristic X-ray depends on which property of target?
  - (A) A

- (B) Z
- (C) Melting point
- (D) All of these

#### Answer (B)

Sol. 
$$E = \frac{hC}{\lambda}$$

$$F \propto 7^2$$

$$\therefore \frac{1}{\lambda} \propto Z^2$$

$$= \lambda \propto \frac{1}{\sqrt{Z}}$$

- 28. The energy of the fast neutrons emitted in a nuclear fission reactor is approximately \_\_\_\_
  - (A) 10 MeV
- (B) 2 KeV
- (C) 2 MeV
- (D) 20 MeV

#### Answer (C)

29. In radioactive reaction

$${}^{A}_{Z}X \rightarrow^{A}_{Z+1}X_{1} \rightarrow^{A}_{Z+2}X_{2} \rightarrow^{A-4}_{Z}X_{3} \rightarrow^{A-4}_{Z+1}X_{4}$$

- (A)  $\beta^-, \beta^-, \alpha, \alpha$
- (B)  $\beta^-, \beta^-, \beta^+, \alpha$
- (C) β-,β-,β-,α
- (D)  $\beta^-, \beta^-, \alpha, \beta^-$

# Answer (D)

Sol. In α-decay (<sup>4</sup><sub>2</sub>He) mass number decreases by 4 and atomic no. decreases by 2.

In  $\beta^-$  - decay  $(n \to p^+ + e^-)$  mass number remains same while atomic no. increases by 1.

$${}_{Z}^{A}X \xrightarrow{\beta^{-}decay} {}_{Z+1}^{A}X \xrightarrow{\beta^{-}decay}$$

$$A_{Z+2}^{A}X_2 \xrightarrow{\alpha-decay} A_{Z}^{A-4}X_3 \xrightarrow{\beta^--decay} A_{Z+1}^{A-4}X_4$$

- 30. In CE transistor amplifier, the collector junction has bias and emitter junction has bias.
  - (A) reverse, forward
- (B) forward, forward
- (C) reverse, reverse
- (D) forward, reverse

# Answer (A)

Sol. -

- 31. When carrier wave of 2.5 MHz frequency is amplitude modulated, the resulting AM wave has maximum amplitude of 15 V and minimum amplitude of 10 V. The modulation index is \_\_\_\_\_.
  - (A) 10%
- (B) 20%
- (C) 30%
- (D) 40%

# Answer (B)

$$= A_c + A_m = 15 \text{ V}$$

$$A_{min} = 10 \text{ V}$$

$$= A_c - A_m = 10 \text{ V}$$

$$2A_{m} = 5$$

from 
$$(A) + (B)$$

$$2A_{c} = 25$$

modulation index.

$$\mu = \frac{A_m}{A_c} = \frac{5}{25} = \frac{1}{5}$$

$$=\frac{1}{5}\times100\%=20\%$$

- 32. Which of the following is wrong for interference fringes?
  - (A) Distance between two consecutive fringes is constant
  - (B) All bright fringes are equally bright
  - (C) Fringes are due to limited portion of wave front
  - (D) Fringes are due to the use of coherent sources

#### Answer (C)

Sol. -



- 33. A ray of light travelling in impure water is incident on a glass plate immersed in it. When the angle of incidence is 51°, the reflected ray is totally plane polarized. Given that refractive index of impure water is 1.4. The refractive index of glass should be \_\_\_\_  $(tan51^{\circ} = 1.235)$ 
  - (A) 1.53
- (B) 1.34
- (C) 1.64
- (D) 1.73

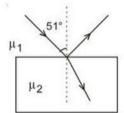
# Answer (D)

Sol. Using Brewster's law

$$\tan\theta_p = \mu_{21} = \frac{\mu_2}{\mu_1}$$



$$= \mu_2 = 1.4 \times 1.235$$
  
= 1.73



- 34. A coil having 200 turns has a surface area of 0.15 m2. A magnetic field of strength 0.2 T applied perpendicular to this changes to 0.6 T in 0.4 s, then the induced emf in the coil is V.
  - (A) 15

(B) 30

(C) 45

(D) 60

#### Answer (B)

Sol. 
$$E = \frac{\Delta \phi}{\Delta t} = \frac{N(\Delta B)A}{\Delta t}$$

$$=\frac{200\times(0.6-0.2)\times0.15}{0.4}=30V$$

- 35. A sinusoidal A.C. current flows through a resistor of resistance 10Ω. If the peak current is 2A flowing through the resistor then the power dissipated in
  - (A) 10

(B) 20

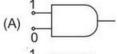
(C) 30

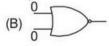
(D) 40

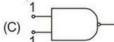
# Answer (B)

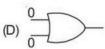
Sol. 
$$P = i_{\text{rms}}^2 R = \left(\frac{i_{\text{max}}}{\sqrt{2}}\right)^2 R = \left(\frac{2}{\sqrt{2}}\right)^2 \times 10$$

36. Which of following gates produces output of 1?









## Answer (B)

- Sol. (A) Output of AND gate is 0
  - (B) Output of NOR gate is 1
  - (C) Output of NAND gate is 0
  - (D) Output of OR gate is 0
- 37. The value of  $\beta$  of a transistor is 19. The value of  $\alpha$ will be
  - (A) 0.99
- (B) 0.98
- (C) 0.93
- (D) 0.95

# Answer (D)

Sol. 
$$\frac{1}{\alpha} = 1 + \frac{1}{\beta} = 1 + \frac{1}{19}$$
  
=  $\alpha = 0.95$ 

- 38. If the half-life of a radioactive element is 10 hr, its average life = hr.
  - (A) 14.4
- (B) 6.93
- (C) 1.44
- (D) 0.693

## Answer (A)

Sol. Average life

$$\tau = \frac{t_{1/2}}{\ln 2} = \frac{10}{0.693}$$

≈ 14.4 hrs.

is the wavelength of photon of energy 35 KeV.

$$h = 6.625 \times 10^{-34} \text{ J}^{-2}, c = 3 \times 10^8 \text{ m/s},$$

1 eV = 
$$1.6 \times 10^{-19} \text{ J}$$
.

- (A) 3.5 mm
- (B) 35 Å
- (C)  $35 \times 10^{-12}$  mm
- (D) 3.5 Å

# Answer (C)

Sol. 
$$E = \frac{hc}{\lambda}$$

$$\Rightarrow \lambda = \frac{hc}{E} = \frac{1242 \text{ eV} - \text{nm}}{35 \times 10^3 \text{ eV}}$$

$$\approx 35 \times 10^{-3} \text{ nm}$$

$$= 35 \times 10^{-12} \text{ m}$$

- 40. The band gaps of an insulator, conductor and semi conductor are respectively  $\mathbf{E}_{\mathrm{g1}}$ ,  $\mathbf{E}_{\mathrm{g2}}$  and  $\mathbf{E}_{\mathrm{g3}}$ . The relationship between them is given as \_\_\_

  - (A)  $E_{g1} < E_{g2} > E_{g3}$  (B)  $E_{g1} > E_{g2} > E_{g3}$
  - (C)  $E_{a1} > E_{a2} < E_{a3}$  (D)  $E_{a1} < E_{a2} < E_{a3}$

#### Answer (C)

Sol. Band gap is largest in insulators while it is smallest in conductors.

# PART-B: CHEMISTRY

- 41. If the edge length of a body centred unit cell is 400pm, what will be the approximate radius of the atom present in it? (in pm)
  - (A) 173
- (B) 141
- (C) 200
- (D) 924

# Answer (A)

Sol. a = 400pm

For Body centered unit cell;

$$\sqrt{3}a = 4r$$

$$\therefore \frac{\sqrt{3}(400)}{4} = r$$
  $r = 173.2 \text{ pm}$ 

- 42. Which of the following is Ferromagnetic?
  - (A) MnO
- (B) CrO<sub>2</sub>
- (C) O2
- (D) Fe<sub>3</sub>O<sub>4</sub>

# Answer (B)

- Sol. Fe, Co, Ni and CrO2 are ferromagnetic in nature
- What is the normality of aqueous solution of H<sub>2</sub>SO<sub>4</sub> having pH = 1.
  - (A) 0.1 N
- (B) 0.05 N
- (C) 1 N
- (D) 0.5 N

# Answer (A)

**Sol.** 
$$H_2SO_4 \rightarrow 2H_{(aq)}^+ + SO_{4(aq)}^{2-}$$

For  $[H^+] = 0.1M$ ; the  $p^H = 1$ 

Molarity of  $H_2SO_4 = 0.05 \text{ M}$ 

- $\therefore$  Normality of H<sub>2</sub>SO<sub>4</sub> = M<sub>H<sub>2</sub>SO<sub>4</sub></sub> x n<sub>f</sub>
  - $= 0.05 \times 2$
  - = 0.1 N
- 44. Which of the following mixture is non-ideal solution?
  - (A) Chlorobenzene and bromobenzene
  - (B) Benzene and toluene
  - (C) Chloroform and acetone
  - (D) Bromoethane and chloroethane

# Answer (C)

Sol. (CHCl<sub>3</sub> + H<sub>3</sub>C - C - CH<sub>3</sub>) forms a non-ideal solution showing negative deviation

- 45. Which solution is isotonic with 6% w/v aqueous solution of urea? [Mole mass of Urea = 60 gm. mol<sup>-1</sup>]
  - (A) 0.1 M NaCl
- (B) 0.5 M NaCl
- (C) 0.25 M NaCl
- (D) 1 M NaCl

# Answer (B)

**Sol.** Isotonic solution means  $(\pi_1 = \pi_2)$ 

Isotonic presure for 6% w/v aqueous soltuion of area  $(\pi_1)$  = icRT

6 gms of area is present in 100ml solution

$$\therefore C = \frac{6}{60} \times \frac{1000}{100} = 1$$

$$\pi_1 = (1) (1) RT (\because i \text{ of area} = 1)$$
  
 $\pi_1 = RT$ 

.. For 0.5 M NaCl solution, i = 2

so  $\pi_2 = (2) (0.5 \text{ RT})$ 

$$\pi_2 = RT$$

46. In which metal container, the aqueous solution of CuSO₄ can be stored?

$$E_{Cu^{3+}/Cu}^{0} = 0.34V$$

$$E_{Fe/Fe^{2+}}^0 = 0.44 \text{ V}, E_{AI/AI^{3+}}^0 = 1.66 \text{ V}$$

$$E_{Ni/Ni^{2+}}^{0} = 0.25V, E_{Ag^{+}/Ag}^{0} = 0.80V$$

- (A) Fe
- (B) Ni
- (C) Aq
- (D) AI

#### Answer (C)

- Sol. Since the SRP value of Ag+/Ag = 0.80 V
  - .. aq solution of CuSO4 can be stored in Ag as

$$E_{Cu^{2+}/Cu}^{0} = 0.34V$$

- 47. For how much time, 10 ampere electric current should be passed through a dilute aqueous NiSO<sub>4</sub> solution during electrolysis using inert electrode, in order to get 5.85 gm Nickel? [At. mass of Ni = 58.5gm]
  - (A) 1930 sec.
- (B) 3860 sec.
- (C) 965 sec.
- (D) 9650 sec.

#### Answer (A)

Sol. By Faraday's 1st law of electrolysis m = zit

$$5.85 = \frac{\mathsf{E}}{\mathsf{F}}(\mathsf{i})(\mathsf{t})$$

( : E = Equivalent mass of Ni)

$$E = \frac{58.5}{2}$$
 5.85 =  $\frac{58.5}{2} \frac{(10)}{(96500)}(t)$ 

.: t = 1930 sec.

48. What will be the oxidation potential for the following hydrogen half cell at 1 bar pressure and 25°C temperature?

$$Pt \left| H_{2(g)} \right| HCI_{(aq)} pH = 3$$

- (A) 0.177 V
- (B) 0.188 V
- (C) 0.059 V
- (D) 0.000 V

# Answer (A)

**Sol.** For the half cell;  $Pt|H_{2(g)}|HCl_{(aq)}pH = 3$ 

 $H_{2(q)} \rightarrow 2H^{+}_{(aq)} + 2e^{-}$  by Nernst equation

$$E_{cell} = E_{Cell}^{\circ} - \frac{0.0591}{n} log \frac{[H^{+}]^{2}}{p_{H_{2}}}$$

$$E_{cell} = 0 - \frac{0.0591}{2} log \frac{(10^{-3})^2}{1} \left[ \therefore [H^+] = 10^{-3} M \right]$$

$$E_{cell} = -\frac{0.0591}{2}(-6)$$

$$E_{cell} = 0.177 V$$

- 49. Which ore does not contain carbonate?
  - (A) Malachite
- (B) Ciderite
- (C) Calamine
- (D) Zincite

## Answer (D)

- Sol. Zincite is ZnO, so does not contain carbonate
- 50. Which is the correct order of metallurgy for the extraction of copper metal?
  - (A) Concentration → roasting → smelting
     → bessimerisation
  - (B) Concentration  $\rightarrow$  smelting  $\rightarrow$  roasting  $\rightarrow$  bessimerisation
  - (C) Concentration → smelting → bessimerisation → roasting
  - (D) Concentration  $\rightarrow$  roasting  $\rightarrow$  bessimerisation  $\rightarrow$  smelting

#### Answer (A)

Sol. In the extraction of copper metal; the correct order is

Concentration  $\rightarrow$  Roasting  $\rightarrow$  Smelting  $\rightarrow$  Bessimerisation

51. How many grams of Cl<sub>2</sub> gas will be obtained by the complete reaction of 31.6 gm of potassium permanganate with hydrochloric acid?

[Mole mass of  $KMnO_4 = 316 \text{ gm/mol}$ ]

- (A) 35.5
- (B) 17.75

(C) 71

(D) 142

# Answer (B)

- Sol. 2KMnO<sub>4</sub> + 16HCl → 2MnCl<sub>2</sub>+5Cl<sub>2</sub> + 2KCl + 8H<sub>2</sub>O
  2 moles KMnO<sub>4</sub> produces 5 moles of Cl<sub>2</sub>
  - 1 mole of  $KMnO_4$  will produce  $\frac{5}{2}$  molles of  $Cl_2$
  - $\therefore \ \frac{31.6}{316} \ \text{moles of KMnO4 will produce} \ \frac{1}{4} \ \text{moles of} \ \text{Cl}_2$
  - ∴ Mass of  $Cl_2$  gas =  $\frac{71}{4}$  = 17.75 gms.
- 52. What is the structure of XeOF<sub>4</sub>?
  - (A) Pyramidal
- (B) Trigonal bipyramidal
- (C) Square pyramidal
- (D) Square bipyramidal

# Answer (C)

Sol. XeOF4

Hybridisation of Xe = 
$$5 + \frac{1}{2}[8 - 6]$$
  
=  $5 + 1$   
=  $sp^3d^2$ 

Hence by the VSEPR theory, due to 5 bond pair & 1 lone pair of e<sup>-</sup>. The shape of XeOF<sub>4</sub> is square pyramidal

- 53. Which one is not an allylic halide?
  - (A) 1 Chloro but 2 ene
  - (B) 1 Chloro but 1 ene
  - (C) 3 Chloro cyclo hex 1 ene
  - (D) 3 Chloro prop 1 ene.

#### Answer (B)

**Sol.** 1 – Chloro but – 1 – ene 
$$\Rightarrow$$
 HC = CH-CH<sub>2</sub>-CH<sub>3</sub> Cl

Hence the above is not an allylic halide but vinylic halide

- 54. Which is the main organic product obtained by the reaction of 2, 2, 2 trichloro ethanal with calcium hydroxide?
  - (A) Chloroform
  - (B) Carbon tetrachloride
  - (C) Methylene chloride
  - (D) Trichloro ethane

#### Answer (A)

Sol. On reaction of 2,2,2 - trichloro ethanal (Chloral) with Ca(OH)<sub>2</sub>; chloroform (CHCl<sub>3</sub>) is the main organic product obtained.



- 55. Which of the following compound is optically inactive?
  - (A) 2 Hydroxy propanoic acid
  - (B) 2, 3 Dichloro butane
  - (C) 3 Chloro but 1 ene
  - (D) 2, 2 Dichloro pentane

#### Answer (D)

- Sol. 2, 2 Dichloropentane  $\Rightarrow$  H<sub>3</sub>C–C–CH<sub>2</sub>–CH<sub>2</sub>–CH<sub>3</sub>
  - .. The above compound is optically inactive
- 56. Which of the organic products of the following reactions has the least boiling point?

(A) 
$$CH_3 - CH_2 - CHO \xrightarrow{NaBH_4}$$

(B) 
$$CH_3 - C - CH_3 \xrightarrow{\text{NaBH}_4} CH_2O \xrightarrow{\text{NaBH}_$$

(C) 
$$CH_3 - CH_2 - COOH \xrightarrow{\text{LiA}|H_4} \rightarrow$$

(D) 
$$CH_3 - CH = CH_2 \xrightarrow{(BH_3)_2} \xrightarrow{(BH_3)_2}$$

## Answer (B)

**Sol.** In the reaction A,C,D the product formed is propan– 1-ol. whereas in the reaction – B

$$H_3C-C-CH_3 \xrightarrow{NaBH_4} H_3C-CH-CH_3$$
  
O
OH

- .. Due to weaker force of attraction in Propan-2-ol; it has least boiling point.
- 57. Which is the final product obtained by the reaction of a grignard reagent ethyl Magnesium bromide with propanone?
  - (A) Pentane 2 ol
  - (B) 2 Methyl butane 2 ol
  - (C) Pentane -1- ol
  - (D) 3 Methyl butane 2 ol

#### Answer (B)

Sol. 
$$C_2H_5MgBr + H_3C-C-CH_3 \rightarrow H_3C^2-C-OH_1$$

$$C_2H_5MgBr + H_3C-C-CH_3 \rightarrow H_3C^2-C-OH_1$$

$$C_3CH_2-CH_3$$

$$C_3CH_2-CH_3$$

$$C_3CH_2-CH_3$$

$$C_3CH_2-CH_3$$

$$C_3CH_2-CH_3$$

$$C_3CH_3-CH_3$$

$$C_3$$

+ Mg(OH)Br

.. Final product formed is 2-Methyl - butan-2-ol

58. Which is the correct structural formula of Aspirin?

- 59. The units for the rate constant and the rate of reaction are same for a reaction. What will be the order of the reaction?
  - (A) First
- (B) Zero
- (C) Second
- (D) Third

#### Answer (B)

**Sol.** Unit of rate constant (k) =  $(conc)^{1-n}$  (s)<sup>-1</sup>

n = order of the reaction

The rate law of the reaction is

Rate = K [Reactant]<sup>n</sup>

For unit of Rate = Rate constant (k); n should be equal to 0

- .. Order is zero
- 60. At 27° C temperature, time required for 75% completion of a first order reaction is 20 seconds. What will be its rate constant?
  - (A) 0.693 sec-1
- (B) 0.0693 sec-1
- (C) 0.693 sec-1 mole-1 lt (D) 0.0693 sec-1 mole-1 lt

#### Answer (B)

Sol. For 1st order reaction;

$$Kt = \ln \left( \frac{A_o}{A_t} \right)$$

$$K (20) = In \left( \frac{A_o}{0.25A_o} \right)$$

$$K(20) = In(4)$$

$$K = \frac{2\ln 2}{20} = \frac{0.693}{10} = 0.0693 \, s^{-1}$$



- 61. Which statement is incorrect for a catalyst?
  - (A) It decreases the activation energy of a reaction
  - (B) It increases the proportion of products in less time
  - (C) It does not affect the equilibrium constant
  - (D) It increases the free energy change for the reaction

## Answer (D)

Sol. A Catalyst can,

- Increase the rate of reaction by decreasing the activation energy
- (ii) Also increase the proportion of products per unit time.
- (iii) Does not alter equilibrium established reaction. Hence does not alter equilibrium constant.
- (iv) Does not alters the valueof  $\Delta\, {\rm G}$  and  $\Delta\, {\rm H}$  Hence the correct answer is (D)
- During electrophoresis of colloidal sol of Fe(OH)<sub>3</sub>, the colloidal particles
  - (A) Move towards anode
  - (B) Move towards cathode
  - (C) Move towards anode and cathode both
  - (D) Do not move

## Answer (B)

- **Sol.** Fe(OH)<sub>3</sub> is a positively charged colloid. Hence under the influence of electricity these particles can migrate towards cathode.
- 63. In manufacturing of sulphuric acid in presence of platinum catalyst, which metal impurity acts as catalytic poison?
  - (A) Cu

(B) Cr

- (C) Fe
- (D) V

#### Answer (A)

- **Sol.** In production of sulphuric acid, in the presence of platinum catalyst, the impurity of copper decreases the efficiency of the catalyst. It is called catalytic poison.
- 64. Which ion has the least value of theoretical magnetic moment?
  - (A) Ti<sup>3+</sup>
- (B) Co3+
- (C) Cr3+
- (D) V3+

#### Answer (A)

**Sol.** Magnatic moment  $\mu = \sqrt{n(n+2)}$  BM

where n = no. of unpaired electrons

As the number of unpaired electrons increases, magnetic moment also increases.

In the given options.

 $Ti^{+3} = [Ar]3d^{1}4s^{0}$ ; n=1

Co+3= [Ar]3d64so;n=4

 $Cr^{+3} = [Ar]3d^34s^o; n=3$ 

V+3= [Ar]3d2 4so;n=2

Hence the correct answer is (A)

- 65. Which of the following mixture can form an alloy?
  - (A) Fe, Mn, Mg
  - (B) Cr, Co, Na
  - (C) Fe, Ni, Cr
  - (D) Ni, Mg, Na

## Answer (C)

Sol. Alloy is the combination of two or more metals.

According to Hume-Rothery ratio, metals which have

- (i) Similar electronic structure in the valence shell
- (ii) Similar crystal structure and
- (iii) Difference in the radius should be less than 15% can form alloy.

Hence Fe, Ni, Cr – belongs to 3d – series can form alloy.

- 66. Which of the following statements is incorrect?
  - (A) K<sub>4</sub> [Ni(CN)<sub>4</sub>] is square planar while K<sub>2</sub>[Ni(CN)<sub>4</sub>] is paramagnetic.
  - (B) K<sub>2</sub> [Ni(CN)<sub>4</sub>] is diamagnetic while K<sub>2</sub>[NiCl<sub>4</sub>] is paramagnetic.
  - (C) K<sub>4</sub> [Ni(CN)<sub>4</sub>] and K<sub>2</sub>[Ni(CN)<sub>4</sub>] both have same magnetic moment
  - (D) K<sub>2</sub> [NiCl<sub>4</sub>] and K<sub>4</sub> [Ni(CN)<sub>4</sub>] both have same geometrical shapes

#### Answer (A)

Sol. Incorrect option is (A) where

K<sub>4</sub>[Ni(CN)<sub>4</sub>] sp<sup>3</sup> Tetrahedran (Diamagnetic)

K<sub>2</sub>[Ni(CN)<sub>4</sub>] dsp<sup>2</sup> square planar (Diamagnetic)

K<sub>2</sub>[NiCl<sub>4</sub>] sp<sup>3</sup> Tetrahedran (Paramagnetic)

- The aqueous solution of which of the following complex has the leaste conductivity under identical conditions.
  - (A) Hexa agua chromium (III) chloride
  - (B) Tetra aqua dichlorido chromium (III) chloride
  - (C) Penta aqua chlorido chromium (III) chloride
  - (D) Tri aqua trichlorido chromium (III)

#### Answer (D)

- **Sol.** The complex which produce least number of ions in aqueous solution will show least conductivity.
  - (A) [Cr(H2O)6]Cl3; 4 ions
  - (B) [Cr(H2O)4Cl2]Cl; 2 ions
  - (C) [Cr(H2O)5Cl]Cl2; 3 ions
  - (D) [Cr(H<sub>2</sub>O)<sub>3</sub>Cl<sub>3</sub>]; No ions.



- 68. Which complex possess facial isomer?
  - (A) [Co(NH<sub>3</sub>)<sub>4</sub>CO<sub>3</sub>]CI
  - (B) [Co(NH<sub>3</sub>)<sub>3</sub>(NO<sub>2</sub>)<sub>3</sub>]
  - (C)  $K[Fe(NH_3)_2(CN)_4]$
  - (D) [Ni(H2O)4(NH3)2]SO4

# Answer (B)

**Sol.** Facial and Meridional isomersm shown by the complex

[MA<sub>3</sub>B<sub>3</sub>] type

Ex:- [Co(NH<sub>3</sub>)<sub>3</sub>(NO<sub>2</sub>)<sub>3</sub>]

- 69. Which of the following is not a final product obtained by cross aldol condensation of ethanal and propanal?
  - (A) But-2-enal
  - (B) 2-Methyl-pent-2-enal
  - (C) 3-Methyl-but-2-enal
  - (D) Pent-2-enal

# Answer (C)

on crossed aldol condensation gives.

$$\begin{array}{c} O \\ \parallel \\ 2 \text{ H}_3\text{C-CH}_2\text{-C-H} \xrightarrow{\text{OH}^-} \\ \end{array} \begin{array}{c} \text{H}_3\text{C-CH}_2\text{-CH} = \text{C-C-H} \\ \text{CH}_3 \\ \text{2-methylpent-2-enal} \end{array}$$

- 70. Which is the main functional group in Acrolein?
  - (A) Nitrile
- (B) Alkene
- (C) Aldehyde
- (D) Ester

#### Answer (C)

- **Sol.** Acrolein H<sub>2</sub>C=C-C-H Hence the main functional group is aldehyde
- 71. Which of the following compound upon oxidation gives isophthalic acid?
  - (A) o-Xvlene
- (B) m-Xylene
- (C) p-Xylene
- (D) m-Cresol

#### Answer (B)

Sol. Isophthalic acid is

$$\begin{array}{c} & \xrightarrow{\text{CH}_3} \text{alk.KMnO}_4 \\ & \xrightarrow{\text{Oxidation}} \end{array} \xrightarrow{\text{CH}_3} \begin{array}{c} \text{CH}_3 \\ \text{CH}_3 \\ \text{m-xylene} \end{array}$$

Note:

- 72. Which is the oxidized product obtained when benzene diazonium chloride reacts with phosphonic acid in presence of water?
  - (A) Benzene
- (B) Phenol
- (C) Chloro benzene
- (D) Phosphorus acid

# Answer (D)

Sol.



73. Which of the following compound is the most basic?

$$(A) \bigcirc (B) \bigcirc (B) \bigcirc (C) \bigcirc (D) \bigcirc (D)$$

#### Answer (B)

Sol.

because of more pronounced + R effect of  $-\ddot{O} - CH_3$  group.

- \* Basic strength α EDG.
- 74. The number of  $\sigma$  and  $\pi$  bonds in orange azo dye is \_\_\_\_ and \_\_\_ respectively.
  - (A) 26 and 7
- (B) 24 and 7
- (C) 27 and 7
- (D) 26 and 6

## Answer (A)

Sol. Orange dye is

It is obtained by the reaction between B.D.C and phenol.

$$H \longrightarrow H \longrightarrow H \longrightarrow H \longrightarrow H \longrightarrow H$$

Total  $\sigma$  bonds = 26

Total  $\pi$  bonds = 7

- 75. Which one is a purine base?
  - (A) Cytosine
- (B) Thymine
- (C) Uracil
- (D) Guanine

## Answer (D)

- **Sol.** [Guanine and adenine] are purine bases Cytosine,Uracil,Thymine are pyrimidine bases.
- 76. Which of the following amino acid has pH greater than 7?
  - (A) Glycine
  - (B) Lysine
  - (C) Glutamic acid
  - (D) Alanine

#### Answer (B)

Sol. pH should be more for basic amino acids.

Lysine is basic amino acid.

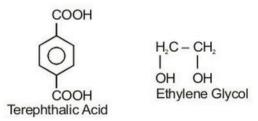
Hence, its pH > 7.

Lysine

77. Which is the correct structural formula for terylene?

#### Answer (A)

Sol. Terylene is the co-polymer of terephthalic acid and Ethylene glycol



- 78. Which are the monomers of Buna N?
  - (A) Buta 1, 3-diene and prop -2-ene-1-nitrile
  - (B) Buta 1, 2-diene and acrylonitrile
  - (C) Buta 1, 3-diene and prop-1-ene-1-nitrile
  - (D) Buta 1, 2-diene and prop-2-ene-1-nitrile

# Answer (A)

Sol. Buna - N

$$H_2C = CH - CH = CH_2 + H_2C = CH - C = N$$

79. Choose the correct option for the suitable match between Column I and Column II

Column - I

Column - II

- (P) Artificial Sweetner
- (L) Caramel
- (Q) Food Preservative
- (M) Ascorbic acid
- (R) Anti Oxidants
- (N) Alitame
- (S) Food colours

- (A)  $P \rightarrow N$ ,  $Q \rightarrow O$ ,  $R \rightarrow M$ ,  $S \rightarrow L$
- (B)  $P \rightarrow N$ ,  $Q \rightarrow M$ ,  $R \rightarrow O$ ,  $S \rightarrow L$
- (C)  $P \rightarrow N$ ,  $Q \rightarrow O$ ,  $R \rightarrow L$ ,  $S \rightarrow M$
- (D)  $P \rightarrow L$ ,  $Q \rightarrow O$ ,  $R \rightarrow M$ ,  $S \rightarrow N$

# Answer (A)

Sol. Artificial sweetner - Alitame

Food Preservative - Sorbic acid

Anti oxidant - Ascorbic acid

Food Colour - Caramel.

- 80. Which of the following drugs gives releif from anxiety and stress?
  - (A) Luminal
- (B) Aspirin
- (C) Ofloxacin
- (D) Mestranol

## Answer (A)

Sol. Barbiturates can release from stress and anxiety.



# Time: 1 hr.

# Answers & Solutions

# **GUJCET - ME- 2018**

(Mathematics)

#### Important Instructions:

- 1. The Mathematics test consists of 40 questions. Each question carries 1 mark. For each correct response, teh candidate will get 1 mark. For each incorrect response, mark will be deducted. The maximum marks are 40.
- 2. This Test is of 1 hour duration
- 3. Use Black Ball Point Pen only for writing particulars on OMR Answer Sheet and marking answers by darketing the circle ".
- 4. Rough work is to be done on the space provided for this purpose in the Test Booklet only.
- 5. On completion of the test, the candidate must handover the Answer Sheet to the Invigilator in the Room / Hall. The candidates are allowed to take away this Test Booklet with them.
- 6. The Set No. for this Booklet is . Mark sure that the Set No. printed on the Answer sheet is the same as that on this booklet. In case of discrepancy, the candidate should immediately report teh matter to the Invigilator for replacement of both the Test Booklet and the Answer Sheet.
- 7. The candidate should ensure that the Answer Sheet is not folded. Do not make any stray marks on the Answer Sheet
- 8. Do not write your Seat No. anywhere else, except in the specified space in the Test Booklet/Answer Sheet.
- 9. Use of White fluid for correction is not permissible on the Answer sheet.
- 10. Each candidate must show on demand his / her Admission Card to the Invigilator.
- 11. No candidate, without special permission of the Superintendent or Invigilator, should leave his/her seat.
- 12. Use of Manual Calculator is permissible.
- 13. The candidate Should not leave the Examination Hall handling over their Answer Sheet to the Invigilator on duty and must sign the Attendance Sheet (Patrak-01). Cases where a candidate has not signed the Attendance Sheet (Patrak-01) will be deemed not to have handed over the Answer Sheet and Will be dealt with as an unfair means case.
- 14. The candidates are governed by all Rules and Regulations of the Board with regard to their conduct in the Examination hall. All cases of unfair means will be dealt with as per Rules and Regulations of the Board.
- 15. No Part of the Test Booklet and Answer Sheet shall be detached under any circumstances.
- 16. The candiates will write the Correct Test Booklet Set No. as given in the Test Booklet / Answer Sheet in the Attendance Sheet. (Patrak 01).



M.M.: 40

# **PART-A: MATHEMATICS**

- 1. Where does  $f(x) = x + \sqrt{1-x}$ ; 0 < x < 1 decrease?
  - (A) (0,1)
- (B)  $(0,\frac{3}{4})$
- (C)  $(\frac{3}{4}, 1)$
- (D)  $(3/4,\infty)$

Answer (C)

Sol.  $f(x) = x + \sqrt{1-x}$ 

- $f'(x) = 1 \frac{1}{2\sqrt{1-x}} = 0 \implies x = \frac{3}{4}$
- $\therefore$  Interval of decrease is  $(\frac{3}{4},1)$
- 2. If  $f'(x) = 2 \frac{5}{x^4}$  and  $f(1) = \frac{14}{3}$ , then f(-1) =
  - (A)  $\frac{11}{3}$
- (B)  $-\frac{8}{3}$
- (C)  $-\frac{14}{3}$
- (D) 0

Answer (B)

**Sol.**  $f'(x) = 2 - \frac{5}{x^4}$ 

$$\Rightarrow$$
  $f(x) = 2x + \frac{5}{3x^3} + c$ 

Now,  $f(1) = \frac{14}{3}$ 

∴ c = 1

$$\Rightarrow$$
  $f(x) = 2x + \frac{5}{3x^3} + 1$ 

 $\therefore f(-1) = \frac{-8}{3}$ 

- 3.  $\int \frac{\cos \alpha}{\sin x \cos (x \alpha)} dx = \dots + c \quad \text{where}$ 
  - $0 < x < \alpha < \frac{\pi}{2}$  and  $\alpha$  constant
  - (A)  $\log |\cot x + \tan \alpha|$  (B)  $\log |\tan x + \cot \alpha|$
  - (C)  $-\log |\tan x + \cot \alpha|$  (D)  $-\log |\cot x + \tan \alpha|$

# Answer (D)

Sol. 
$$\int \frac{\cos \alpha \, dx}{\sin x \, \cos(x - \alpha)}$$

$$= \int (\cot x + \tan(x - \alpha)) dx$$

$$= \ln \left| \frac{1}{\cot x \cos \alpha + \sin \alpha} \right| + c$$

- =  $-\ln(\cot x \cos \alpha + \sin \alpha) + c$
- $= -\ln(\cot x + \tan \alpha) + \cot \alpha$
- 4.  $\int \frac{e^{\cot^{-1}x}}{1+x^2} (x^2 x + 1) dx = \dots + c$ 
  - (A) x . e cot-1 x
- (B) e<sup>cot-1</sup> x
- (C)  $\frac{e^{\cot^{-1}x}}{1+x^2}$
- (D) -e<sup>cot-1</sup> x

Answer (A)

Sol.  $\int \frac{e^{\cot^{-1}x}}{1+x^2} (x^2-x+1) dx$ 

Let  $\cot^{-1} x = t$ 

$$\Rightarrow -\frac{1}{1+x^2}dx = dt$$

$$\int e^{t} (\cot t - \csc^{2} t) dt$$

et cot t + c

x ecot-1x + C

- 5.  $\int_{0}^{\frac{\pi}{2}} (x [\cos x]) dx = \dots$  where [t] = greatest integer less or equal to t
  - (A)  $\frac{\pi^2}{8} \frac{\pi}{8}$
- (B)  $\frac{\pi^2}{9}$
- (C)  $\frac{\pi^2}{8} 1$
- (D)  $\frac{\pi}{4}$

# Answer (B)

Sol. 
$$\int_{0}^{\frac{\pi}{2}} (x - [\cos x]) dx$$

$$\left[\frac{x^2}{2} - 0\right]_0^{\frac{\pi}{2}}$$

$$\frac{\pi^2}{2}$$

6. If 
$$\int_{\log 2}^{a} \frac{e^{x}}{\sqrt{e^{x}-1}} dx = 2$$
, then  $a =$ 

- (A) 2log2
- (B) log2
- (C) log5
- (D) 0

# Answer (C)

Sol. 
$$\int_{\log 2}^{a} \frac{e^{x}}{\sqrt{e^{x}-1}} dx = 2$$

$$\implies \left[2\sqrt{e^x-1}\right]_{\log 2}^a = 2$$

$$\Rightarrow 2\sqrt{e^a-1}-2=2$$

$$\Rightarrow$$
  $2\sqrt{e^a-1}=4$ 

$$\Rightarrow \sqrt{e^a - 1} = 2$$

$$\Rightarrow$$
  $e^a - 1 = 4$ 

$$\Rightarrow$$
  $e^a = 5$ 

$$\Rightarrow$$
 a =  $\log_e 5$ 

7. 
$$\int_{0}^{\sqrt{2}} \sqrt{2 - x^2} dx =$$

(A) π

(B)  $-\frac{\pi}{2}$ 

(C) 0

(D)  $\frac{\pi}{2}$ 

# Answer (D)

Sol. 
$$\int_{0}^{\sqrt{2}} \sqrt{2-x^2} dx$$

$$= \left[ \frac{x}{2} \sqrt{2 - x^2} + \frac{2}{2} \sin^{-1} \left( \frac{x}{\sqrt{2}} \right) \right]_0^{\sqrt{2}}$$

$$=\frac{\pi}{2}$$

- Area of the region bounded by rays |x|+y=1 and Xaxis is
  - (A) 2

(B) 1

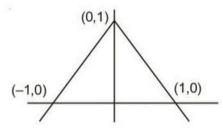
(C)  $\frac{1}{2}$ 

(D)  $\frac{1}{4}$ 

# Answer (B)

Sol. Area bounded by rays

$$|x|+y=1$$
 and X-axis



$$2\left(\frac{1}{2}\times1\times1\right)=1$$

- 9. If area bounded by the curves  $x = ay^2$  and  $y = ax^2$  is 1, then a =\_\_\_\_ (a>0)
  - (A)  $\frac{1}{3}$
- (B)  $\frac{1}{\sqrt{3}}$

(C)  $\frac{1}{2}$ 

(D)  $\frac{1}{3}$ 

# Answer (B)

**Sol.** Area bounded by  $y^2 = 4ax$  and  $x^2 = 4by$ 

given by 
$$\left| \frac{16ab}{3} \right| = 1$$

$$\left| \frac{16}{3} \times \frac{1}{4a} \times \frac{1}{4a} \right| = 1$$

$$a^2 = \frac{1}{3}$$

$$a = \frac{1}{\sqrt{3}} \qquad (a > 0)$$

10. The solution of the differential equation

$$2x\frac{dy}{dx} - y = 0; y(1) = 2$$
 represents ......

- (A) Parabola
- (B) Straightline
- (C) Circle
- (D) Ellipse

# Answer (A)

$$\textbf{Sol. } 2x\frac{dy}{dx} - y = 0$$

$$\frac{dy}{dy} = \frac{dx}{2x} \implies \int \frac{dy}{y} = \int \frac{dx}{2x}$$

$$\ln y = \ln \sqrt{x} + \ln c$$

$$y = c\sqrt{x}$$
 as  $y(1) = 2$ 

$$c = 2$$

$$y = 2\sqrt{x}$$

$$x = \frac{y^2}{4}$$

.: Parabola

11. Particular solution of differential equation

$$e^{\frac{dy}{dx}} = x$$
;  $y(1) = 3$ ;  $x > 0$  is.....

(A) 
$$y = \log x - x + 4$$

(B) 
$$y^2 = \log x + 4$$

(C) 
$$\log y = x^2 + 4$$
 (D)  $2y = x^2 + 5$ 

(D) 
$$2y = x^2 + 5$$

# Answer (A)\*

Sol. 
$$\frac{dy}{dx} = \log x$$

$$y = x \log x - x + c$$

as 
$$y(1) = 3$$

$$3 = -1 + c$$

$$c = 4$$

$$y = x \log x - x + 4$$

Note: option (A) can be taken, but 'x' is missing

12. The population of a city increases at the rate 3% per year. If at time t the population of city is p, then find equation of p in time t.

(A) 
$$p = 3e^{\frac{3t}{100}}$$

(B) 
$$p = e^{\frac{3t}{100}}$$

(C) 
$$p = ce^{\frac{3t}{100}}$$

(D) 
$$p = \frac{3}{100}e^{3t}$$

# Answer (C)

Sol. 
$$\frac{dp}{dt} = \frac{3}{100}p$$

$$\Rightarrow \int \frac{dp}{p} = \int \frac{3}{100} dt$$

$$\Rightarrow$$
  $\ln p = \frac{3}{100} t + \ln c$ 

$$\Rightarrow$$
  $p = ce^{\frac{3}{100}t}$ 

- 13. If  $\bar{a}$  is unit vector, then  $|\bar{a} \times \hat{i}|^2 + |\bar{a} \times \hat{j}|^2 + |\bar{a} \times \hat{k}|^2 =$ 
  - (A) 1

(B) 0

(C) 2

(D) 3

# Answer (C)

Sol. Let 
$$a = x\hat{i} + y\hat{j} + z\hat{k}$$
;

as 
$$x^2 + y^2 + z^2 = 1$$

$$|\mathbf{a} \times \mathbf{i}|^2 + |\mathbf{a} \times \mathbf{j}|^2 + |\mathbf{a} \times \mathbf{k}|^2$$

$$= y^2 + z^2 + x^2 + z^2 + x^2 + y^2$$

$$= 2(x^2 + y^2 + z^2) = 2$$

- 14. If for unit vectors  $\bar{a}$  and  $\bar{b}$ ,  $\bar{a} + 2\bar{b}$  and  $5\bar{a} 4\bar{b}$ are perpendicular to each other, then  $(\bar{a}^{\,\wedge}\bar{b})$  =
  - $(A) \frac{\pi}{2}$

- (B)  $\frac{\pi}{4}$
- (C)  $\cos^{-1}\frac{1}{2}$
- (D)  $\cos^{-1}\frac{2}{7}$

# Answer (A)

Sol. 
$$(\overline{a} + 2\overline{b}) \cdot (5\overline{a} - 4\overline{b}) = 0$$

$$5-4(\overline{a}\cdot\overline{b})+10(\overline{a}\cdot\overline{b})-8=0$$

$$-3 + b(\overline{a} \cdot \overline{b}) = 0$$

$$\overline{a} \cdot \overline{b} = \frac{1}{2}$$

$$\cos\theta = \frac{1}{2}$$

$$\theta = \frac{\pi}{3}$$

15. If a vector  $\frac{1}{x}$  makes angles with measure  $\frac{\pi}{4}$  and  $\frac{5\pi}{4}$  with positive directions of X-axis and Y-axis

respectively, then x made angle of measure ..... with positive direction of Z-axis

Sol. 
$$\cos \alpha = \frac{1}{2}$$
;  $\cos \beta = -\frac{1}{\sqrt{2}}$ 

Now, 
$$\cos^2 \alpha + \cos^2 \beta + \cos^2 \gamma = 1$$

$$\frac{1}{2} + \frac{1}{2} + \cos^2 \gamma = 1$$

$$\cos^2 \gamma = 0$$

$$\gamma = 90^{\circ}$$

16. If a plane has X-intercept I, Y-intercept m and Zintercept n, and perpendicular distance of plane from origin is k, then

(A) 
$$\frac{1}{I^2} + \frac{1}{m^2} + \frac{1}{n^2} = \frac{1}{k^2}$$
 (B)  $I^2 + m^2 + n^2 = k^2$ 

(B) 
$$I^2 + m^2 + n^2 = k^2$$

(C) 
$$l^2 + m^2 + n^2 = \frac{1}{k^2}$$

(C) 
$$I^2 + m^2 + n^2 = \frac{1}{k^2}$$
 (D)  $\frac{1}{I^2} + \frac{1}{m^2} + \frac{1}{n^2} = k^2$ 

Answer (A)

**Sol.** 
$$\frac{x}{1} + \frac{y}{m} + \frac{z}{n} = 1$$

As distance from origin is k,

$$\Rightarrow \frac{1}{\sqrt{\frac{1}{l^2} + \frac{1}{m^2} + \frac{1}{l^2}}} = k$$

$$\implies \frac{1}{l^2} + \frac{1}{m^2} + \frac{1}{n^2} = \frac{1}{k^2}$$

17. Lines  $\vec{r} = (3+t)\hat{i} + (1-t)\hat{j} + (-2-2t)\hat{k}$ ,  $t \in \mathbb{R}$  and

x = 4 + k, y = -k, z = -4 - 2k,  $k \in \mathbb{R}$ , then relation between lines is

- (A) Coincident
- (B) Parallel
- (C) Skew
- (D) Perpendicular

Answer (A)

**Sol.** 
$$\vec{r} = (3\hat{i} + \hat{j} - 2\hat{k}) + t(\hat{i} - \hat{j} - 2\hat{k})$$

and

$$\frac{x-4}{1} = \frac{y-0}{-1} = \frac{z+4}{-2}$$

As direction ratio is same and (3, 1, -2) point is satisfying other line :. lines are coincident.

18. The equation of plane containing intersecting lines

$$\frac{x+3}{3} = \frac{y}{1} = \frac{z-2}{2}$$
 and  $\frac{x-3}{4} = \frac{y-2}{2} = \frac{z-6}{3}$  is

- (A) 2x-y+z+9=0 (B) x+y-2z+7=0
- (C) x+y+z+5=0 (D) x+2y-2z+9=0

Answer (B)

Sol. Direction ratio normal to the plane is given by

$$=-\hat{i}-\hat{j}+2\hat{k}$$

and plane is passing through (-3, 0, 2)

$$\Rightarrow$$
 -1(x+3)-1(y-0)+2(z-2)=0

$$\Rightarrow$$
  $-x-3-y+2z-4=0$ 

$$\Rightarrow$$
  $x + y - 2z + 7 = 0$ 

- 19. The number of binary operations on the set {1,2,3}
  - (A) 93

- (B) 27
- (C) 39

(D) 3!

Answer (C)

**Sol.** Number of binary operations =  $n^{n^2}$ 

$$\Rightarrow$$
 3 $^9$ 

- 20. Function  $f: N \to Z$ ;  $f(n) = \begin{cases} \frac{n}{2}, & n-\text{even} \\ -\left(\frac{n-1}{2}\right), & n-\text{odd} \end{cases}$ 
  - (A) One-one but not onto
  - (B) One-one and onto
  - (C) Not one-one but onto
  - (D) Not one-one and not onto

Answer (B)

Sol. 
$$f(n) = \begin{cases} \frac{n}{2}; & n-even \\ -\left(\frac{n-1}{2}\right); & n-odd \end{cases}$$

when n = 2, 4, 6, 8,...

$$f(n) = \{1,2,3....\}$$

when n = 1,3,5...

$$f(n) = \{0, -1, -2, -3...\}$$

Function is one-one and onto

- 21. The relation  $S = \{(3,3),(4,4)\}$  on the set  $A = \{3,4,5\}$  is
  - (A) Reflexive only
  - (B) Symmetric only
  - (C) Not reflexive but symmetric and transitive
  - (D) An equivalence relation

**Sol.** 
$$S = \{(3,3)(4,4)\}$$

As (5,5) is not present, therefor it is not reflexive But it is symmetric and transitive

22. 
$$\cot^{-1}\left(\frac{\sqrt{1+x^2}-1}{x}\right) =$$

- (A)  $\cot^{-1} x$  (B)  $\frac{\pi}{2} \frac{1}{2} \tan^{-1} x$
- (C)  $-\frac{1}{2} \tan^{-1} x$
- (D)  $\frac{\pi}{2} \frac{1}{2} \cot^{-1} x$

# Answer (B)

**Sol.** 
$$\cot^{-1} \left( \frac{\sqrt{1+x^2}-1}{x} \right)$$

put 
$$(x = \tan \theta)$$

$$\cot^{-1}\left(\frac{\sec\theta-1}{\tan\theta}\right)$$

$$= \cot^{-1} \left( \tan \frac{\theta}{2} \right)$$

$$= \cot^{-1} \left( \cot \left( \frac{\pi}{2} - \frac{\theta}{2} \right) \right)$$

$$=\frac{\pi}{2}-\frac{\theta}{2}$$

$$=\frac{\pi}{2}-\frac{1}{2}\tan^{-1}x$$

- 23. If  $\cos(2\tan^{-1}x) = \frac{1}{2}$ , then value of x is
  - (A) ±√3
- (B)  $\pm \frac{1}{\sqrt{3}}$
- (C)  $\sqrt{3}-1$
- (D)  $1 \frac{1}{\sqrt{3}}$

# Answer (B)

**Sol.** 
$$\cos(2\tan^{-1}x) = \frac{1}{2}$$

$$2\tan^{-1}x = \pm \frac{\pi}{3}$$

$$\Rightarrow$$
  $tan^{-1}x = \pm \frac{\pi}{6}$ 

$$\Rightarrow$$
  $x = \pm \frac{1}{\sqrt{3}}$ 

24. 
$$\sin^{-1}(\cos(\sin^{-1}x)) + \cos^{-1}(\sin(\cos^{-1}x)) =$$

(A)  $\frac{\pi}{4}$ 

(B) 0

(D)  $-\frac{\pi}{2}$ 

#### Answer (C)

**Sol.** 
$$\sin^{-1}(\cos(\sin^{-1}x)) + \cos^{-1}(\sin(\cos^{-1}x))$$

$$= \sin^{-1} \left( \cos \left( \frac{\pi}{2} - \cos^{-1} x \right) \right) + \cos^{-1} \left( \sin \left( \cos^{-1} x \right) \right)$$

$$= \sin^{-1} \left( \sin(\cos^{-1} x) \right) + \cos^{-1} \left( \sin(\cos^{-1} x) \right)$$

$$=\frac{\pi}{2} \qquad \left( \because \sin^{-1} x + \cos^{-1} x = \frac{\pi}{2} \right)$$

25. If 
$$x^4 + y^4 + z^4 = 0$$
 then  $\begin{vmatrix} 1 & xy & yz \\ zx & 1 & xy \\ yz & zx & 1 \end{vmatrix} = \dots$ 

(where  $x, y, z \in R$ )

- (A) x+y+z+3
- (B) xyz+2

(C) 1

(D) 0

**Sol.** As 
$$x^4 + y^4 + z^4 = 0$$
  
  $x = y = z = 0$ 

$$\Rightarrow \begin{vmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{vmatrix} = 1$$

- (A) 2(10!·11!·12!) (B) 2(10!·13!)
- (C)  $-2(10! \cdot 11! \cdot 12!)$  (D)  $2(10! \cdot 12! \cdot 13!)$

# Answer (A)

$$c_{\scriptscriptstyle 2} \rightarrow c_{\scriptscriptstyle 2} - c_{\scriptscriptstyle 1}$$
 and  $c_{\scriptscriptstyle 3} \rightarrow c_{\scriptscriptstyle 3} - c_{\scriptscriptstyle 1}$ 

# 2(10!11!12!)

# 27. If s = p + q + r, then value of

- (A) 2s<sup>3</sup> (B) 2s<sup>2</sup> (C) e<sup>3</sup> (D) 3e<sup>3</sup>
- (C) s3
- (D) 3s3

# Answer (A)

Sol. 
$$C_1 \rightarrow C_1 + C_2 + C_3$$

$$\begin{array}{l} R_3 \rightarrow R_3 - R_1 \\ R_2 \rightarrow R_2 - R_1 \end{array}$$

$$\begin{vmatrix} 2s & p & q \\ 0 & s & 0 \\ 0 & 0 & s \end{vmatrix} = 2s^3$$

28. If 
$$A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$$
 and  $B =$ \_\_\_\_\_ then  $AB =$ 

BA, where B≠I

(B) 
$$\begin{bmatrix} x & x \\ y & 0 \end{bmatrix}$$

(C) 
$$\begin{bmatrix} x & y \\ 0 & y \end{bmatrix}$$
 (D)  $\begin{bmatrix} x & 0 \\ y & y \end{bmatrix}$ 

(D) 
$$\begin{bmatrix} x & 0 \\ y & y \end{bmatrix}$$

# Answer (A)

**Sol.** As AB = BA, and 
$$A = \begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix}$$

$$\therefore \text{ By option } B = \begin{bmatrix} x & y \\ 0 & x \end{bmatrix}$$

29. If 
$$A = \begin{bmatrix} 3 & 3 & 3 \\ 3 & 3 & 3 \\ 3 & 3 & 3 \end{bmatrix}$$
, then  $A^3 = \begin{bmatrix} 3 & 3 & 3 \\ 3 & 3 & 3 \end{bmatrix}$ 

- (A) 81 A
- (B) 27 A
- (C) 243 A
- (D) 729 A

# Answer (A)

Sol. 
$$A = \begin{bmatrix} 3 & 3 & 3 \\ 3 & 3 & 3 \\ 3 & 3 & 3 \end{bmatrix}$$

$$A^3 = \begin{bmatrix} 243 & 243 & 243 \\ 243 & 243 & 243 \\ 243 & 243 & 243 \end{bmatrix}$$

$$A^3 = 81A$$

30. 
$$\frac{d}{dx}log_{|x|}e = \dots$$

(A) 
$$\frac{1}{(\log x)^2}$$
 (B)  $\frac{1}{|x|}$ 

(B) 
$$\frac{1}{|x|}$$

(C) 
$$-\frac{1}{x(\log |x|)^2}$$
 (D)  $e^x$ 

# Answer (C)

Sol. 
$$\frac{d}{dx} \log_{|x|} e$$

$$= \frac{d}{dx} (\log_e |x|)^{-1}$$

$$= -\frac{1}{x(\log|x|)^2}$$

31. 
$$\frac{d}{dx} \tan^{-1} \left( \frac{1-x}{1+x} \right) =$$

(A) 
$$\frac{-1}{1+x^2}$$

(B) 
$$\frac{1}{1+x^2}$$

(C) 
$$\frac{2}{1+x^2}$$

(D) 
$$\frac{-2}{1+x^2}$$

Answer (A)

$$\textbf{Sol. } \frac{d}{dx} \Bigg( tan^{-1} \Bigg( \frac{1-x}{1+x} \Bigg) \Bigg)$$

$$= -\frac{1}{1+x^2}$$

32. If 
$$x = at^2$$
,  $y = 2at$ , then  $\frac{d^2x}{dy^2} = ....$ 

(B) 
$$\frac{-1}{t^2}$$

(C) 
$$\frac{-1}{2at^3}$$

(D) 
$$\frac{1}{2a}$$

Answer (D)

Sol. 
$$x = at^2$$
,  $y = 2at$ 

$$\frac{dx}{dy} = t$$

$$\Rightarrow \frac{d^2x}{dy^2} = \frac{d}{dt}(t) \times \frac{dt}{dy}$$

$$=1\times\frac{dt}{dy}=\frac{1}{2a}$$

33. 
$$\int x e^{x^2 \log 2} \cdot e^{x^2} dx = \underline{\hspace{1cm}} + c$$

(A) 
$$\frac{2^{x^2} \cdot e^{x^2}}{1 + \log 2}$$

(B) 
$$\frac{e^{x^2 \log 2} \cdot e^{x^2}}{\log 2}$$

(C) 
$$\frac{2^{x^2} \cdot e^{x^2}}{2(1 + \log 2)}$$
 (D)  $\frac{(2e)^{x^2}}{\log(2e)}$ 

(D) 
$$\frac{(2e)^{x^2}}{\log(2e)}$$

Answer (C)

Sol. 
$$\int x \cdot e^{x^2 \log 2} \cdot e^{x^2} dx$$

$$\int x \cdot 2^{x^2} \cdot e^{x^2} dx$$

$$\int x \cdot (2e)^{x^2} dx$$

$$x^2 = t$$

$$xdx = \frac{dt}{2}$$

$$\frac{1}{2}\int (2e)^t dt$$

$$\frac{1}{2}\frac{\left(2e\right)^{t}}{\log 2e} + c$$

$$\frac{2^{x^2} \cdot e^{x^2}}{2(\log 2 + 1)} + c$$

34. 
$$\int \left(\frac{1}{x-3} - \frac{1}{x^2 - 3x}\right) dx = \dots + c; x > 3$$

(A) 
$$\frac{1}{3}\log(\sqrt{x}(x-3))$$
 (B)  $\frac{2}{3}\log(\sqrt{x}(x-3))$ 

(B) 
$$\frac{2}{3}\log(\sqrt{x}(x-3))$$

(C) 
$$\frac{2}{3}\log(x(x-3))$$
 (D)  $\frac{1}{3}\log(x(x-3))$ 

(D) 
$$\frac{1}{3}\log(x(x-3))$$

Answer (B)

Sol. 
$$\int \left(\frac{1}{x-3} - \frac{1}{x^2 3x}\right) dx$$

$$\frac{2}{3}\int \frac{1}{x-3} dx + \frac{1}{3}\int \frac{1}{x} dx$$

$$\frac{2}{3}\ln(x-3) + \frac{1}{3}\ln x + c$$

$$\frac{2}{3}\ln\left(\sqrt{x}(x-3)\right)+c$$

35. What is the mean of f(x) = 3x + 2 where x is a random variable with probability distribution

X=x	1	2	3	4
P(X=x)	1/6	1/3	1/3	1/6

(A) 
$$\frac{15}{2}$$

(B) 
$$\frac{5}{3}$$

(C) 
$$\frac{5}{2}$$

(D) 
$$\frac{19}{2}$$

# Answer (D)

- **Sol.** Mean  $(\overline{x}) = \sum x_i p(x_i)$ 
  - $=\frac{1}{6}+\frac{2}{3}+1+\frac{2}{3}$   $=\frac{5}{2}$
  - $\therefore$  Mean of  $f(x) = 3\left(\frac{5}{2}\right) + 2$
  - $=\frac{19}{2}$
- 36. The probability that an event A occurs in a single trial of an experiment is 0.3. Six independent trials of the experiment are performed. What is the variance of probability distribution of occurrence of event A?
  - (A) 0.18
- (B) 1.26
- (C) 12.6
- (D) 1.8

# Answer (B)

- **Sol.** Variance = npq =  $6 \times 0.3 \times 0.7 = 1.26$
- 37. The probability that A speaks truth is  $\frac{4}{5}$ , while this probability fo B  $\frac{3}{5}$ . The probability of at least one of them is true when asked to speak on an event is .......
  - (A)  $\frac{2}{25}$
- (B)  $\frac{23}{25}$
- (C)  $\frac{3}{25}$
- (D)  $\frac{4}{25}$

# Answer (B)

- **Sol.**  $P(A) = \frac{4}{5}$ ;  $P(\overline{A}) = \frac{1}{5}$ 
  - $P(B) = \frac{3}{5}; \qquad P(\overline{B}) = \frac{2}{5}$

required probability =  $\frac{4}{5} \times \frac{2}{5} + \frac{3}{5} \times \frac{1}{5} + \frac{4}{5} \times \frac{3}{5}$ 

$$=\frac{23}{25}$$

- 38. The comer points of the feasible region determined by the system of linear constraints are (0,10), (5,5), (15,15), (0,20). Let Z = px + qy where p, q > 0. Condition on p and q so that the maximum of z occurs at both the points (15,15) and (0,20) is
  - (A) p = 2q
- (B) p = q
- (C) q = 2p
- (D) q = 3p

# Answer (D)

**Sol.** 
$$15p + 15q = 20q$$

$$3p = q$$

- 39. What is the approximate value of \$\sqrt{242,999}\$?
  - (A)  $\frac{1115}{405}$
- (B)  $\frac{121499}{40500}$
- (C)  $\frac{1214999}{405000}$
- (D)  $\frac{1214999}{4050}$

# Answer (C)

Sol. 
$$\Delta x = -\frac{1}{5x^{4/5}} \times .001$$

Here 
$$x = 243$$

$$\therefore \Delta x = -\frac{1}{405000}$$

Approximate value = 
$$\frac{1214999}{405000}$$

- The length of subtangent at any point of the curve log y = 25x is
  - (A) Proportional to y
  - (B) Proportional to x
  - (C) Zero
  - (D) Constant

# Answer (D)

**Sol.** Length of subtangent =  $y_1 \cot \theta$ 

$$= y \times \frac{1}{25y} = \frac{1}{25}$$

.: constant

# Time: 1 hrs. Answers & Solutions



# GUJCET-2018

(Biology)

#### Important Instructions:

- 1. The Biology test consists of 40 questions. Each question carries 1 mark. For each correct response, teh candidate will get 1 mark. For each incorrect response, mark will be deducted. The maximum marks are 40.
- 2. This Test is of 1 hour duration
- 3. Use Black Ball Point Pen only for writing particulars on OMR Answer Sheet and marking answers by darketing the circle ".
- 4. Rough work is to be done on the space provided for this purpose in the Test Booklet only.
- 5. On completion of the test, the candidate must handover the Answer Sheet to the Invigilator in the Room / Hall. The candidates are allowed to take away this Test Booklet with them.
- 6. The Set No. for this Booklet is . Mark sure that the Set No. printed on the Answer sheet is the same as that on this booklet. In case of discrepancy, the candidate should immediately report teh matter to the Invigilator for replacement of both the Test Booklet and the Answer Sheet.
- 7. The candidate should ensure that the Answer Sheet is not folded. Do not make any stray marks on the Answer Sheet.
- 8. Do not write your Seat No. anywhere else, except in the specified space in the Test Booklet/Answer Sheet.
- 9. Use of White fluid for correction is not permissible on the Answer sheet.
- 10. Each candidate must show on demand his / her Admission Card to the Invigilator.
- 11. No candidate, without special permission of the Superintendent or Invigilator, should leave his/her seat.
- 12. Use of Manual Calculator is permissible.
- 13. The candidate Should not leave the Examination Hall handling over their Answer Sheet to the Invigilator on duty and must sign the Attendance Sheet (Patrak-01). Cases where a candidate has not signed the Attedance Sheet (Patrak-01) will be deemed not to have handed over the Answer Sheet and Will be dealt with as an unfair means case.
- 14. The candidates are governed by all Rules and Regulations of the Board with regard to their conduct in the Examination hall. All cases of unfair means will be dealt with as per Rules and Regulations of the Board.
- 15. No Part of the Test Booklet and Answer Sheet shall be detached under any circumstances.
- 16. The candiates will write the Correct Test Booklet Set No. as given in the Test Booklet / Answer Sheet in the Attendance Sheet. (Patrak 01).



M.M.: 40

# PART-A: BIOLOGY

- When the MTP act came into force in India?
  - (A) 1973
- (B) 1972
- (C) 1971
- (D) 1970

# Answer (B)

- Why transgenic mice are being developed?
  - (A) To stop the harmful activities in house
  - (B) For the use in Agriculture
  - (C) Testing the safety of vaccines
  - (D) In the form of bioinsecticide

# Answer (C)

- For DNA fingerprinting, short repetitive nucleotide sequences are known as?
  - (A) VNTR
- (B) DNA probes
- (C) Introns
- (D) DNA primers

## Answer (A)

- In operon the segments of DNA which carry codes for the synthesis of proteins are known as
  - (A) structural gene
- (B) Regulator gene
- (C) Repressor gene
- (D) Promoter gene

#### Answer (A)

- The amp<sup>R</sup> gene has recognition site.
  - (A) Pst-I
- (B) Pvu-II
- (C) Hind-III
- (D) Bam H-I

#### Answer (A)

- In Africa, two distinct types of Rhinoceros are found. One is grazing which lives in open land and second is a browsing type which lives in wooded areas. It is which type of adaptive radiation?
  - (A) Local adaptive branching
  - (B) Contemporaneous radiation
  - (C) Continental adaptive radiation
  - (D) Wide adaptive branching

#### Answer (A)

- Which gland is associated with regulation of body rhythm and in maintaining sleep-wake cycle?
  - (A) Pituitary gland
- (B) Parathyroid gland
- (C) Pineal gland
- (D) Adrenal gland

# Answer (C)

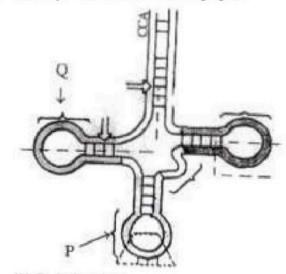
- Which part of the brain receives impulses from eyes and muscles of head?
  - (A) Superior colliculi
- (B) Inferior colliculi
- (C) Pineal body
- (D) All of them

## Answer (A)

- under normal conditions the wall of RBC acts as permeable membrane to which ions?
  - (A) Na+, K+
- (B) Na+, HCO<sub>2</sub>-
- (C) Cl-, HCO<sub>3</sub>- (D) K+, Cl-

#### Answer (C)

10. Indentify P and Q in the following figure?



- (A) P- Anticondon;
  - Q D Loop
- (B) P D Loop;
  - Q-T \u00fc C Loop
- (C) P Anticondon Loop;
  - Q D Loop
- (D) P Site of amino acid attachment
  - Q-TWCLoop

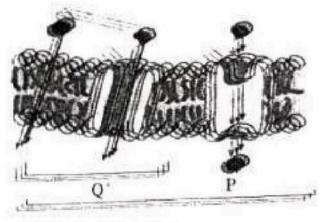
#### Answer (C)

- 11. How much water is absorbed in 15 hours by a mustard plant having 2 kg wt.
  - (A) 2 Kg
  - (B) 6 Kg
  - (C) 4 Kg
  - (D) 12 Kg

Answer (B)



12. Identify P and Q in the given diagram



- (A) P = Facilitated diffusion
  - Q = Simple diffusion
- (B) P = Facilitated diffusion
  - Q = Active transport
- (C) P = Simple diffusion
  - Q = Passive transport
- (D) P = Simple diffusion
  - Q = Active transport

# Answer (A)

- 13. What happens when gall bladder is removed in humans?
  - (A) Lipid metabolism decreases
  - (B) Jaundice
  - (C) Protein metabolism decreases
  - (D) Carbohydrate metabolism decreases

#### Answer (A)

14. Match the following and choose the correct option.

Column I		Column II		
P) SA node	i)	lower left corner of the right atrium		
Q) Purkinje fibres	ii)	from the AV node, a tract of conducting fiber		
R) AV node	iii)	right upper corner of the right atrium		
S) Bundle of His	iv)	branches that emerge from the bundle of His		

- (A) (P iii) (Q i) (R iv) (S ii)
- (B) (P iii) (Q iv) (R i) (S ii)
- (C) (P iii) (Q iv) (R ii) (S i)
- (D) (P iv) (Q ii) (R iii) (S i)

## Answer (B)

- 15. The diversity which is richness of different species in a range of habitats within a geological area in known
  - (A) α diversity
- (B) delta diversity
- (C) ecosystem diversity (D) γ(gamma) diversity

## Answer (D)

- 16. "India is a country of youngesters" on this basis, if age pyramid is made. What type of pyramid it will be?
  - (A) Triangular shape
- (B) Bell shape
- (C) Urn shape
- (D) Spindle shape

## Answer (A)

- 17. In the filtrate and plsama get isotonic.
  - (A) Distal convoluted tubule
  - (B) Descending limb of the loop of Henle
  - (C) Proximal convoluted tubule
  - (D) Ascending limb of the loop of Henle

#### Answer (C)

- 18. How the urea enter in descending capillaries?
  - (A) Diffusion
  - (B) Active transport
  - (C) Osmosis
    - (D) Diffusion and Osmosis

#### Answer (A)

- 19. Which company is providing CNG in Surat?
  - (A) GAIL
- (B) ADANI
- (C) GGCL
- (D) RELIANCE

#### Answer (C)

- 20. In which stage in the process of decomposition Bacteria and Fungi become active?
  - (A) Fragmentation
  - (B) Accumulation
  - (C) Leaching
  - (D) Catabolism

#### Answer (D)

21. Statement A: All the locomotions are movements.

Statement B: All the movements are not locomotions

- (A) Statement A and B both are correct
- (B) Statement A is true but B is false
- (C) Statement A and B both are false
- (D) Statement A is false but B is false

#### Answer (A)



- 22. The vertebral formula of human is
  - (A) T<sub>12</sub>, C<sub>7</sub>, L<sub>5</sub>, S<sub>8</sub>
- (B) C<sub>7</sub>, T<sub>12</sub>, L<sub>5</sub>, S<sub>5</sub>
- (C) C<sub>7</sub>, L<sub>8</sub>, T<sub>12</sub>, S<sub>5</sub> (D) C<sub>7</sub>, S<sub>5</sub>, T<sub>22</sub>, L<sub>5</sub>

# Answer (B)

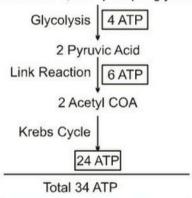
- 23. How is green house gas raise the temperature of Farth?
  - (A) It absorbs the long wave length infrared rays and reflect them back towards the earth
  - (B) It absorbs sunrays and decreases the temperature of earth
  - (C) It absorbs sun rays and increases the temperature of earth
  - (D) It absorb shorter wave length of infrared wave

# Answer (A)

- 24. How many ATP are synthesized in Eukaryotic cell during aerobic repiration of 1, 3 biphosphoglyceric acid?
  - (A) 34 ATP
- (B) 80 ATP
- (C) 38 ATP
- (D) 68 ATP

# Answer (A)

Sol. 2 molecules of 1, 3 bisphosphoglyceric acid



Note: Number of 1, 3 bisphosphoglyceric acid is not given in paper. So glucose is taken as reference

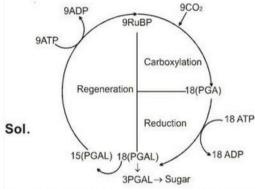
- 25. If Respiratory substrate like sucrose dipeptide protein and lipid are present in living cell, which substrate is utilised first?
  - (A) Sucrose
- (B) Lipid
- (C) Protein
- (D) Dipeptide

#### Answer (A)

- **Sol.** Carbohydrate is most preferred respiratory substrate.
- 26. In the presence of bright sunlight small bubbles are formed around the green parts of the plant'. Who showed this?
  - (A) Joseph Priestley
- (B) Robert Hill
- (C) Jan Ingenhousz
- (D) Julius Von Sachs
- Answer (C)

- 27. If 18 PGAL are formed during dark reaction, how many Calvin cycles and ATPs are required respectively?
  - (A) 9 Calvin cycle, 24 ATP
  - (B) 6 Calvin cycle, 18 ATP
  - (C) 9 Calvin cycle, 27 ATP
  - (D) 6 Calvin cycle, 36 ATP

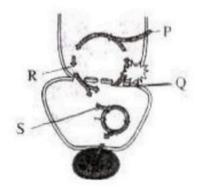
# Answer (C)



- 28. What is the time for P wave in ECG?
  - (A) 0.10 sec.
- (B) 040 sec.
- (C) 0.30 sec.
- (D) 0.80 sec

# Answer (A)

29. At which site CO2 enters in the given diagram labelled with P,Q, R, S? Choose the correct option.



- (A) P, S
- (B) R, S
- (C) P. R
- (D) Q. S

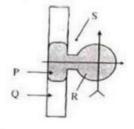
#### Answer (A)

- 30. Identify the part which is made up of peripheral membrane protein complex in the given figure?
  - (A) P
  - (B) R
  - (C) Q
  - (D) S

# Answer (B)

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Sol. Peripheral is Extrinsic protein.



- 31. Which is correct for VC?
  - (A) IC + ERV
  - (B) TV + ERV
  - (C) RV + IRV + ERV
  - (D) VC + RV + TV

# Answer (A)

- 32. Morphologically and Physiologically similar and usually motile and flagellated gametes are known as \_\_\_\_ and its correct example?
  - (A) Isogamete, Fucus
  - (B) Isogamete, Cladophora
  - (C) Anisogamete, Spirogyra
  - (D) Anisogamete, Human gametes

#### Answer (B)

- 33. Which hormone stimulates the development and differentiation of T-lymphocytes?
  - (A) Parathormone
  - (B) Thyrocalcitonin
  - (C) Thyroxine
  - (D) Thymosin

## Answer (D)

- 34. Where the pollengrains are develop in anther during microsporogenesis?
  - (A) Epidermis
  - (B) Sporogenous tissue
  - (C) Endothecium
  - (D) Tapetum

#### Answer (B)

35. Statement A: Due to sudden influx of a large amount of Na+ towards inside, the plasma membrane becomes positively charged on its inner side

Statement R: It is said to be depolarized

- (A) A and R both are true
- (B) A is true, R is false
- (C) A and R both are false
- (D) A is false, R is true

#### Answer (A)

- 36. America obtained a patent for germplam of Indian Basmati rice. This process is known by which name?
  - (A) Biopatent
- (B) Bioinsecticide
- (C) Biowar
- (D) Biopiracy

# Answer (D)

- 37. By Which process uncertainty of flowering due to photoperiodism can be avoided?
  - (A) Phototropism
  - (B) Senescence
  - (C) Vernalization
  - (D) Abscissin

# Answer (C)

- 38. Klinefelter's syndrome
  - (A) Trisomy of autosomes
  - (B) Monosomy of autosome
  - (C) Trisomy of sex chromosomes
  - (D) Monosomy of sex chromosome

#### Answer (C)

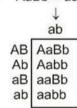
Sol. Klinefelter's syndrome -2A+ XXY

Trisomy is 2n + 1

- 39. What is the ratio for test cross in dihybrid experiment of Mendel?
  - (A) 9:3:3:1
  - (B) 1:1:1:1
    - (C) 7:1:1:7
    - (D) 11:1:1:3

## Answer (B)

Sol. AaBb × aabb Test cross



Ratio = 1:1:1:1

- 40. Which one forms axial filament of the human sperm?
  - (A) Mitochondria
  - (B) Proximal centriole
  - (C) Distal centriole
  - (D) Golgi body

# Answer (C)

