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COMEDK 2018 Question Paper with Solution

Consortium of Medical, Engineering and Dental Colleges of Karnataka
Under Graduate Entrance Test

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SOLVED PAPER – 2018 (COMEDK)

Instructions

. There are 180 questions in all. The number of questions in each section is as given below.

Sections No. of Questions Section I: Physics 1-60

61-120 Section II: Chemistry Section III: Mathematics 121-180

- · All the questions are Multiple Choice Questions having four options out of which ONLY ONE is correct.
- . Candidates will be awarded 1 mark for each correct answer. There will be no negative marking for incorrect answer.
- Time allotted to complete this paper is 3 hrs.

PHYSICS

1. A ray of light enters from a rarer to a denser medium. The angle of incidence is i. Then, the reflected and refracted rays are mutually perpendicular to each other. The critical angle for the pair of media is

$$a \cdot \sin^{-1}(\tan i)$$

b.
$$\tan^{-1}(\sin i)$$

$$c. \sin^{-1}(\cot i)$$

$$d \cdot \cos^{-1}(\tan i)$$

A fish in water (refractive index n) looks at a bird vertically above in the air. If y is the height of the bird and x is the depth of the fish from the surface, then the distance of the bird as estimated by the fish is

$$a. x + y \left(1 - \frac{1}{n}\right)$$

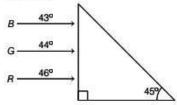
$$b. x + ny$$

$$c. x + y \left(1 + \frac{1}{n}\right)$$

$$c. x + y \left(1 + \frac{1}{n}\right)$$

$$d. y + x \left(1 - \frac{1}{n}\right)$$

3. Figure shows a mixture of blue, green and red coloured rays incident normally on a right angled prism. The critical angles of the material of the prism for red, green and blue are 46°, 44° and 43°, respectively. The arrangement will separate



- a. red colour from blue and green
- b. blue colour from red and green
- c. green colour from red and blue
- d. All the three colours
- 4. A convex and a concave lens separated by distance d are then put in contact. The focal length of the combination
 - a. decreases
- b. increases
- c. becomes zero
- d. remains the same

5. A convex lens is made of 3 layers of glass of 3 different materials as in the figure. A point object is placed on its axis. The number of images of the object are



- a. 1 c. 3
- b. 2 d. 4
- If μ₀ is permeability of free space and ε₀ is permittivity of free space, then the speed of light in vacuum is given by
- b. $\sqrt{\mu_0/\epsilon_0}$

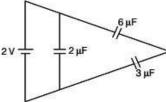
- 7. In Young's double slit experiment, a third slit is made in between the double slits. Then,
 - a. intensity of fringes totally disappears
 - b. only bright light is observed on the screen
 - c. fringes of unequal width are formed
 - d. contrast between bright and dark fringes is
- 8. The maximum number of possible interference maxima when slit separation is equal to 4 times the wavelength of light used in a double slit experiment is
 - a. ∞
- **b.** 9
- c. 8
- d. 4
- 9. In a Fraunhofer diffraction experiment at a single slit using a light of wavelength 400 nm, the first minimum is formed at an angle of 30°. The direction θ of the first secondary maximum is given by
 - a. sin-1(2/3)
- $b. \sin^{-1}(3/4)$
- $c. \sin^{-1}(1/4)$
- $d. \tan^{-1}(2/3)$
- 10. Maximum diffraction takes place in a given slit
 - a. y-rays
- b. ultraviolet light
- c. infrared light
- d. radio waves
- 11. An unpolarised beam of intensity Io falls on a polaroid. The intensity of the emergent light is
 - a. Io/2
- $b. I_0$
- c. In / 4
- d. Zero
- 12. Which of the following is a dichroic crystal?
 - a. Quartz
- b. Tourmaline
- c. Mica
- d. Selenite

13. Two identical metal spheres charged with + 12 µF and -8 µF are kept at certain distance in air. They are brought into contact and then kept

at the same distance. The ratio of the magnitudes of electrostatic forces between them before and after contact is

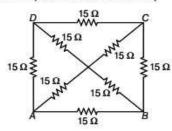
- a. 12:1
- b. 8:1
- c. 24:1
- d. 4:1
- 14. A small conducting sphere of radius r is lying concentrically inside a bigger hollow conducting sphere of radius R. The bigger and smaller spheres are charged with Q and q(Q > q)and are insulated from each other. The potential difference between the spheres will be

- $b. \frac{1}{4\pi\varepsilon_0} \left(\frac{q}{R} \frac{Q}{r} \right)$ $d. \frac{1}{4\pi\varepsilon_0} \left(\frac{Q}{R} + \frac{q}{r} \right)$
- **15.** The charges Q, +q and +q are placed at the vertices of an equilateral triangle of side l. If the net electrostatic potential energy of the system is zero, then Q is equal to
 - a q/2
- b q
- c. + q/2
- d. Zero
- 16. How many 6µF, 200 V condensers are needed to make a condenser of 18 µF, 600 V?
 - a. 9
- b. 18
- c. 3
- d. 27
- 17. The total energy stored in the condenser system shown in the figure will be

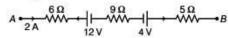


- a. 2µJ
- b. 4 μJ
- c. 8µJ
- d. 16 µJ
- 18. A metal wire is subjected to a constant potential difference. When the temperature of the metal wire increases, the drift velocity of the electron
 - a. increases, thermal velocity of the electron decreases
 - b. decreases, thermal velocity of the electron
 - c. increases, thermal velocity of the electron increases
 - decreases, thermal velocity of the electron increases

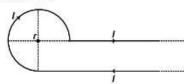
19. The equivalent resistance between the points A and B will be (each resistance is 15Ω)



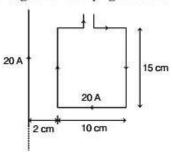
- a. 30 Ω c. 10 Ω
- b. 8 Ω d. 40 Ω
- 20. The terminals of a 18 V battery with an internal resistance of 1.5 Ω are connected to a circular wire of resistance 24Ω at two points distant at one quarter of the circumference of a circular wire. The current through the bigger arc of the
 - circle will be a. 0.75 A
- b. 1.5 A
- c. 2.25 A
- d. 3 A
- 21. The potential difference between A and B in the following figure is



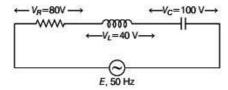
- a. 32 V
- b. 48 V
- c. 24 V
- d. 14 V
- 22. The magnetic field at the centre of a circular current carrying conductor of radius r is B_c . The magnetic field on its axis at a distance r from the centre is B_a . The value of $B_c: B_a$ will be
 - a. 1: $\sqrt{2}$
- c. $2\sqrt{2}:1$
- d. $\sqrt{2}:1$
- 23. Current I is flowing in a conductor shaped as shown in the figure. The radius of the curved part is r and the length of straight portion is very large. The value of the magnetic field at the centre O will be



- 24. Two tangent galvanometers A and B are identical except in their number of turns. They are connected in series. On passing a current through them, deflections of 60° and 30° are produced. The ratio of the number of turns in A and B is
 - a. 1:3
- b. 3:1
- c. 1:2
- d. 2:1
- 25. The resultant force on the current loop PQRS due to a long current carrying conductor will be



- a. 10-4 N
- **b.** $3.6 \times 10^{-4} \,\mathrm{N}$
- c. 1.8 × 10⁻⁴ N
- $d.5 \times 10^{-4} \text{ N}$
- 26. A certain current on passing through a galvanometer produces a deflection of 100 divisions. When a shunt of one ohm is connected, then the deflection reduces to 1 division. The galvanometer resistance is b. 99 Ω
 - a. 100 Ω
- c. 10 Ω
- 27. Two similar circular loops carry equal currents in the same direction. On moving the coils further apart, the electric current will
 - a. increase in both
 - b. decrease in both
 - c. remain unaltered
 - d. increases in one and decreases in the second
- 28. The value of alternating emf E in the given circuit will be



- a. 220 V
- b. 140 V
- c. 100 V
- d. 20 V

29. A current of 5 A is flowing at 220 V in the primary coil of a transformer. If the voltage produced in the secondary coil is 2200 V and 50% of power is lost, then the current in the secondary will be

a. 2.5 A

b. 5 A

c. 0.25 A

d. 0.5 A

- **30.** For a series *L-C-R* circuit at resonance, the statement which is not true?
 - Peak energy stored by a capacitor = peak energy stored by an inductor
 - b. Average power = Apparent power
 - c. Wattless current is zero.
 - d. Power factor is zero.
- 31. Solar spectrum is an example for
 - a. line emission spectrum
 - b. continuous emission spectrum
 - c. band absorption spectrum
 - d. line absorption spectrum
- 32. When a piece of metal is illuminated by a monochromatic light of wavelength λ, then stopping potential is 3V-s. When same surface is illuminated by light of wavelength 2λ, then stopping potential becomes V_s. The value of threshold wavelength for photoelectric emission will be

a. 4 \lambda

b. 8 λ

c. 4/3 \

d. 6 \lambda

 The maximum kinetic energy of emitted electrons in a photoelectric effect does not depend upon

a. wavelength

b. frequency

c. intensity

d. work-function

34. The ratio of minimum wavelength of Lyman and Balmer series will be

a. 1.25

b. 0.25

c. 5

d. 10

- 35. Hydrogen atom does not emit X-rays because
 - a. it contains only a single electron
 - b. energy levels in it are far apart
 - c. its size is very small
 - d. energy levels in it are very close to each other
- 36. If an electron and a proton have the same de-Broglie wavelength, then the kinetic energy of the electron is
 - a. Zero
 - b. less than that of a proton
 - c. more than that of a proton
 - d. equal to that of a proton

37. Two protons are kept at a separation of 40 Å. F_n is the nuclear force and F_e is the electrostatic force between them. Then,

 $a. F_n >> F_e$

 $b. F_n = F_c$

c. $F_n << F_n$

 $d. F_n \simeq F_e$

- 38. Blue colour of sea water is due to
 - a. interference of sunlight reflected from the water surface
 - b. scattering of sunlight by the water molecules
 - c. image of sky in water
 - d. refraction of sunlight
- The ratio of the nuclear radii of elements with mass numbers 216 and 125 is

a. 216:125

b. $\sqrt{216}$: $\sqrt{125}$

c. 6:5

d. None of these

40. On bombarding U²³⁵ by slow neutron, 200 MeV energy is released. If the power output of atomic reactor is 1.6 MW, then the rate of fission will be

 $a.5 \times 10^{22} / s$

 $b.5 \times 10^{16} / s$

c. 8×10¹⁶/s

 $d. 20 \times 10^{16} / s$

41. The masses of two radioactive substances are same and their half-lives are 1 year and 2 years, respectively. The ratio of their activities after 6 years will be

a. 1:4

b. 1:2

c. 1:3

d. 1:6

42. $_{92}$ U 235 undergoes successive disintegrations with the end product of $_{82}$ Pb 203 . The number of α and β particles emitted are

 α . $\alpha = 6, \beta = 4$

 $b. \alpha = 6, \beta = 0$

 $\mathbf{c} \cdot \alpha = 8, \beta = 6$

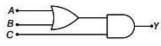
 \mathbf{d} . $\alpha = 3, \beta = 3$

The most stable particle in Baryon group is
 neutron
 omega-particle

a. neutronc. proton

d. lamda-particle

- 44. In an unbiased p-n junction
 - \boldsymbol{a} . potential at p is more than that at n
 - b. potential at p is less than that at n
 - c. potential at p is equal to that at n
 - **d.** potential at p is + ve and that at n is ve
- 45. To get an output Y = 1 from the circuit shown, the inputs A, B and C must be respectively



a. 0, 1, 0

b. 1, 0, 0

c. 1, 0, 1

d. 1, 1, 0

46. Dimensional formula for the universal gravitational constant G is

a. $[M^{-1}L^2T^{-2}]$

b. [M0L0T0]

c. [M-1L3T-2]

- $d. [M^{-1}L^3T^{-1}]$
- 47. A body is projected vertically upwards. The times corresponding to height h, while ascending and descending are t_1 and t_2 , respectively. Then, the velocity of projection is (g is acceleration due to gravity)

 $a. g \sqrt{t_1 t_2}$

c. $\frac{g\sqrt{t_1t_2}}{2}$

- **d.** $\frac{g(t_1+t_2)}{2}$
- 48. A mass of 10 kg is suspended from a spring balance. It is pulled a side by a horizontal string, so that it makes an angle of 60° with the vertical. The new reading of the balance is

a. 20 kg-wt

b. 10 kg-wt

c. 10√3 kg-wt

- d. 20√3 kg-wt
- 49. A body weight 50 g in air and 40 g in water. How much would it weight in a liquid of specific gravity 1.5?

a. 30 g

b. 35 g

- c. 65 g
- d. 45 g
- 50. A body of mass 4 kg is accelerated upon by a constant force, travels a distance of 5 m in the 1st second and a distance of 2 m in the 3rd second. The force acting on the body is

a. 2 N

b. 4 N

- d. 8 N
- 51. A simple pendulum is suspended from the ceiling of a lift. When the lift is at rest its time period is T. With what acceleration should the lift be accelerated upwards in order to reduce its period to T/2?

(g is acceleration due to gravity)

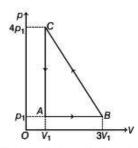
a. 2g

c. 4g

- d. g
- **52.** If γ is the ratio of specific heats and R is the universal gas constant, then the molar specific heat at constant volume C_V is given by

a. yR

- 53. An ideal gas is taken via path ABCA as shown in figure.



The network done in the whole cycle is d. Zero

 $a. 3p_1V_1$

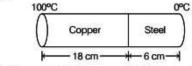
- **b.** $-3p_1V_1$
- $c. 6p_1V_1$
- 54. In which of the processes, does the internal energy of the system remain constant?

a. Adiabatic

b. Isochoric

c. Isobaric

- d. Isothermal
- 55. The coefficient of thermal conductivity of copper is 9 times that of steel. In the composite cylindrical bar shown in the figure, what will be the temperature at the junction of copper and steel?



a. 75°C b. 67°C c. 25°C d. 33°C

- **56.** The equation of a simple harmonic wave is given by $y = 6\sin 2\pi(2t - 0.1x)$, where x and y are in mm and t is in seconds. The phase difference between two particles 2 mm apart at any instant is
 - a. 18° b. 36°
- c. 54°
- d. 72°
- 57. With what velocity should an observer approach a stationary sound source, so that the apparent frequency of sound should appear double the actual frequency? (v is velocity of sound). d. v
 - a. v/2
- b. 30
- c. 20
- 58. If a black body emits 0.5 J of energy per second when it is at 27°C, then the amount of energy emitted by it when it is at 627°C will be

a. 40.5 [

- b. 162 [
- c. 13.5 J
- d. 135 J
- A string vibrates with a frequency of 200 Hz. When its length is doubled and tension is altered, it begins to vibrate with a frequency of 300 Hz. The ratio of the new tension to the original tension is
 - a. 9:1
- b. 1:9
- c. 3:1
- d. 1:3
- 60. How many times more intense is a 60 dB sound than a 30 dB sound?
 - a. 1000
- b. 2
- c. 100
- d. 4

CHEMISTRY

- 61. Which of the following is not an ore of magnesium?
 - a. Carnallite
- b. Dolomite
- c. Calamine
- d. Sea water
- 62. The atomic numbers of Ni and Cu are 28 and 29 respectively. The electron configuration 1s²2s²2p⁶3s²3p⁶3d¹⁰ represents
 - a. Cu+
- b. Cu2+
- c. Ni²⁺
- d. Ni
- 63. In the following, the element with the highest ionisation energy is
 - a. [Ne] 3s2, 3p1
- **b.** [Ne] $3s^2$, $3p^3$
- c. [Ne] 3s2, 3p2
- d. [Ne] 3s2, 3p4
- 64. In the conversion of Br₂ to BrO₃⁻, the oxidation number of Br changes from
 - a. zero to +5
- **b.** +1 to +5
- c. zero to 3
- d. + 2 to + 5
- 65. Among the alkali metals caesium is the most reactive because
 - a. its incomplete shell is nearest to the nucleus
 - b. it has a single electron in the valence shell
 - c. it is the heaviest alkali metal
 - d. the outermost electron is more loosely bound than the outermost electron of the other alkali metals.
- 66. Which of the following represents the Lewis structure of N₂ molecule?
 - $a. \times N = N \times$
- A XX XX
- c. *N N*
- $\mathbf{d}. \overset{\mathsf{x}}{\times} \overset{\mathsf{x}}{\overset{\mathsf{x}}}{\overset{\mathsf{x}}{\overset{\mathsf{x}}{\overset{\mathsf{x}}{\overset{\mathsf{x}}{\overset{\mathsf{x}}}{\overset{\mathsf{x}}{\overset{\mathsf{x}}}{\overset{\mathsf{x}}{\overset{\mathsf{x}}}{\overset{\mathsf{x}}{\overset{\mathsf{x}}}{\overset{\mathsf{x}}}{\overset{\mathsf{x}}}{\overset{\mathsf{x}}}{\overset{\mathsf{x}}}}{\overset{\mathsf{x}}}}{\overset{\mathsf{x}}}}}}}}$
- 67. Hydrogen bond is strongest in
 - a. S—H ---- O
- b. O—H ----S
- c. F—H ---- F
- d. O—H----N
- 68. The decomposition of a certain mass of CaCO₃ gave 11.2 dm³ of CO₂ gas at STP. The mass of KOH required to completely neutralise the gas is
 - a. 56 g
- **b.** 28 g
- c. 42 g
- d. 20 g
- **69.** The density of a gas is $1.964 \,\mathrm{g} \,\mathrm{dm}^{-3}$ at $273 \,\mathrm{K}$ and $76 \,\mathrm{cm}$ Hg. The gas is
 - a. CH₄
- b. C2H6
- c. CO,
- d. Xe

- **70.** 0.06 mole of KNO₃ solid is added to 100 cm³ of water at 298 K. The enthalpy of KNO₃(aq) solution is 35.8 kJ mol⁻¹. After the solute is dissolved the temperature of the solution will be a. 293 K b. 298 K c. 301 K d. 304 K
- 71. 4 moles each of SO₂ and O₂ gases are allowed to react to form SO₃ in a closed vessel. At equilibrium 25 % of O₂ is used up. The total number of moles of all the gases present at equilibrium is
 - a. 6.5
- b. 7.0
- c. 8.0
- d. 2.0
- 72. An example for auto-catalysis is
 - a. oxidation of NO to NO2
 - b. oxidation of SO2 to SO3
 - c. decomposition of KClO3 to KCl and O3
 - d. oxidation of oxalic acid by acidified KMnO.
- 73. During the fusion of an organic compound with sodium metal, nitrogen of the compound is converted into
 - a. NaNO,
- b. NaNH,
- c. NaCN
- d. NaNC
- 74. Identify the product Y in the following reaction sequence

$$CH_2$$
— CH_2 — COO
 Ca
 $\xrightarrow{Heat} X \xrightarrow{Zn-Hg} Y$
 CH_2 — COO

- a. pentane
- b. cyclobutane
- c. cyclopentane
- d. cyclopentanone
- 75. The reaction $C_2H_5ONa + C_2H_5I \longrightarrow C_2H_5OC_2H_5 + NaI$ is known as
 - a. Kolbe's synthesis
 - b. Wurtz's synthesis
 - c. Williamson's synthesis
 - d. Grignard's synthesis
- 76. ΔG^o vs T plot in the Ellingham's diagram, slopes downwards for the reaction

$$a. \text{Mg} + \frac{1}{2} \text{O}_2 \longrightarrow \text{MgO}$$

b.
$$2Ag + \frac{1}{2}O_2 \longrightarrow Ag_2O$$

$$\mathbf{c}. \mathbf{C} + \frac{1}{2} \mathbf{O}_2 \longrightarrow \mathbf{CO}$$

$$d. CO + \frac{1}{2} O_2 \longrightarrow CO_2$$

	$a. CaCO_3 \longrightarrow CaO + C$	02		a. very tast		o. very slov	N.			
	b. $2C + O_2 \longrightarrow 2CO$			c. moderate	ely fast	d. spontane	eous			
	$c. C + O_2 \longrightarrow CO_2$ $d. Fe_2O_3 + 3CO \longrightarrow 2F$	e+3CO ₂		88. Which of electricity		g does not co	nduct			
78	Liquor ammonia bottle		only after	a. Fused N		b. Solid Na	Cl			
70.	cooling. This is because		omy anei	c. Brine sol		d. Copper	iCI			
	a. it is a mild explosive					a. 10 - 500 - 400 - 500				
	b. it is a corrosive liquid			89. When a qu						
	c. it is a lachrymatory					g of copper g				
79. 80. 81.	d. it generates high vapor	ir proceiiyo		deposited. If the same quantity of electricity is passed through acidulated water, then the						
100			2 2							
79.	The formation of O_2^+ [P	경영(해)에 된다. 항공하다면서 가다				at STP will	be			
	formation of xenon fluo		s because	[Given, atomic weight of $Cu = 64$] a. 4.0 cm^3 b. 56 cm^3 c. 604 cm^3 d. 80 cm^3						
	a. O2 and Xe have compa	rable sizes		a. 4.0 cm	0. 56 Cm	c. 604 Cm	a. ao cin			
	b. Both O2 and Xe are gas	es		90. Solubility	product of a	salt AB is 1 >	$(10^{-8} \text{ M}^2 \text{ in})$			
	c. O2 and Xe have compa				그리아 아내리 아이를 하는 것 같아 되었다.	concentratio				
	d. O2 and Xe have compa	rable electron	egativities			l precipitate				
80.	The highest magnetic r				tion of B^- io					
	transition metal ion wit	h the config		a. between	10 ⁻⁸ M to 10	⁻⁷ M				
	a. $3d^2$ b. $3d^5$	c. $3d^7$	d. $3d^9$	b. between	10-7 M to 10	⁻⁶ M				
81.	A transition metal ion e	xists in its h	ighest	$c. > 10^{-5} \text{ M}$	4					
0750000	oxidation state. It is exp			$d. < 10^{-8}$	A .					
	a. a chelating agent									
	b. a central metal, in a coo	ordination cor	npound	91. Which one of the following condition will increase the voltage of the cell represented by						
	c. an oxidising agent									
	d. a reducing agent			the equati		G 2+/ \				
82	In which of the following	og complex i	on the			$Cu^{2+}(aq) + 2A$				
	central metal ion is in a			 a. increase in the dimensions of Cu electrode b. increase in the dimensions of Ag electrode c. increase in the concentration of Cu²⁺ ions 						
	hybridisation?									
	a. [CoF ₆] ³⁻	b. [Co(NH:	() ₆] ³⁺							
	c. [Fe(CN) ₆] ³⁻	d. [Cr(NH.	The state of the s	d. increase	in the concer	ntration of Ag ⁺	ions			
~~		the state of the same		92. The pH of	10 ⁻⁸ M HC	l solution is				
83.	Which of the following	can particip	ate in	a. 8		b. more tha	an 8			
	linkage isomerism?			c. between	6 and 7	d. slightly	more than 7			
	a. NO ₂	I ₂ CH ₂ NH ₂	O3 The mass	of alvoore th						
	c. H ₂ O	d. :NH3		93. The mass of glucose that should be dissol 50 g of water in order to produce the sam						
0.4	SERVICE DOMESTIC STREET, NO.		act band			essure as is pi				
04.	Which of the following order?	nas the nigh	est bond			n the same qu				
		• Uo	d. H ₂	water is						
^-	a. N ₂ b. O ₂	c. He ₂		a. 1 g	b . 3 g	c. 6 g	d. 18 g			
85.	Which of the following	1	20	94. Osmotic p						
	a. H ₂ b. O ₂	c. Li ₂	d. He ₂ ⁺			e is less than				
86.	The concentration of a	reactant X d	ecreases							
	from 0.1 M to 0.025 M			expected from theoretical considerations. This is because a. benzoic acid is an organic solute						
	follows I order kinetics									
	when the concentration			b. benzoic acid has higher molar mass than benzene						
	a. $1.73 \times 10^{-4} \text{ M min}^{-1}$		0 ⁻⁴ M min ⁻¹	c. benzoic acid gets associated in benzene						
	c. $3.47 \times 10^{-5} \text{ M min}^{-1}$	d. 1.73×10) ⁻⁵ M min ⁻¹	d. benzoic acid gets dissociated in benzene						

87. Chemical reactions with very high E_a values are

d. benzoic acid gets dissociated in benzene

generally

77. Which of the following reaction taking place in

the blast furnace is endothermic?

- 95. For a reaction to be spontaneous at all temperatures
 - \boldsymbol{a} . ΔG and ΔH should be negative
 - **b.** ΔG and ΔH should be positive
 - c. $\Delta G = \Delta S = 0$
 - $d. \Delta H < \Delta G$
- 96. Which of the following electrolyte will have maximum flocculation value for Fe(OH)₃ sol.?
 - a. NaCl
- b. Na₂S
- c. (NH₄)₃PO₄
- d. K2SO4
- 97. For a reversible reaction,

$$X(g) + 3Y(g) \rightleftharpoons 2Z(g)$$

 $\Delta H = -40 \text{ kJ}$ the standard entropies of X, Y and Z are 60, 40 and 50 JK⁻¹mol⁻¹respectively.

The temperature at which the above reaction attains equilibrium is about

- a. 400 K
- **b.** 500 K
- c. 273 K
- d. 373 K
- 98. The radii of Na⁺ and Cl⁻ ions are 95 pm and 181 pm respectively. The edge length of NaCl unit cell is
 - a. 276 pm
- **b.** 138 pm
- c. 552 pm
- d. 415 pm
- 99. Inductive effect involves
 - a. displacement of σ-electrons
 - b. delocalisation of π-electrons
 - c. delocalisation of σ-electrons
 - d. displacement of π -electrons
- 100. The basicity of aniline is less than that of cyclohexylamine. This is due to
 - a. + R-effect of -NH2 group
 - b. I-effect of -NH2 group
 - c. R-effect of -NH2 group
 - d. hyperconjugation effect
- 101. Methyl bromide is converted into ethane by heating it in ether medium with
 - a. Al
- b. Zn
- c. Na
- d. Cu
- 102. Which of the following compound is expected to be optically active?
 - a. (CH₃)₂CHCHO
 - b. CH₃CH₂CH₂CHO
 - c. CH₃CH₂CHBrCHO
 - d. CH₃CH₂CBr₂CHO
- 103. Which cycloalkane has the lowest heat of combustion per CH₂ group?
 - a. cyclopropane
- b. cyclobutane
- c. cyclopentane
- d. cyclohexane

- 104. The catalyst used in the preparation of an alkyl chloride by the action of dry HCl on an alcohol is
 - a. anhydrous AlCl₃
- b. FeCl₃
- c. anhydrous ZnCl,
- d. Cu
- 105. In the reaction,

$$R \longrightarrow X \xrightarrow{\text{Alcoholic}} KCN$$

b. aldehyde

 $\xrightarrow{\text{Dilute}} B$, the product B is

- a. alkyl chloride
 c. carboxylic acid
- aldehy
 ketone
- evolve CO₂ when treated with NaHCO₃
 - b. Phenol
- a. Salicylic acid
 c. Benzoic acid
- d. 4-nitro benzoic acid
- By heating phenol, with chloroform in alkali, it is converted into

106. Which of the following compound would not

- a. salicylic acid
- b. salicylaldehyde
- c. anisole
- d. phenyl benzoate
- 108. When a mixture of calcium benzoate and calcium acetate is dry distilled, the resulting compound is
 - a. acetophenone
- benzaldehyde
- c. benzophenone
- d. acetaldehyde
- 109. Which of the following does not give benzoic acid on hydrolysis?
 - a. Phenyl cyanide
- b. Benzoyl chloride
- c. Benzyl chloride
- d. Methyl benzoate
- 110. Which of the following would undergo Hofmann reaction to give a primary amine?

- b. RCO NH CH₃
- c. RCONH,
- d. RCOOR
- 111. Glucose contains in addition to aldehyde group
 - a. one secondary OH and four primary OH groups
 - b. one primary OH and four secondary OH groups
 - c. two primary OH and three secondary OH groups
 - d. three primary OH and two secondary OH groups
- A distinctive and characteristic functional group of fats is
 - a. a peptide group
- an ester group
- c. an alcoholic group
- a ketonic group
- 113. At pH = 4 glycine exists as

- 114. Insulin regulates the metabolism of
 - a. minerals
- b. amino acids
- c. glucose
- d vitamine
- 115. The formula mass of Mohr's salt is 392 g. The iron present in it is oxidised by KMnO4 in acid medium. The equivalent mass of Mohr's salt is
 - a. 392
- b. 31.6
- c. 278
- d. 156
- 116. The brown ring test for nitrates depends on
 - a. the reduction of nitrate to nitric oxide
 - b. oxidation of nitric oxide to nitrogen dioxide
 - c. reduction of ferrous sulphate to iron
 - d. oxidising action of sulphuric acid
- 117. Acrolein test is positive for
 - a. polysaccharides
- b. proteins
- c. oils and fats
- d. reducing sugars

- 118. An organic compound which produces a bluish green coloured flame on heating in presence of copper is
 - a. chlorobenzene
- b. benzaldehvde
- c. aniline
- d. benzoic acid
- **119.** For a reaction, A + B - $\rightarrow C + D$.

If the concentration of A is doubled without altering the concentration of B, the rate gets doubled. If the concentration of B is increased by nine times without altering the concentration of A, the rate gets tripled. The order of the reaction is

- a. 2
- b. 1

- 120. Which of the following solutions will exhibit highest boiling point?
 - a. 0.01 M Na2SO4(aq)
- b. 0.01 M KNO3(aq)
- c. 0.015 M urea(aq)
- d. 0.015 M glucose(aq)

MATHEMATICS

- **121.** If u = a b, v = a + b, and |a| = |b| = 2, then

 - | $\mathbf{u} \times \mathbf{v}$ | \mathbf{s} \mathbf{a} . $2\sqrt{16 (\mathbf{a} \cdot \mathbf{b})^2}$ \mathbf{c} . $\sqrt{16 (\mathbf{a} \cdot \mathbf{b})^2}$ \mathbf{d} . $\sqrt{4 (\mathbf{a} \cdot \mathbf{b})^2}$
- 122. The volume of the tetrahedron formed by the points (1, 1, 1), (2, 1, 3) (3, 2, 2) and (3, 3, 4) in cubic units is
- c. 5

- 123. Unit vector perpendicular to î 2ĵ + 2k and lying in the plane containing $\hat{i} + \hat{j} - 2\hat{k}$ and $-\hat{1} + 2\hat{j} + \hat{k}$ is
 - $a. 8\hat{i} 7\hat{i} + 11\hat{k}$
- **b.** $8\hat{i} + 7\hat{j} 11\hat{k}$
- c. $8\hat{i} 7\hat{j} 11\hat{k}$
- d. $\frac{1}{\sqrt{224}}(8\hat{i}-7\hat{j}-11\hat{k})$
- 124. In the group Q {1} under the binary operation * defined by a * b = a + b + ab the inverse of 10 is

- a. $\frac{1}{10}$ b. $\frac{11}{10}$ c. $\frac{-11}{10}$ d. $\frac{-10}{11}$
- **125.** In the group {1, 2, 3, 4, 5, 6} under multiplication mod 7, $2^{-1} X_7^4 =$
 - a. 1
- c. 2
- d. 3

- **126.** The group (Z, +) has
 - a. exactly one sub-group
 - b. only two sub-groups
 - c. no sub-groups
 - d. infinitely many subgroups
- **127.** If $3x \equiv 5 \pmod{7}$, then
 - $a. x \equiv 2 \pmod{7}$
- $b. x \equiv 3 \pmod{7}$
- $c. x \equiv 4 \pmod{7}$
- d. None of these
- 128. The argument of the complex number

$$\sin\left(\frac{6\pi}{5}\right) + i\left(1 + \cos\frac{6\pi}{5}\right) is$$

- **129.** The maximum value of n < 101, such that

$$1 + \sum_{k=1}^{n} i^k = 0$$
 is

- **130.** The value of $(-1 + \sqrt{-3})^{62} + (-1 \sqrt{-3})^{62}$ is a. 2^{62} b. 2^{+3}

- 131. All complex number z which satisfy the

equation
$$\left| \frac{z - 6i}{z + 6i} \right| = 1$$
 lie on the

- a. imginary axis
- b. real axis
- c. neither of the axes
- d. None of the above

132. The value of $\sin[\cot^{-1}(\cos(\tan^{-1}x))]$ is

$$a.\left(\sqrt{\frac{1+x^2}{2+x^2}}\right)$$

$$b.\left(\sqrt{\frac{2+x^2}{1+x^2}}\right)$$

$$c.\left(\sqrt{\frac{x^2-2}{x^2-1}}\right)$$

$$d.\left(\sqrt{\frac{x^2-1}{x^2-2}}\right)$$

- The value of α(≠0) for which the function $f(x) = 1 + \alpha x$ is the inverse of itself is
 - a. 2c. - 1
- **134.** If x occurs is the expansion of $\left(x + \frac{1}{x}\right)^n$, then its

coefficient is

$$a.\frac{n!}{(r!)^1}$$

b.
$$\frac{n!}{(r+1)!(r-1)!}$$

c.
$$\frac{n!}{\left(\frac{n+r}{2}\right)\left(\frac{n-r}{2}\right)}$$

$$d. \frac{n!}{\left[\left(\frac{n}{2}\right)!\right]^2}$$

- **135.** If $\tan A \tan B = x$ and $\cot B \cot A = y$, then
 - $\cot(A-B) =$ $a. \frac{1}{y} \frac{1}{x}$
- $b.\frac{1}{x}-\frac{1}{y}$
- d. None of these
- $136.\cos^2\frac{\pi}{12} + \cos^2\frac{\pi}{4} + \cos^2\frac{5\pi}{12} =$

- 137. If $\sin \theta$, $\cos \theta$ and $\tan \theta$ are in GP, then $\cot^6 \theta - \cot^2 \theta$ is
 - a. 1
- b.1/2
- c. 2
- **138.** If $\frac{3x^2 2x + 4}{(x-1)^6} = \frac{A_1}{x+1} + \frac{A_2}{(x+1)^2} + \frac{A_3}{(x+1)^3}$
 - $+\frac{A_4}{(x+1)^4}+\frac{A_5}{(x+1)^5}+\frac{A_6}{(x+1)^6}$, then
 - $(A_1 + A_2 + A_2 A_4 A_6) =$ a. (0,0)
 - **b.** (-8, -12)
 - c. (8, -12)
- d. (-8, 12)
- **139.** If $\log_{2}(2^{x-1}+6) + \log_{2}(4^{x-1}) = 5$, then x =
- b. 1
- c. 3
- d. 2

- **140.** If a, b, c, and d are the roots of the equation $x^4 + 2x^3 + 3x^2 + 4x + 5 = 0$, then
 - $1 + a^2 + b^2 + c^2 + d^2$ is equal to
- c. 2
- **141.** If $c_0, c_1, c_2, ..., c_n$ are binomial coefficients of order n, then the value of $\frac{c_1}{2} + \frac{c_2}{4} + \frac{c_3}{6} + \dots$
 - a. $\frac{2^{n}+1}{n-1}$

- **142.** The value of (0.2) $\log_{\sqrt{5}} \left(\frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \dots \right)$ is

- c. 2
- **143.** If n(A) = n(B) = m, then the number of possible bijection from A to B is
 - a. m
- b. m2
- c. m!
- d. 2m
- **144.**sin⁻¹ $\left[x\sqrt{1-x} \sqrt{x}\sqrt{1-x^2} \right] =$
 - **a.** $\sin^{-1} x \sin^{-1} \sqrt{1 x^2}$ **b.** $\sin^{-1} x + \sin^{-1} \sqrt{1 x}$

 - c. $\sin^{-1} x \sin^{1} \sqrt{x}$ d. $\sin^{-1} x + \sin^{-1} \sqrt{x}$
- **145.** If $\tan \theta + \tan 4\theta + \tan 7\theta = \tan \theta \tan 4\theta \tan 7\theta$, then the general solution is
- $b. \theta = \frac{n\pi}{12}$
- $\mathbf{c.}\ \theta = \frac{n\pi}{2}$
- d. None of these
- 146. If a circle with the point (-1, 1) as its center touches the straight line x + 2y + 9 = 0, then the coordinates of the points of contact is
 - a. (-3, 3)
- c. (0, 0)
- $d.\left(\frac{7}{3}, -\frac{17}{3}\right)$
- **147.** If the circles $x^2 + y^2 + 2gx + 2fy = 0$ and $x^2 + y^2 + 2g'x + 2f'y = 0$ touch each other,
 - a. fg = f'g'c. ff' = gg'

- 148. The number of common tangents to the circles $x^{2} + y^{2} = 4$ and $x^{2} + y^{2} - 4x + 2y - 4 = 0$ is

- 149. The length of the tangent drawn from any point on the circle $x^{2} + y^{2} - 4x + 6y - 4 = 0$ to the circle $x^2 + y^2 - 4x + 6y = 0$ is

- **150.** If the foci of the ellipse $\frac{x^2}{25} + \frac{y^2}{h^2} = 1$ and the
 - hyperbola $\frac{x^2}{144} \frac{y^2}{81} = \frac{1}{25}$ coincide, then the value of b^2 is
 - a. 25
- c. 16
- d. 4
- 151. The latusrectum of the ellipse is half the minor axis. Then, its eccentricity is
 - $\sqrt{2}$

- d. None of these
- 152. The ends of the latusrectum of the parabola $x^2 + 10x - 16y + 25 = 0$ are
 - a. (3, 4), (-13, 4)
- **b.** (5, -8), (-5, 8)
- c. (3, -4), (13, 4)
- d. (-3, 4), (13, -4)
- 153. Which of the following functions is differentiable at x = 0?
 - $a. \cos(|x|) + |x|$ $c. \sin(|x|) + |x|$
- **b.** $\cos(|x|) |x|$ $d.\sin(|x|)-|x|$
- **154.** If $x = a \left(\cos t + \log \tan \frac{t}{2}\right)$, $y = a \sin t$, then $\frac{dy}{dx} = a \sin t$
 - a. tan t
- c. cot t
- - then
 - a. a = 1 = b
 - **b.** $a = \cos 2\theta$, $b = \sin 2\theta$
 - $c. a = \sin 2\theta, b = \cos 2\theta$
 - $d. a = \cos \theta, b = \sin \theta$

157. If α , β , γ are the roots of the equation $x^3 + px + q = 0$, then the value of the

determinant
$$\begin{vmatrix} \alpha & \beta & \gamma \\ \beta & \gamma & \alpha \\ \gamma & \alpha & \beta \end{vmatrix}$$
 is

- **a.** q
- b. 0
- $d. p^2 2q$
- 158. The number of distinct real roots of

$$\begin{vmatrix} \sin x & \cos x & \cos x \\ \cos x & \sin x & \cos x \\ \cos x & \cos x & \sin x \end{vmatrix}$$
 in the interval $\left[\frac{-\pi}{4}, \frac{\pi}{4} \right]$ is

- a. 0
- c. 2
- d. 3
- 159. The sum of non-prime positive divisors of 450 is **b.** 1299 c. 1199
- **160.** The last digit of $\sum_{\substack{1 is$

- d. 8
- **161.** The interval I such that $\int_{0}^{1} \frac{dx}{\sqrt{1+x^4}} \in I$ is given by

- **162.** $\int_{0}^{\pi/2} \log(\tan x) dx =$ **a.** $\frac{\pi}{2}$ **b.** 0 **c.** 1

- **163.** The value of $\int_{-\infty}^{\infty} (ax^3 + bx + c) dx$ depends on the
 - a. value of b
- b. value of c
- c. value of a
- d. values of a and b
- 164. The area of the region bound by the curves $y = x^{2}$ and $y = 4x - x^{2}$ is
 - $a. \frac{16}{3}$ sq. units
- **b.** $\frac{8}{3}$ sq. units
- c. $\frac{4}{3}$ sq. units $d \cdot \frac{2}{3}$ sq. unit
- **165.** The particular solution of $\frac{y}{x} \frac{dy}{dx} = \frac{1+y^2}{1+x^2}$, when

$$x = 1, y = 2$$
 is

- **a.** $5(1+y^2) = 2(1+x^2)$ **b.** $2(1+y^2) = 5(1+x^2)$
- $c. 5(1 + y^2) = (1 + x^2)$ $d. (1 + y^2) = 2(1 + x^2)$

166. The solution of the differential equation

$$\frac{dy}{dx} = (x+y)^2 \text{ is}$$

$$a. \frac{1}{x+y} = c$$

$$b. \sin^{-1}(x+y) = x+c$$

$$c. \tan^{-1}(x+y) = c$$

d.
$$\tan^{-1}(x+y) = x+c$$

167. The maximum value of $\left(\frac{1}{x}\right)^{2x^2}$ is

$$a. e^{1/\epsilon}$$

$$d.e^2$$

- **168.**Let x be a number which exceeds its square by the greatest possible quantity, then x =
- b. 1/4
- c. 3/4
- d. 1/3
- **169.** The subtangent at $x = \pi/2$ on the curve y = xsin x is
 - a. 0

- d. None of these
- **170.** The value of $\int \frac{10^{x/2}}{\sqrt{10^{-x} 10^x}} dx$ is

$$a. \frac{1}{\log_e 10} \sin^{-1}(10^x) + c$$

b.
$$2\sqrt{10^{-x}+10^x}+c$$

c.
$$\frac{1}{\log_{e} 10} \sin h^{-1} (10^{x}) + c$$

d.
$$\frac{-1}{\log_{2} 10} \sin h^{-1} (10^{x}) + c$$

- 171. $\int e^x \left\{ \frac{1 + \sin x \cos x}{\cos^2 x} \right\} dx =$
- **b.** $e^x \sec x \tan x + c$
- $c. e^x \tan x + c$
- $\mathbf{d} \cdot e^{x} \cos^{2} x 1 + c$
- 172. $\int \frac{x^2+1}{x^4+1} dx$

a.
$$\frac{1}{\sqrt{2}}\log_e(x^2+1) + e^{-x^2}$$

a.
$$\frac{1}{\sqrt{2}}\log_e(x^2+1) + c$$
 b. $\frac{1}{\sqrt{2}}\tan^{-1}\left(\frac{x^2+1}{x\sqrt{2}}\right) + c$

c.
$$\frac{1}{\sqrt{2}} \tan^{-1}(x^2 - 1) + \epsilon$$

c.
$$\frac{1}{\sqrt{2}} \tan^{-1}(x^2 - 1) + c$$
 d. $\frac{1}{\sqrt{2}} \tan^{-1}\left(\frac{x^2 - 1}{x\sqrt{2}}\right) + c$

- 173. The locus of the mid-point of the intercept of the line $x \cos \alpha + y \sin \alpha = p$ between the coordinate axes is
 - a. $x^{-2} + y^{-2} = 4p^{-2}$ b. $x^{-2} + y^{-2} = p^{-2}$ c. $x^2 + y^2 = 4p^{-2}$ d. $x^2 + y^2 = p^2$
- **174.** If the line through A = (4, -5) is inclined at an angle 45° with the positive direction of the X-axis, then the coordinates of the two points on opposite sides of A at a distance of $3\sqrt{2}$ units are
 - a. (7, 2), (1, 8)
- b. (7, 2), (1, -8)
- c. (7, -2), (1, -8)
- d. (7, 2), (-1, 8)
- **175.** If the line px + qy = 0 coincides with one of the lines given by $ax^2 + 2hxy + by^2 = 0$, then

a.
$$ap^2 + 2hpq + bq^2 = 0$$
 b. $aq^2 + 2hpq + bp^2 = 0$

$$aa^2 + 2hpa + bp^2 = 0$$

$$c. aq^2 - 2hpq + bp^2 = 0$$

- d. None of these
- 176. The function

$$f(x) = \left(\frac{\log_e(1+ax) - \log_e(1-bx)}{x}\right)$$
is

undefined at x = 0. The value which should be assigned to f at x = 0 so that it is continuous at x = 0 is

$$a.\frac{a+b}{2}$$

$$b. a + b$$

$$b. a+b$$
 $c. \log_e(ab)$

- 177. $\lim_{n \to \infty} \frac{(1^2 + 2^2 + \dots + n^2) \sqrt[n]{n}}{(n+1)(n+10)(n+100)} =$

b.
$$\frac{1}{3}$$

$$c.\frac{2}{3}$$

178. The number of triangles in a complete graph with 10 non-collinear vertices is d. 60

179. The angle between hands of a clock when the time is 4.25 AM is signed to

180. The point (5, -7) lies outside the circle

$$a. x^2 + y^2 - 8x = 0$$

b.
$$x^2 + y^2 - 5x + 7y = 0$$

$$c. x^2 + y^2 - 5x + 7y - 1 = 0$$

$$d. x^2 + y^2 - 8x + 7y - 2 = 0$$

ANSWERS

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Phy	/sics
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1. (c)	2. (b)	3. (a)	4. (a)	5. (a)	6. (c)	7. (d)	8. (*)	9. (c)	10. (d)
11. (a)	12. (b)	13. (c)	14. (a)	15. (a)	16. (d)	17. (c)	18. (d)	19. (b)	20. (a)
21. (b)	22. (c)	23. (a)	24. (b)	25. (d)	26. (b)	27. (a)	28. (c)	29. (c)	30. (d)
31. (d)	32. (a)	33. (c)	34. (b)	35. (d)	36. (c)	37. (a)	38. (b)	39. (c)	40. (b)
41. (a)	42. (c)	43. (a)	44. (b)	45. (c)	46. (c)	47. (d)	48. (a)	49. (b)	50. (c)
51. (b)	52. (c)	53. (b)	54. (d)	55. (a)	56. (d)	57. (d)	58. (a)	59. (a)	60. (a)

Chemistry

61. (c)	62. (a)	63. (b)	64. (a)	65. (d)	66. (a)	67. (c)	68. (a)	69. (c)	70. (a)
71. (b)	72. (d)	73. (c)	74. (c)	75. (c)	76. (c)	77. (a)	78. (a)	79. (c)	80. (b)
81. (c)	82. (a)	83. (a)	84. (a)	85. (c)	86. (b)	87. (b)	88. (b)	89. (b)	90. (c)
91. (d)	92. (c)	93. (b)	94. (c)	95. (a)	96. (a)	97. (b)	98. (c)	99. (a)	100. (a)
101. (c)	102. (c)	103. (d)	104. (c)	105. (c)	106. (b)	107. (b)	108. (a)	109. (c)	110. (c)
111. (b)	112. (b)	113. (b)	114. (c)	115. (a)	116. (a)	117. (c)	118. (a)	119. (c)	120. (a)

Mathematics

122. (a)	123. (d)	124. (d)	125. (c)	126. (d)	127. (c)	128. (c)	129. (c)	130. (c)
132. (a)	133. (c)	134. (c)	135. (c)	136. (a)	137. (a)	138. (d)	139. (d)	140. (b)
142. (a)	143. (c)	144. (c)	145. (b)	146. (b)	147. (b)	148. (b)	149. (c)	150. (c)
152. (a)	153. (d)	154. (d)	155. (b)	156. (c)	157. (b)	158. (b)	159. (c)	160. (a)
162. (b)	163. (b)	164. (b)	165. (b)	166. (d)	167. (a)	168. (a)	169. (c)	170. (a)
172. (d)	173. (a)	174. (c)	175. (c)	176. (b)	177. (b)	178. (c)	179. (a)	180. (a)
	132. (a) 142. (a) 152. (a) 162. (b)	132. (a) 133. (c) 142. (a) 143. (c) 152. (a) 153. (d) 162. (b) 163. (b)	132. (a) 133. (c) 134. (c) 142. (a) 143. (c) 144. (c) 152. (a) 153. (d) 154. (d) 162. (b) 163. (b) 164. (b)	132. (a) 133. (c) 134. (c) 135. (c) 142. (a) 143. (c) 144. (c) 145. (b) 152. (a) 153. (d) 154. (d) 155. (b) 162. (b) 163. (b) 164. (b) 165. (b)	132. (a) 133. (c) 134. (c) 135. (c) 136. (a) 142. (a) 143. (c) 144. (c) 145. (b) 146. (b) 152. (a) 153. (d) 154. (d) 155. (b) 156. (c) 162. (b) 163. (b) 164. (b) 165. (b) 166. (d)	132. (a) 133. (c) 134. (c) 135. (c) 136. (a) 137. (a) 142. (a) 143. (c) 144. (c) 145. (b) 146. (b) 147. (b) 152. (a) 153. (d) 154. (d) 155. (b) 156. (c) 157. (b) 162. (b) 163. (b) 164. (b) 165. (b) 166. (d) 167. (a)	132. (a) 133. (c) 134. (c) 135. (c) 136. (a) 137. (a) 138. (d) 142. (a) 143. (c) 144. (c) 145. (b) 146. (b) 147. (b) 148. (b) 152. (a) 153. (d) 154. (d) 155. (b) 156. (c) 157. (b) 158. (b) 162. (b) 163. (b) 164. (b) 165. (b) 166. (d) 167. (a) 168. (a)	132. (a) 133. (c) 134. (c) 135. (c) 136. (a) 137. (a) 138. (d) 139. (d) 142. (a) 143. (c) 144. (c) 145. (b) 146. (b) 147. (b) 148. (b) 149. (c) 152. (a) 153. (d) 154. (d) 155. (b) 156. (c) 157. (b) 158. (b) 159. (c) 162. (b) 163. (b) 164. (b) 165. (b) 166. (d) 167. (a) 168. (a) 169. (c)

Note (*) None of the option is correct.

HINTS & SOLUTIONS

Physics

1. (c) The angle of incidence = i

Let r be the angle of refraction.

According to given situation, reflected rays and refracted rays are perpendicular to each other.

i.e.
$$i + r = 90^{\circ}$$
 ...(i)

.. According to Snell's law,

$$\mu = \frac{\sin i}{\sin r}$$

$$= \frac{\sin i}{\sin(90 - i)}$$
 [:: From Eq. (i)]
$$= \frac{\sin i}{\cos i}$$

$$\mu = \tan i$$
 ...(ii)

If ic be the critical angle for the pair of media, then

$$\mu = \frac{1}{\sin i_C} \qquad ...(iii)$$

From Eqs. (ii) and (iii), we get

$$\tan i = \frac{1}{\sin i_C}$$

$$\sin i_C = \cot i$$

$$i_C = \sin^{-1}(\cot i)$$

2. (b) Refractive index of water = n

Since, fish looks the bird from water (denser medium) to air (rarer medium).

Hence, normal shift d = (n-1)h

But according to question, real depth h = y

$$d = (n-1)y \quad (\because \text{ height of bird} = y)...(i)$$

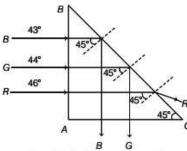
The bird's height from the surface of the water is equal to the summation of the normal shift and height of the bird from the surface.

i.e.
$$d' = y + d = y + (n - 1)y$$
 [From Eq. (i)] $d' = ny$...(ii

Total actual distance between bird and fish

$$=x+d'=x+ny$$

3. (a) The given situation is shown below



Since, critical angles for blue colour and green colour are less than angle of incidence, hence total internal reflection occurs for blue and green colours of light. Again, since critical angle for red colour is greater than angle of incidence hence red colour transmitted outside from surface BC.

4. (a) Let f₁ and f₂ are focal lengths of convex and concave lens respectively, when they are kept in contact co-axially, then focal length F of the combination is given as

$$\frac{1}{F} = \frac{1}{f_1} + \frac{1}{(-f_2)} \quad \begin{bmatrix} \text{Focal length of concave} \\ \text{lens is negative.} \end{bmatrix}$$

$$\Rightarrow \quad \frac{1}{F} = \frac{f_2 - f_1}{f_1 f_2}$$

$$\Rightarrow \quad F = \frac{f_1 f_2}{f_2 - f_1} \quad \dots (i)$$

When both lenses are kept at a distance d, then their combined focal length F' is given as

$$\frac{1}{F'} = \frac{1}{f_1} + \frac{1}{(-f_2)} - \frac{d}{f_1(-f_2)}$$

$$\Rightarrow \frac{1}{F'} = \frac{1}{f_1} - \frac{1}{f_2} + \frac{d}{f_1 f_2}$$

$$\Rightarrow \frac{1}{F'} = \frac{f_2 - f_1 + d}{f_1 f_2}$$

$$\Rightarrow F' = \frac{f_1 f_2}{f_2 - f_2 + d} \qquad ...(ii)$$

From Eqs. (i) and (ii), it is clear that F' < F i.e. focal length of combination will decrease.

- (a) Since, convex lens made of 3 layers of different materials have only one focal length. Thus, for a given object, there is only one image.
- 6. (c) Speed of light in terms of permittivity of free space ϵ_0 and permeability of free space μ_0 is given as

$$C = \frac{1}{\sqrt{\mu_0 \varepsilon_0}} = \sqrt{\frac{1}{\mu_0 \varepsilon_0}}$$

- 7. (d) When a third slit is made in between the double slits in YDSE, then contrast between bright and dark fringes is reduced. It is because in the case of double slits, light passes only two slits. Now, the same light is passing through the three slits which results in reducing the contrast of bright fringes as well as dark
- (*) In double slit experiment, for possible interference maxima on the screen is given as

$$d\sin\theta = n\lambda$$

Given, slit width,
$$d = 4\lambda$$

$$\therefore \qquad 4\lambda \sin\theta = n\lambda$$

$$\Rightarrow$$
 $4\sin\theta = n$

Since, maximum value of $\sin \theta = 1$

 For maximum number of possible interference maxima,

$$4 \cdot 1 = n$$

$$\Rightarrow \qquad n = 4$$
i.e., $n = 0, 1, 2, 3$

∴ Maximum number of possible maxima will be 7 i.e. 0. ± 1. ± 2. ± 3

Hence, no option is correct.

9. (c) Given, wavelength of used light,

$$\lambda = 400 \, \mathrm{nm}$$

For minima in Fraunhofer diffraction,

$$d\sin\theta = n\lambda$$

For first minima n = 1, where $\theta = 30^{\circ}$

For maxima in diffraction,

$$d\sin\theta = (2n+1)\frac{\lambda}{2}$$

For first maxima n = 0

$$\therefore \qquad d\sin\theta = (0+1)\frac{\lambda}{2}$$

$$\Rightarrow \qquad d\sin\theta = \frac{\lambda}{2}$$

$$\Rightarrow \qquad 800\sin\theta = \frac{400}{2}$$

$$\Rightarrow \qquad \sin\theta = \frac{1}{4}$$

$$\Rightarrow \qquad \theta = \sin^{-1}\left(\frac{1}{4}\right)$$

- 10. (d) Greater is the wavelength of wave higher will be its degree of diffraction, since radiowave has maximum wavelength, hence maximum diffraction takes place in a given slit for radio waves.
- 11. (a) When an unpolarised beam of intensity I_0 falls on a polaroid, then after polarisation, the intensity of the emergent beam of light becomes $\frac{I_0}{2}$.
- 12. (b) Materials which have different absorption for perpendicular incident plane for light are called dichoric material crystal. Tourmaline is one example of such type of crystal.

13. (c) Given,
$$Q_1 = 12\mu F = 12 \times 10^{-6} F$$

$$Q_2 = -8\mu F$$

= $-8 \times 10^{-6} F$

Initial value of electrostatic force of attraction between both spheres,

$$\begin{split} F_1 &= \frac{1}{4\pi\epsilon_0} \frac{Q_1 Q_2}{r^2} \\ &= \frac{1}{4\pi\epsilon_0} \cdot \frac{12 \times 10^{-6} \times 8 \times 10^{-6}}{r^2} \\ F_1 &= \frac{1}{4\pi\epsilon_0} \frac{96 \times 10^{-12}}{r^2} & ...(i) \end{split}$$

When both charged spheres are kept in contact, then new charges on the spheres will be

$$Q_1' = Q_2' = \frac{Q_1 + Q_2}{2}$$

= $\frac{12 + (-8)}{2} = 2\mu F = 2 \times 10^{-6} F$

.. Final value of electrostatic force between the spheres,

$$\begin{split} F_2 &= \frac{1}{4\pi\epsilon_0} \frac{Q_1^{'} \times Q_2^{'}}{r^2} \\ &= \frac{1}{4\pi\epsilon_0} \cdot \frac{2 \times 10^{-6} \times 2 \times 10^{-6}}{r^2} \\ F_2 &= \frac{1}{4\pi\epsilon_0} \cdot \frac{4 \times 10^{-12}}{r^2} & ...(ii) \end{split}$$

From Eqs. (i) and (ii), we get

$$From Eqs. (f) and (fif), we get
$$\frac{F_1}{F_2} = \frac{\frac{1}{4\pi\epsilon_0} \cdot \frac{96 \times 10^{-12}}{r^2}}{\frac{1}{4\pi\epsilon_0} \cdot \frac{4 \times 10^{-12}}{r^2}}$$

$$\Rightarrow \qquad \frac{F_1}{F_2} = \frac{24}{1}$$

$$\Rightarrow \qquad F_1 : F_2 = 24 : 1$$$$

 (a) According to given situation, potential at the surface of small conducting sphere of radius r,

$$V_r = \frac{kq}{r} + \frac{kQ}{R}$$

Potential at the surface of bigger conducting sphere of radius R,

$$V_R = \frac{kq}{R} + \frac{kQ}{R}$$

.. Potential difference between the spheres is given as

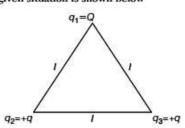
otential difference between the s

$$V_r - V_R = \frac{kq}{r} + \frac{kQ}{R} - \frac{kq}{R} - \frac{kQ}{R}$$

$$= \frac{kq}{r} - \frac{kq}{R} = k\left(\frac{q}{r} - \frac{q}{R}\right)$$

$$= \frac{1}{4\pi\epsilon_0} \left[\frac{q}{r} - \frac{q}{R}\right]$$

15. (a) The given situation is shown below



Net potential energy of the system = 0

i.e.
$$U_{\text{net}} = 0$$

$$\Rightarrow \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 q_2}{l} + \frac{1}{4\pi\epsilon_0} \cdot \frac{q_2 q_3}{l} + \frac{1}{4\pi\epsilon_0} \cdot \frac{q_3 q_1}{l} = 0$$

$$\Rightarrow q_1q_2 + q_2q_3 + q_3q_1 = 0$$

$$\Rightarrow Q.q + q.q + q.Q = 0$$

$$\Rightarrow 2Qq + q^2 = 0$$

$$\Rightarrow q(2Q + q) = 0$$
Since, $q \neq 0$

$$\therefore 2Q + q = 0$$

$$\Rightarrow Q = \frac{-q}{2}$$

16. (d) We know that, in series combination of capacitors, net potential difference is equal to sum of the

individual potential difference of each capacitor i.e.,
$$V = V_1 + V_2 + V_3 \dots$$
 $[V_1 = V_2 = V_3 = 200 \, V]$ $\Rightarrow 600 = n \times 200$ $\Rightarrow n = 3$

So, there should be 3 capacitors in series to obtain the required potential difference. The equivalent capacitance of 3 capacitors in series is given as

$$\frac{1}{C_{\text{eq}}} = \frac{1}{6} + \frac{1}{6} + \frac{1}{6} = \frac{3}{6} = \frac{1}{2}$$

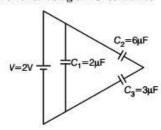
$$\Rightarrow$$
 $C_{eq} = 2\mu I$

Now, we require 18 µF capacitance for this, we need 9 number of such capacitors in parallel.

.: Total number of capacitors (condensers)

$$=9\times3=27$$

17. (c) The given circuit diagram is redrawn as



Equivalent capacitance is given as
$$C_{\rm eq} = \frac{C_2C_3}{C_2+C_3} + C_1 = \frac{6\times 3}{6+3} + 2 = 4\mu {\rm F}$$

∴ Total energy stored in the condenser system,
$$U = \frac{1}{2}C_{eq} \cdot V^2 = \frac{1}{2} \times 4 \times 10^{-6} \times 2^2$$

$$= 8 \times 10^{-6} \text{ J} = 8 \mu \text{J}$$

18. (d) Drift velocity of the electron is given as

$$v_d = \frac{eE\tau}{m}$$

where, e = charge on electron,

E = electric field,

 τ = relaxation time

and m = mass of the electron.

Since,
$$E = \frac{V}{l}$$

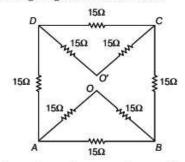
 $\therefore v_d = \frac{eV\tau}{ml}$

Since, e, V, m and l are constant.

On increasing the temperature of metal wire, relaxation time decreases, therefore drift velocity of electrons also decreases.

But on increasing temperature of metal wire, thermal velocity of electron increases.

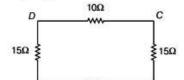
19. (b) Redrawing the given circuit network as



Equivalent resistance between points D and C,

$$R_{DC} = \frac{(15+15)\times15}{(15+15)+15} = \frac{30\times15}{45} = 10\,\Omega$$

Similarly, $R_{AB} = R_{DC} = 10\Omega$ Now, circuit, diagram reduces as



100 :. Equivalent resistance between points A and B is

$$R_{AB} = (15 + 10 + 15) ||10 = 40 || 10 = \frac{40 \times 10}{40 + 10}$$

= $\frac{400}{50} = 8\Omega$

20. (a) Since, the terminals of battery is connected at one quarter distance. Hence, ratio of lengths between two parts will be

$$\frac{l_1}{l_2} = \frac{1}{3}$$

Since,
$$R \propto l$$

$$\therefore R_1 : R_2 = 1:3$$

$$R_1 = \frac{24}{1+3} = 6\Omega$$

$$R_2 = 24 \times \frac{3}{1+3} = 18\Omega$$

Since, potential difference across R_1 and R_2 is same, so they are connected in parallel.

∴ Equivalent resistance of R₁ and R₂,

$$R' = \frac{R_1 R_2}{R_1 + R_2}$$
$$= \frac{6 \times 18}{6 + 18} = 45 \Omega$$

∴ Total resistance,
$$R_T = R' + r$$

= $4.5 + 1.5$ [∴ $r = 1.5 \Omega$]
= 6Ω

Current,
$$I = \frac{V}{R_T} = \frac{18}{6} = 3 \text{ A}$$

According to current division rule, current through bigger arc (i.e. through R_2)

$$I_{R_2} = I.\frac{R_1}{R_1 + R_2} = 3 \times \frac{6}{6 + 18} = 0.75 \text{ A}$$

21. (b)
$$A \xrightarrow{2A} 6\Omega \qquad A \xrightarrow{6\Omega} B$$

Applying Kirchhoff's voltage law, we get
$$-V_{AB} + 6 \times 2 + 12 + 9 \times 2 - 4 + 5 \times 2 = 0$$

$$\Rightarrow \qquad -V_{AB} + 48 = 0$$

$$\Rightarrow \qquad V_{AB} = 48V$$

 (c) Magnetic field at the centre of circular carrying conductor,

$$B_c = \frac{\mu_0 I}{2\pi} \qquad ...(i)$$

Magnetic on the axis at a distance x from the centre is given as

$$B_{\text{axis}} = \frac{\mu_0 I r^2}{2(r^2 + x^2)^{3/2}}$$

Here, x = r

$$B_{\text{axis}} = \frac{\mu_0 I r^2}{2(r^2 + r^2)^{3/2}}$$

$$= \frac{\mu_0 I r^2}{2(2r^2)^{3/2}} = \frac{\mu_0 I r^2}{2 \cdot 2\sqrt{2} \cdot r^3}$$

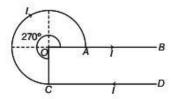
$$B_{\text{axis}} = \frac{\mu_0 I}{4\sqrt{2}r}$$

$$B_{\text{axis}} = B_a = \frac{\mu_0 I}{4\sqrt{2}r}$$

$$\frac{B_c}{B_a} = \frac{\mu_0 I / 2r}{\mu_0 I} = \frac{4\sqrt{2}r}{2r} = 2\sqrt{2}$$

$$B_c : B_a = 2\sqrt{2} : 1$$

23. (a) The given current carrying conductor is shown below



Magnetic field at the centre due to circular wire,

eld at the centre due to circ

$$B_1 = \frac{\mu_0 I}{2r} \times \frac{270}{360} = \frac{\mu_0 I}{2r} \times \frac{3}{4}$$

$$B_1 = \frac{3\mu_0 I}{8r}$$

[in downward to the plane of paper]

Magnetic field at centre O due current carrying wire AB will be zero because point O lies along AB

$$B_2 = 0$$

Magnetic field at O due to current carrying wire CD

$$B_3 = \frac{\mu_0 I}{4\pi r}$$
 (in downward to the plane of paper)

.. Net magnetic field at the centre,

$$\begin{split} B_{\text{net}} &= B_1 + B_2 + B_3 = \frac{3\mu_0 I}{8r} + 0 + \frac{\mu_0 I}{4\pi r} \\ &= \frac{\mu_0 I}{r} \left[\frac{3}{8} + \frac{1}{4\pi} \right] = \frac{\mu_0 I}{4\pi r} \left[\frac{3\pi}{2} + 1 \right] \end{split}$$

24. (b) Given,
$$\theta_A = 60^{\circ}$$
, $\theta_B = 30^{\circ}$

We know that, deflection in galvanometer θ and current I are related as

$$\tan \theta = KNI$$

where, K = constant,

N = number of turns in the coil of galvanometer

and
$$I = \text{current.}$$

$$\therefore \frac{\tan \theta_A}{\tan \theta_B} = \frac{N_A}{N_B}$$

$$\Rightarrow \frac{\tan 60^\circ}{\tan 30^\circ} = \frac{N_A}{N_B}$$

$$\Rightarrow \frac{\sqrt{3}}{\sqrt{3}} = \frac{N_A}{N_B}$$

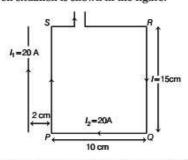
$$\Rightarrow \frac{3}{2} = \frac{N_A}{N_B}$$

25. (d)
$$I_1 = 20$$
A, $I_2 = 20$ A

$$r_1 = 2 \text{ cm}$$

 $r_2 = (10 + 2) \text{ cm} = 12 \text{ cm}$

The given situation is shown in the figure.



The forces on arm SR and PQ are equal in magnitude and opposite in direction and also having same line of action, hence they cancel to each other. :. Resultant force on the current loop PQRS,

$$\begin{split} F &= F_{PS} - F_{QR} \\ &= \frac{\mu_0}{2\pi} \cdot \frac{I_1 I_2 \times l}{r_1} - \frac{\mu_0}{2\pi} \cdot \frac{I_1 I_2 l}{r_2} \\ &= \frac{\mu_0}{2\pi} \cdot I_1 I_2 l \left[\frac{1}{r_1} - \frac{1}{r_2} \right] \\ &= 2 \times 10^{-7} \times 20 \times 20 \times 15 \times 10^{-2} \left[\frac{1}{2 \times 10^{-2}} - \frac{1}{12 \times 10^{-2}} \right] \\ &= 5 \times 10^{-4} \text{ N} \end{split}$$

26. (b) Given, shunt resistance, $R_S = 1\Omega$

Total current, $I = 100 \,\mathrm{A}$

Galvanometer current, $I_{\sigma} = 1A$

We know that,

$$I_g = \frac{IR_S}{R_S + G}$$

$$\Rightarrow \qquad 1 = \frac{100 \times 1}{1 + G}$$

$$\Rightarrow \qquad 1 + G = 100$$

$$\Rightarrow \qquad G = 99\Omega$$

- 27. (a) On moving the circular loops further apart, flux linked with loops will be reduced. Therefore, according to Lenz's law, current will increase in both circular loops to increase the linked flux.
- 28. (c) The given circuit diagram is L-C-R. series circuit,

$$V_R = 80 \text{ V}, V_C = 100 \text{ V}$$

$$V_L = 40 \text{ V}$$
Since, $V_C > V_L$
Value of emf *E* is given as
$$E = \sqrt{V_R^2 + (V_C - V_L)^2}$$

$$= \sqrt{80^2 + (100 - 40)^2}$$

$$= \sqrt{6400 + 3600} = 100 \text{ V}$$

29. (c) For a transformer,

$$I_P = 5 \text{ A}, V_P = 220 \text{ V}$$

 $V_S = 2200 \text{V}$

Power at primary side, $P_i = V_P I_P$ $= 220 \times 5 = 1100 \text{ W}$

Since, 50% power is lost, hence power at secondary side,

$$P_0 = 50\% \text{ of } P_i = \frac{50}{100} \times 1100$$

 $\Rightarrow P_0 = 550 \text{ W}$
 $\Rightarrow V_S I_S = 550$
 $\Rightarrow 2200 \times I_S = 550$
 $\Rightarrow I_S = \frac{550}{2200} = \frac{1}{4} = 0.25 \text{ A}$

30. (d) In series L-C-R circuit,

$$X_L = X_C$$

$$\therefore Z = \sqrt{R^2 + (X_L - X_C)^2}$$

$$= \sqrt{R^2 + 0^2}$$

$$Z = R$$

$$\therefore \text{Power factor} = \cos \phi$$

$$= \frac{R}{Z} = \frac{R}{R} = 1$$

Hence, power factor is not zero.

Therefore option (d) is not correct.

In L-C-R series resonance circuit, peak energy stored by a capacitor is equal to peak energy stored by an inductor.

Average power,
$$P_{\text{avg}} = V_{\text{rms}} \times I_{\text{rms}} \times \cos 0^{\circ}$$

= $V_{\text{rms}} \times I_{\text{rms}}$
= apparent power

L-C-R series resonance circuit is purely resistive because $X_L = X_C$, hence no wattless current exists in this circuit therefore wattless current is zero.

- 31. (d) Solar spectrum is a line absorption spectrum which is also called as Fraunhofer line of missing wavelengths.
- 32. (a) According to first situation wavelength of incident radiation,

$$\lambda_1 = \lambda$$

Stopping potential, $V_{01} = 3V_S$

According to Einstein's photoelectric equation,

$$K_{\text{max}} = h\nu_1 - \phi$$

$$eV_{01} = \frac{hc}{\lambda_1} - \frac{hc}{\lambda_0}$$
[where, λ_0 = threshold wavelength.]
$$\Rightarrow e \cdot 3V_s = hc \left(\frac{1}{\lambda} - \frac{1}{\lambda_0}\right)$$

$$\Rightarrow 3V_{s}e = hc\left(\frac{1}{\lambda} - \frac{1}{\lambda_{0}}\right) \qquad ...(i)$$

According to second situation, wavelength of incident radiation,

$$\lambda_a = 2\lambda$$

 $\lambda_2 = 2 \lambda \label{eq:lambda2}$ Stopping potential, $V_{02} = V_{\rm S}$

Again, Einstein's photelectric equation,

$$K_{\text{max}} = hv_2 - \phi$$

$$\Rightarrow eV_{02} = hc\left(\frac{1}{\lambda_2} - \frac{1}{\lambda_0}\right)$$

$$\Rightarrow eV_s = hc\left(\frac{1}{2\lambda} - \frac{1}{\lambda_0}\right) \qquad ...(ii)$$

Dividing Eq. (i) by Eq (ii), we get
$$3 = \frac{\frac{1}{\lambda} - \frac{1}{\lambda_0}}{\frac{1}{2\lambda} - \frac{1}{\lambda_0}}$$

$$\Rightarrow \frac{3}{2\lambda} - \frac{3}{\lambda_0} = \frac{1}{\lambda} - \frac{1}{\lambda_0}$$

 (c) According to Einstein's photoelectric equation maximum kinetic energy,

$$K_{\text{max}} = eV_0 = hv - \phi_0$$

$$= h(v - v_0) = hc\left(\frac{1}{\lambda} - \frac{1}{\lambda_0}\right)$$

Hence, in photoelectric effect, maximum kinetic energy of emitted photoelectrons depends on work function of metal surface, frequency and wavelength of incident radiation but does not depend on intensity of incident radiation.

34. (b) We know that, wavelength of hydrogen spectrum is given by

$$\frac{1}{\lambda} = R \left(\frac{1}{n_1^2} - \frac{1}{n_2^2} \right)$$

For minimum wavelength of Lyman series,

$$\begin{array}{ll} n_1 = 1 \text{ and } n_2 = \infty \\ & \frac{1}{(\lambda_L)_{\min}} = R \bigg(\frac{1}{(1)^2} - \frac{1}{\infty} \bigg) = R \\ \Rightarrow & (\lambda_2)_{\min} = \frac{1}{R} \end{array}$$

For minimum wavelength of Balmer series,

$$\begin{array}{ccc} n_1 = 2 \text{ and } n_2 = \infty \\ & \frac{1}{(\lambda_B)_{\min}} = R \bigg(\frac{1}{2^2} - \frac{1}{\infty} \bigg) \\ & = R \bigg(\frac{1}{4} - 0 \bigg) = \frac{R}{4} \\ \\ \Rightarrow & (\lambda_B)_{\min} = \frac{4}{R} \\ \\ \therefore & \frac{(\lambda_L)_{\min}}{(\lambda_B)_{\min}} = \frac{R}{\frac{1}{4}} = \frac{1}{4} = 0.25 \end{array}$$

35. (d) Hydrogen atom does not emit X-rays because its energy level are very close to each other. Hence, the transition of electron emits high energy radiations having short wavelength.

36. (c) Given,
$$\lambda_e = \lambda_p$$
 ...(i)

Since, de-Broglie wavelength,

$$\lambda = \frac{h}{mv} = \frac{h}{p} = \frac{h}{\sqrt{2mK}}$$

$$\lambda = \frac{h}{\sqrt{2mK}}$$

 \Rightarrow $\lambda = \frac{h}{\sqrt{2mK}}$

where, K is kinetic energy.

$$\frac{\lambda_e}{\lambda_p} = \sqrt{\frac{m_p}{m_e}} \cdot \sqrt{\frac{K_p}{K_e}}$$

$$\Rightarrow \frac{\lambda_e}{\lambda_e} = \sqrt{\frac{m_p}{m_e}} \cdot \sqrt{\frac{K_p}{K_e}}$$
[From Eq. (i)]
$$\Rightarrow 1 = \sqrt{\frac{m_p}{m_e}} \cdot \sqrt{\frac{K_p}{K_e}}$$

$$\Rightarrow \sqrt{\frac{K_e}{K_p}} = \sqrt{\frac{m_p}{m_e}}$$

Squaring both sides, we get

$$\frac{K_e}{K_p} = \frac{m_p}{m_e}$$

since $m_p > m_e$ $K_e > K_p$

37. (a) Nuclear force between two protons at a separation of 40Å is much greater than electrostatic force between them.

i.e. $F_n >> F_c$

38. (b) Blue colour of water in the sea is due to scattering of light by water molecules. As blue colour of light has smaller wavelength, therefore scattering of blue colour of light is exceptionally large.

Therefore, blue colour of sea water is due to scattering of sunlight by the water molecules.

 (c) Nuclear radius and mass number A are related with following relation,

$$R = R_0 A^{1/3}$$

$$\frac{R_1}{R_2} = \left(\frac{A_1}{A_2}\right)^{1/3}$$

Given, $A_1 = 216$ and $A_2 = 125$

$$\therefore \frac{R_1}{R_2} = \left(\frac{216}{125}\right)^{1/3}$$

$$= \left[\left(\frac{6}{5}\right)^3\right]^{1/3}$$

$$= \frac{6}{5}$$

$$R_1: R_2 = 6:5$$

40. (b) Given, output power, $P_o = 1.6 \text{ MW}$ = $1.6 \times 10^6 \text{ W}$

Energy released per fission,

$$E_1 = 200 \text{ MeV}$$

= $200 \times 10^6 \times 1.6 \times 10^{-19} \text{ J}$
= $320 \times 10^{-13} \text{ J}$
= $3.2 \times 10^{-11} \text{ J}$

The rate of fission R is given as

$$\begin{split} R &= \frac{P_0}{E_1} \\ &= \frac{1.6 \times 10^6}{3.2 \times 10^{-11}} \\ &= 0.5 \times 10^{17} = 5 \times 10^{16} \text{/s} \end{split}$$

 (a) Let initial masses of two radioactive substances be N₀.

If T_1 and T_2 be the half-lives of two radioactive substances,

Then, $T_1 = 1 \text{ yr}$

$$T_2 = 2 \text{ yrs}$$

Total time, t = 6 yrs

Hence, remaining mass of the first substances after

$$t = 6 \text{ yrs}$$

$$N_1 = N_0 \left(\frac{1}{2}\right)^{\frac{t}{1_1}} = N_0 \left(\frac{1}{2}\right)^{6/1}$$

$$= \frac{N_0}{2^6}$$

$$N_1 = \frac{N_0}{2^6}$$

Similarly, remaining mass of the second substance after t = 6 yrs

$$N_{2} = N_{0} \left(\frac{1}{2}\right)^{\frac{t}{T_{2}}} = N_{0} \left(\frac{1}{2}\right)^{6/2} = \frac{N_{0}}{8}$$

$$\Rightarrow \qquad N_{2} = \frac{N_{0}}{8}$$

$$\therefore \qquad \frac{N_{1}}{N_{2}} = \frac{\frac{N_{0}}{64}}{\frac{N_{0}}{9}} = \frac{1}{8} \Rightarrow \frac{N_{1}}{N_{2}} = \frac{1}{8} \qquad ...(i)$$

Since, activity, $A = \lambda N = \frac{0.693}{T}N$

$$\Rightarrow A \propto \frac{N}{T}$$

$$\therefore \frac{A_1}{A_2} = \frac{N_1 T_2}{N_2 T_1} = \frac{1}{8} \times \frac{2}{1} = \frac{1}{4}$$

$$\Rightarrow A_1 : A_2 = 1 : 4$$

42. (c) When an α - particle emits from a radioactive nuclei, then its mass number is decreased by 4 unit and atomic number is decreased by 2 unit.

When a β -particle emits from a radioactive nuclei, then its mass number is unaffected, whereas atomic number is increased by one unit.

Here, initial nuclei = $_{92}U^{235}$

Final nuclei = $_{82}P^{203}$

Change in mass number = 235 - 203 = 32

Number of α -particle emitted = $\frac{32}{4}$ = 8

.. Number of emitted β-particles

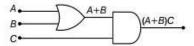
$$= 8 \times 2 - (92 - 82) = 16 - 10 = 6$$

- (a) Neutron is the most stable particle in the baryon group.
- 44. (b) An unbiased p-n junction is shown below.

From the diagram, it is clear that in depletion region, *n*-side has immobile positive charge, whereas *p*-side has immobile negative charge.

Therefore, potential at p is less than that of n.

45. (c) The given logic diagram is shown as



Output of logic gate is given as

$$Y = (A + B)C$$

In option (a), A = 0, B = 1, C = 0

$$Y = (0 + 1) \cdot 0 = 0$$

In option (b), A = 1, B = 0, C = 0

$$Y = (1+0) \cdot 0 = 0$$

In option (c), A = 1, B = 0, C = 1

$$Y = (1+0) \cdot 1 = 1$$

In option (d), A = 1, B = 1, C = 0

$$Y = (1+1) \cdot 0 = 0$$

Hence, to get an output Y = 1

$$A = 1, B = 0 \text{ and } C = 1$$

46. (c) According to Newton's law of gravitation,

$$F = \frac{Gm_1m_2}{r^2}$$

where, F = gravitational force between two bodies of masses m_1 and m_2 ,

r = distance between the two masses

and G = universal gravitational constant.

$$G = \frac{Fr^2}{m_1 m_2}$$

$$G = \frac{[F][r^2]}{[m_1][m_2]}$$

$$= \frac{[MLT^{-2}][L^2]}{[M][M]} = [M^{-1}L^3T^{-2}]$$

 (d) Let u be the initial vertical velocity of the body by which it is projected vertically upward.

If t be the time taken by the body to reach a height h from the point of projection, then using equation of vertical motion,

$$h = ut - \frac{1}{2}gt^{2}$$

$$\Rightarrow gt^{2} - 2ut + 2h = 0$$

$$\Rightarrow t = \frac{2u \pm \sqrt{4u^{2} - 4g \times 2h}}{2g}$$

$$= \frac{u \pm \sqrt{u^{2} - 2gh}}{g}$$

It means t has two values which is already given in question,

$$t_1 = \frac{u + \sqrt{u^2 - 2gh}}{g}$$

and
$$t_2 = \frac{u - \sqrt{u^2 - 2g}}{g}$$

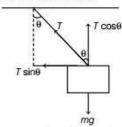
$$\therefore \qquad t_1 + t_2 = \frac{2u}{g}$$

$$\Rightarrow \qquad u = \frac{g(t_1 + t_2)}{2}$$

48. (a) Given, mass suspended from spring balance, m = 10 kg

$$\theta = 60^{\circ}$$

The given situation is shown below



From the diagram, reading of spring balance,

$$F_{c} = T$$
 ...(i)

Since, $T\cos\theta = mg$

$$T = \frac{mg}{\cos \theta} \qquad \dots (ii)$$

From Eqs. (i) and (ii) we get

$$F_s = \frac{mg}{\cos \theta} = \frac{mg}{\cos 60^{\circ}}$$
$$= 2mg$$
$$= 2 \times 10 \times g$$
$$= 20 \text{ kg-wt}$$

49. (b) Weight of body in air,

$$m_1 = 50g = 5 \times 10^{-2} \text{ kg}$$

Weight of body in water,

$$m_2 = 40 \text{ g} = 4 \times 10^{-2} \text{ kg}$$

Buoyant force on the body,

$$\begin{split} F' &= m_1 g - m_2 g \\ &= g (m_1 - m_2) \\ &= g (5 \times 10^{-2} - 4 \times 10^{-2}) \\ F' &= 10^{-2} \ g \ N \\ & \dots (i) \end{split}$$

But buoyant force is given as

$$F' = V\rho g$$
⇒ 10⁻²g = Vρg [From Eq. (i)]
⇒ 10⁻² = ρV
$$10^{-2} = 10^{3} \text{ V} \qquad [\because \rho = 10^{3} \text{ kg/m}^{3}]$$
⇒ V = 10⁻⁵ m³
∴ Loss of weight in liquid = $\rho_{l}Vg$

$$W' = 1.5\rho \times 10^{-5} \times 10$$
= 1.5 × 10³ × 10⁻⁵ × 10
= 0.15 N

:. Loss of weight (in kg) =
$$\frac{w'}{g} = \frac{0.15}{10} = 0.015 \text{ kg} = 15 \text{ g}$$

∴ Weight of body in water = 50 - 15 = 35g

50. (c) We know that, displacement travelled by a moving body with constant acceleration a in nth second,

$$s_n=u+\frac{1}{2}a(2n-1)$$

For first second, n = 1

$$\label{eq:s1} \begin{array}{ll} \therefore & s_1 = u + \frac{1}{2}a(2\times 1 - 1) \\ \\ 5 = u + \frac{a}{2} & \dots \\ \text{(i) } [\because s_1 = 5 \text{ m}] \end{array}$$

For third second, n = 3

$$s_3 = u + \frac{a}{2}(2 \times 3 - 1)$$

$$2 = u + \frac{5a}{2} \qquad ...(ii) [\because s_3 = 2m]$$

Subtracting Eq. (i) from Eq. (ii), we get

$$-3 = 2a$$

$$\Rightarrow a = \frac{-3}{2} \text{ m / s}^2$$

Force acting on the body,

$$F = ma = 4 \times \left(\frac{-3}{2}\right) = -6 \text{ N}$$

Hence, force acting on the body in opposite direction of its motion will be 6N.

51. (b) Time-period of simple pendulum is given as

$$T = 2\pi \sqrt{\frac{l}{g}} \qquad ...(i)$$

If a be the acceleration of the lift, so that time-period of simple pendulum is reduced to T/2.

i.e.
$$T' = T/2$$

$$\Rightarrow 2\pi \sqrt{\frac{l}{g+a}} = \frac{1}{2} \times 2\pi \sqrt{\frac{l}{g}}$$

$$\Rightarrow \frac{l}{g+a} = \frac{1}{4} \cdot \frac{l}{g}$$

$$\Rightarrow g+a = 4g$$

$$\Rightarrow a = 3g$$

52. (c) According to Mayer's formula,

$$C_p - C_V = R$$

where, C_p = specific heat at constant pressure,

 C_V = specific heat at constant volume

R = gas constant.

$$\Rightarrow \frac{C_p}{C_V} - 1 = \frac{R}{C_V}$$

$$\Rightarrow \gamma - 1 = \frac{R}{C_V}$$

$$\Rightarrow$$
 $C_V = \frac{R}{V-1}$

53. (b) Net work done in cyclic process ABCA,

$$W_{\text{net}}$$
 = Area enclosed by path ABCA

$$= \frac{1}{2} \times (3V_1 - V_1)(4p_1 - p_1)$$

$$= \frac{1}{2} \times 2V_1 \times 3p_1 = 3p_1V_1$$

Since, cyclic process is taken in anti-clockwise direction, hence net work done will be negative.

$$W_{\text{net}} = -3p_1V_1$$

- 54. (d) In isothermal process, temperature remains constant, hence internal energy of the system remains constant in isothermal process.
- 55. (a) The given situation is shown below

$$T_1=100^{\circ}\text{C}$$
 T $T_2=0^{\circ}\text{C}$

Copper Steel

 $t_1=18 \text{ cm}$ $t_2=6 \text{ cm}$

Thermal conductivity of copper

$$K_c = 9 K_s$$

Since, both bar are connected in series, hence heat current along the bar will be same.

i. e
$$\frac{dQ}{dt} = \frac{K_{c}A(T_{1} - T)}{l_{1}}$$

$$= \frac{K_{s}A(T - T_{2})}{l_{2}}$$

$$\Rightarrow \frac{9K_{s}A(100 - T)}{18} = \frac{K_{s}A(T - 0)}{6}$$

$$\Rightarrow 3(100 - T) = T$$

$$300 - 3T = T$$

$$\Rightarrow 4T = 300$$

$$\Rightarrow T = 75^{\circ}C$$

56. (d) Equation of simple harmonic wave is given as $y = 6\sin 2\pi (2t - 0.1x)$

Path difference, $\Delta x = 2 \, \text{mm}$

Comparing with standard equation of wave,

$$y = A\sin(\omega t - kx)$$

$$= A\sin 2\pi \left(vt - \frac{k}{2\pi} \cdot x \right)$$

$$\frac{k}{2\pi} = 0.1$$

$$k = 0.2\pi$$
Wavelength, $\lambda = \frac{2\pi}{k} = \frac{2\pi}{0.2\pi} = 10 \text{ mm}$

.. We know that, phase difference,

$$\phi = \frac{2\pi}{\lambda} \times \text{ path difference } (\Delta x)$$
$$= \frac{2\pi}{10} \times 2 = \frac{2\pi}{5} = \frac{2 \times 180}{5} = 72^{\circ}$$

57. (d) Given, sound source is stationary, $v_s = 0$

Apparent frequency, f' = 2f

where, f is actual frequency of sound.

By using Doppler's effect,

$$f' = f\left(\frac{v + v_0}{v}\right)$$

$$f' = f\left(\frac{v + v_0}{v}\right)$$
[where, v is velocity of sound A.]
$$\Rightarrow 2f = f\left(\frac{v + v_0}{v}\right)$$

$$\Rightarrow$$
 $2v = v + v_0$

$$\Rightarrow$$
 $v = v$

$$\Rightarrow$$
 $v_0 = v$

58. (a) Given,
$$T_1 = 27^{\circ} \text{ C} = (273 + 27) \text{ K} = 300 \text{ K}$$

$$T_2 = 627^{\circ} \text{ C}$$

= $(627 + 273)\text{K}$
= 900 K

Energy emitted per second

$$E_1=05~\mathrm{J}$$

$$E_2 = ?$$

According to Stefan's Boltzmann law,

Energy radiated per unit area per second is given by

$$E = \sigma T^*$$

$$E = (T_*)^*$$

$$\Rightarrow \frac{E_2}{E_1} = \left(\frac{T_2}{T_1}\right)^4$$

$$= \left(\frac{900}{300}\right)^4 = 81$$

$$\Rightarrow E_2 = 81E_1 = 81 \times 0.5$$
$$= 40.5 \text{ J}$$

59. (a) Given, $L_2 = 2L_1$, $f_1 = 200$ Hz, $f_2 = 300$ Hz

We know that, frequency of vibrating string is given as

$$f = \frac{1}{2L} \sqrt{\frac{T}{\mu}}$$

where, $\mu = \text{mass per unit length of string}$

L =length of the string.

$$f \propto \frac{\sqrt{T}}{T}$$

$$\Rightarrow \frac{f_2}{f} = \sqrt{\frac{T_2}{T}} \cdot \frac{L_1}{I}$$

$$\Rightarrow$$
 $\sqrt{\frac{T_2}{T_1}} = \frac{f_2 L_2}{f_1 L_1} = \frac{300}{200} \times \frac{2L_1}{L_1}$

$$\sqrt{\frac{T_2}{T_1}} = 3$$

$$\Rightarrow \frac{T_2}{T_1} = 9$$

$$T_2: T_1 = 9:1$$

60. (a) Loudness of sound is given as

$$L=10\log_{10}\frac{I}{I_0}$$
 So, we get $L_2-L_1=10\log_{10}\frac{I_2}{I_1}$ here $L_1=30$ dB, $L_2=60$ dB

Chemistry

61. (c) Carnallite: KCl-MgCl2-6H2O

Dolomite: MgCO3 · CaCO3

Calamine: ZnCO3

Sea water: ore of magneisum

:. Calamine is not an ore of magnesium.

62. (a) Electronic configuration of Ni, Cu and their ions are

Ni =
$$1s^2 2s^2 2p^6 3s^2 3p^6 3d^8 4s^2$$

Cu = $1s^2 2s^2 2p^6 3s^2 3p^6 3d^{10} 4s^1$
Ni²⁺ = $1s^2 2s^2 2p^6 3s^2 3p^6 3d^8 4s^0$
Cu⁺ = $1s^2 2s^2 2p^6 3s^2 3p^6 3d^{10} 4s^0$

Electronic configuration represents Cu+ ions.

63. (b) The element [Ne]3s²3p³ have half-filled p-orbital. As a result, it is more stable.

.. The ionisation energy is highest for this element.

64. (a) The oxidation number of Br in Br2 is zero.

The oxidation number of Br is BrO₃

$$x + 3 \times (-2) = -1$$

$$x = -1 + 6$$

$$x = +5$$

- 65. (d) Among the alkali metals, caesium is most reactive because the outermost electron is more loosely bound than the outermost electron of other alkali metals.
- 66. (a) Electronic configuration of nitrogen is ${}_{7}N = 1s^{2}2s^{2}2p^{3}$ i.e. 2, 5

In outer most shell, it has five electrons.

:. It share 3 electrons to complete its octet as follows :

- 67. (c) Hydrogen bond is strongest in F—H --- F, as the electronegativity of fluorine is highest.
- 68. (a) Decomposition of CaCO₃ as follows:

$$\begin{array}{ccc} {\rm CaCO}_3 & \stackrel{\Delta}{\longrightarrow} & {\rm CaO} + {\rm CO}_2 \\ {\rm 100~g} & {\rm 44~g} \\ {\rm 11.2~dm^2~or}\,({\rm 1/2~mole}) & {\rm 22~g~or}\,{\rm 1/2~mole} \end{array}$$

Neutralisation reaction of KOH and CO2 as follows:

$$2KOH + CO_2 \xrightarrow{\Delta} K_2CO_3 + H_2O$$

2 moles 1 mole
1 mole
$$\frac{1}{2}$$
 mole

$$\therefore \qquad 60 - 30 = 10 \log_{10} \frac{I_2}{I_1}$$

$$\Rightarrow \qquad 3 = \log_{10} \frac{I_2}{I_1}$$

$$\Rightarrow \qquad \frac{I_2}{I_1} = 10^3 \Rightarrow I_2 = 1000I_1$$

1 mole of CO₂ reacts with 2 moles of KOH 1/2 mole of CO₂ reacts with 1 mole of KOH

: Mass of KOH =
$$1 \times 56.1 = 56.1 \text{ g} = 56 \text{ g}$$

1
$$\begin{bmatrix} \because p = 76 \text{ cm Hg} = 1 \text{ atm,} \\ d = 1.964 \text{ g dm}^{-3} \\ R = 0.0821 \text{ dm}^3 \text{ atm K}^{-1} \text{mol}^{-1} \end{bmatrix}$$

M = 44 g/mol \therefore So, gas is CO_2 .

70. (a) 0.06 mole KNO₃ added to 100 cm³ of water at 298 K.

$$\Delta H = 35.8 \text{ kJ/mol}$$
 $\Delta H = m \times C \times \Delta T$

$$\begin{bmatrix} \Delta H \text{ for } 0.06 \text{ mole} = 35.8 \times 0.06 = 2.148 \text{ kJ} \\ \text{Mass} = 100 \text{ cm}^3 = 100 \text{ g} \\ \therefore 2148 = 100 \times 0.004184 \text{ kJ} \times \Delta T \end{bmatrix}$$

 $\Delta T = 5.133 \text{ K}$ It is an endothermic process as heat absorbed.

So, temperature will decrease.

:. Final temperature

$$T = 298 - 5.133$$

 $T = 292.867 \text{ K} \approx 293 \text{ K}$

71. (b)
$$2SO_2 + O_2 \implies 2SO_3$$
Initially 4 moles 4 moles 0
At equili. $(4-2)$ $(4-0.25 \times 4)$ 2
 $= 2$ $= 3$

 \therefore Total moles at equilibrium = 2 + 3 + 2 = 7 moles.

 (d) An example of auto-catalysis is oxidation of oxalic acid by acidified KMnO₄ solution.

In this reaction, one of the product (Mn²⁺) formed act as a catalyst and speed up the reaction.

$$2MnO_4^- + 6H^+ + 5C_2H_2O_4$$

Permagnate ion Oxalic acid $\longrightarrow 2Mn^{2+} + 8H_2O + 10CO_2$
Auto-catalyst

73. (c) When a nitrogeneous organic compound is fused with sodium, the nitrogen present in the compound is converted into sodium cyanide.

This reaction is also called Lassaigne's test.

74. (c) The complete reaction is as follows:

$$\begin{array}{c|c} \operatorname{CH_2-CH_2-COO^-} & \operatorname{CH_2-CH_2} \\ | & \operatorname{CH_2-CH_2-COO^-} \\ & \operatorname{Calcium\ salt} \\ \text{of\ carboxylic\ acid} & \operatorname{Clemmenson} \\ & \operatorname{Clemmenson} \\ & \operatorname{Particle} \\ | & \operatorname{CH_2-CH_2} \\ | & \operatorname{Clemmenson} \\$$

75. (c) Williamson ether synthesis is an organic reaction, forming an ether from alkyl halide and deprotonated alcohol i.e.

76. (c) For the reaction,
$$C + \frac{1}{2}O_2 \longrightarrow CO$$
,

 ΔG° vs T plot in the Ellingham's diagram slopes downwards.

As for this reaction ΔG° become more negative with increase in temperature.

 (a) Decomposition of calcium carbonate to form calcium oxide and carbondioxide is endothermic reaction.

$$CaCO_3 \longrightarrow CaO + CO_2$$

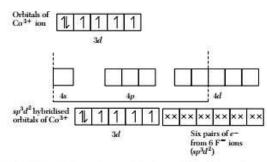
 (a) Liquor ammonia bottle is opened only after cooling because it is a mild explosive.

Note The concentrated ammonia solution in water results in liquor ammonia.

- 79. (c) The formation of O₂⁺[PtF₆]⁻ is the basis for the formation of xenon fluorides because O₂ and Xe have comparable ionisation energies.
- 80. (b) Magnetic moment of the element / ion is highest for configuration 3d⁵, 11111 because number of unpaired electron is maximum i.e. five.
- 81. (c) If a transition metal ion exists in its highest oxidation state, then it behave as oxidising agent. The oxidation number of metal can only decrease from its highest oxidation number i.e. it will undergoes reduction and oxidise other element.
- 82. (a) In [CoF₆]³⁻, F⁻ is a weak ligand. It cannot pair up d-electrons and form outer orbital octahedral complex while NH₃ and CN⁻ are strong ligand.

 $In [CoF_6]^{3-}$, outer orbital 4d is used in hybridisation. Thus, it is called outer orbital or high spin or spin free complex.

$$Co = [Ar] 3d^7 4s^2$$
 and $Co^{3+} = [Ar] 3d^6$



83. (a) Linkage isomerism can be shown by compound containing ambidentate ligand. In NO₂, NO₂ can bind either by N or by O.

e.g.
$$[Co(NH_3)_3(NO_2)]Cl_2$$
 and $[Co(NH_3)_3ONO]Cl_2$

84. (a) N₂[14 electrons] =

$$\begin{split} &\sigma 1s^2, \sigma^* 1s^2, \sigma 2s^2, \sigma^* 2s^2, \ \pi 2\rho_x^2 = \pi 2\rho_y^2, \sigma 2\rho_z^2 \\ &\operatorname{Bond} \operatorname{order} = \frac{N_b - N_a}{2} \left[\begin{aligned} N_b & \operatorname{and} N_a & \operatorname{are} \operatorname{bonding} \operatorname{and} \\ \operatorname{anti} \operatorname{bonding} & \operatorname{molecular} \\ \operatorname{orbital} s - \operatorname{electron} \end{aligned} \right] \end{split}$$

$$=\frac{10-4}{2}=3$$

.. N2 has highest bond order i.e. 3.

While O_2 , He_2 and H_2 have 2, 0 and 1/2 bond order respectively.

85. (c) H₂ and He₂ contains odd number of electrons

... They are paramagnetic.

Among Li₂ and O₂

$$Li_2(6) = \sigma 1s^2, \sigma^* 1s^2, \sigma 2s^2$$

Li have no unpaired electron.

∴ It is diamagnetic

$$O_2(18) = \sigma 1s^2$$
, $\sigma 1s^2$, $\sigma 2s^2$, $\sigma 2s^2 \pi 2p_x^2 = \pi 2p_y^2$
 $\sigma 2p_x^2$, $\pi^* 2p_x^1 = \pi^* 2p_y^1$

It has two unpaired electrons. So, it is paramagnetic.

86. (b) For 1st order reaction

$$k = \frac{2303}{t} \log \frac{[R_0]}{[R]} = \frac{2303}{40} \log \left[\frac{0.1}{0.025} \right]$$
$$= \frac{2303}{40} \times \log 4 = 0.0347 \text{ min}^{-1}$$

Rate expression,

$$r = k[A] = 0.0347 \times 0.01 = 3.47 \times 10^{-4} \text{ M min}^{-1}$$
.

87. (b) According to Arrhenius equation

$$k = Ae^{\frac{-E_d}{RT}}$$

Here, k decreases with increase in E_a (activation energy).

Chemical reaction with very high E_a values are generally slow.

- 88. (b) Solid NaCl does not conduct electricity because the ions (Na+ and Cl-) are well arranged in the crystal structure and not free to move to conduct electricity.
- 89. (b) According to second law of Faraday,

We have a second law of Faraday,
$$\frac{w_1}{E_1} = \frac{w_2}{E_2}$$

$$\frac{0.16}{64} = \frac{w_2}{2}$$

$$w_2 = \frac{0.16 \times 2}{64} = \frac{0.01}{2} = 0.005 \text{ g}$$
Volume of $H_2 = \frac{0.005}{2} \times 22.400 \text{ cm}^3 = \frac{22.4}{4} = 56 \text{ cm}^3$

90. (c)
$$K_{\rm sp} = 10^{-8} {\rm M}^2$$

$$K_{\rm sp} = [A^+][B^-]$$

$$10^{-8} = (10^{-3})[B^{-}]$$

$$[B^{-}] = 10^{-5} \text{ M}$$

... Salt will precipitate, when concentration of $[B^-] > 10^{-5} \text{ M}.$

91. (d) According to Nernst equation,

$$E_{\text{cell}} = E_{\text{cell}}^* - \frac{0.0591}{n} \log \frac{[\text{Cu}^{+2}]}{[\text{Ag}^+]^2}$$

.. The voltage of cell will increase with increase in concentration of Ag+ ions.

92. (c)
$$pH = -\log[H^+]$$

$$[H^+] = 10^{-8} + 10^{-7} = 1.1 \times 10^{-7}$$

$$pH = -\log(1.1 \times 10^{-7})$$

$$pH = 7 - \log(1.1)$$

- ∴ It is between 6 and 7.
- 93. (b) Lowering in vapour pressure is directly proportional to moles of solute particles

$$(\Delta p)_{\text{glucose}} = (\Delta p)_{\text{urea}}$$

$$(\chi_B)_{\text{glucose}} = (\chi_B)_{\text{ure}}$$

i.e.
$$\frac{(\chi_B)_{\text{glucuse}}}{(\chi_B)_{\text{glucuse}}} = (\chi_B)_{\text{urrea}}$$
$$\frac{W_B}{50} \times \frac{18}{180} = \frac{1 \times 18}{50 \times 60}$$

$$W_n = 3 \sigma$$

- 94. (c) Osmotic pressure is a colligative property. It depends upon the number of solute particles. Benzoic acid undergoes dimerisation.
 - ... Number of particles reduces (i < 1) Hence, osmotic pressure observed is less than the theoretical consideration.
- 95. (a) For a reaction to be spontaneous at all temperature ΔG should be negative. As we know $\Delta G = \Delta H - T\Delta S$

$$= -ve - T (+ve) = -ve$$

∴ ∆G and ∆H should be negative.

96. (a) Flocculation value ≈ Coagulating power

Fe(OH) is a positively charged sol.

For coagulating Fe(OH)3 negatively charged electrolyte is used and greater the value of -ve charge, coagulating power will be strong. Among given electrolyte, NaCl has lowest coagulating power. Hence, its flocculation value will be maximum.

97. (b)
$$\Delta H = -40 \text{ kJ} = -40 \times 10^3 \text{ J}$$

$$\Delta S = \Delta S_{Product} - \Delta S_{Reactant}$$

= 2(50) - 3(40) - 60
= 100 - 120 - 60 = -80

$$\Delta G = \Delta H - T\Delta S$$

$$0 = -40 \times 10^3 - T(-80)$$

$$T = \frac{40 \times 10^3}{80} = 500 \text{ K}.$$

98. (c) NaCl forms fee structure.

:.(Diagonal length)² =
$$(\sqrt{2}a)^2 = 2(r^+)^2 + 2(r^-)^2$$

Where, a = edge length, r^+ and r^- are radii of Na⁺ and Cl ions.

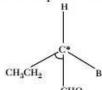
$$a = 2[(r^+)^2 + (r^-)^2] = 2(95 + 181) = 2 \times 276 = 552 \text{pm}$$

- 99. (a) Inductive effect involves the displacement of σ-electrons from less electronegative element to more electronegative element in a compound.
- 100. (a) The basicity of aniline is less than that of cyclohexylamine because of + R-effect of NH2 group in aniline.
- 101. (c) Methyl bromide is converted into ethane by heating, it is ether medium with Na.

$$2CH_3$$
—Br + $2Na$ — $\rightarrow CH_3$ — CH_3 + $2NaBr$
Methyl bromide Sodium Ethane

102. (c) The compound having chiral centre,

CH3CH3CHBrCHO is expected to be optically active.



- 103. (d) Cyclohexane has the lowest heat of combustion per CH2 group. As, stability increase upto 6 membered ring due to decrease in angular strain. Also heat of combustion is measure for chemical stability.
- 104. (c) The catalyst used in preparation of an alkyl chloride by action of dry HCl on alcohol is anhy. ZnCl2. This process is also called Grove's process.

$$\begin{array}{c} \text{ROH + HCl} \xrightarrow{\text{Anhy. ZnCl}_2} \text{RCl + H}_2\text{O} \\ \xrightarrow{\text{Alloyl}} \text{chloride} \end{array}$$

105. (c) The complete reaction is as follows:

$$\begin{array}{c} R \longrightarrow X \xrightarrow{\text{Ale. KCN}} R \longrightarrow \text{CN} \xrightarrow{\text{Dil. HCl}} R \longrightarrow \text{COOH} \\ \text{Alkyl halide} & \text{Alkylcyanide} & \text{Carboxylic acid} \end{array}$$

- 106. (b) Phenol does not decompose sodium bicarbonate (NaHCO₃) as it is a weaker acid than carbonic acid. ∴CO₂ gas is not evolved by phenol.
- 107. (b) Phenol on heating with chloroform in alkali get converted into salicylaldehyde.

This reaction is called Reimer-Tiemann reaction.

108. (a) When a mixture of calcium benzoate and calcium acetate is dry distilled, the resulting compound is acetophenone.

109. (c) Benzylchloride does not give benzoic acid on hydrolysis. It forms benzyl alcohol as major product.

110. (c) In Hofmann bromamide reaction, primary amide reacts with bromine and sodium hydroxide to form isocyanate, which is hydrolysed to give primary amine (with one carbon less) along with decarboxylation.

$$\begin{array}{c} R{\rm CONH_2} + {\rm Br_2} + {\rm NaOH} {\longrightarrow} R {\longrightarrow} {\rm N} {\Longrightarrow} {\rm C} {\Longrightarrow} {\rm O} \\ \\ \frac{{\rm H_2O}}{-{\rm CO_2}} R{\rm NH_2} \\ \end{array}$$

 (b) Glucose contains in addition to aldehyde group on primary OH and four secondary OH groups.

The structure of glucose is

- 112. (b) Fats are triglycerides which are triesters of fatty acid with glycerol. So, the characteristic feature of fats is an ester group.
- 113. (b) At pH = 4, glycine reacts with H+ ion as

$$H_3N^+$$
— CH_2 — $COO^ \xrightarrow{H^+}$
 H_3N^+ — CH_2 — $COOH$

- (c) Insulin regulate the metabolism of glucose (carbohydrates).
- 115. (a) The reaction between Mohr's salt and KMnO₄ is 2KMnO₄ + 10FeSO₄(NH₄)₂SO₄ ·6H₂O + 8H₂SO₄

$$\begin{array}{l} \longrightarrow \mathrm{K_2SO_4} + 2\mathrm{MnSO_4} + 10(\mathrm{NH_4})_2\mathrm{SO_4} \\ + 2\mathrm{Fe_2}(\mathrm{SO_4})_3 + 8\mathrm{H_2O} \end{array}$$

Oxidation sate of Fe changes from +2 to +3.

.: Equivalent weight of Mohr's salt

$$= \frac{\text{molecular weight}}{n\text{-factor}} = \frac{392}{1} = 392 \text{ g}$$

- 116. (a) The brown ring is appeared due to formation of a brown complex between nitric oxide and Fe²⁺ ion. This nitric oxide is formed as a result of reduction of nitrate. Brown ring test for nitrates depends on reduction of nitrate to nitric oxide.
- 117. (c) Acrolein test is positive for oils and fats when fat is heated in presence of KHSO₄, the glycerol portion of molecule is dehydrated and form unsaturated aldehyde. CH₂ = CH—CHO (acrolein) a bad smelling compound.
- 118. (a) An organic compound which produces a bluish green flame, when heated in presence of copper is chlorobenzene. This is called Beilstein's test used to detect presence of halogen in an organic compound.
- 119. (c) Let rate expression, $r = k[A]^x[B]^y$...(i)

 If, $[A_1] = [2A]$, then $r_1 = 2r$ $\therefore x = 1$ If, $[B_2] = [9B]$, then $r_2 = 3r$ $\therefore y = \frac{1}{2}$ Rate expression, $r = k[A][B]^{1/2}$ [By Eq. (i)] \therefore Order = $1 + \frac{1}{2} = \frac{3}{2}$
- 120. (a) For, assume complete dissociation

$$\begin{aligned} \text{For Na}_2 \text{SO}_4; \quad i = 3, m = 0.01 \\ \Delta T_b &= i K_b m \\ \Delta T_b &= 3 \times K_b \times 0.01 = 0.03 \, K_b \end{aligned}$$

$$\text{For, 0.01 M KNO}_3; \quad i = 2, m = 0.01 \\ \Delta T_b &= 2 \times K_b \times 0.01 \, K_b = 0.02 \, K_b \end{aligned}$$

While, urea and glucose are non-electrolyte They do not dissociate into ions highest boiling point is shown by $0.01~\mathrm{M~Na_2SO_4}$ (aq) solution.

Mathematics

121. (a) Given that,
$$u = a - b$$
, $v = a + b$

and
$$|a| = |b| = 2$$

Now,
$$|\mathbf{u} \times \mathbf{v}| = |\mathbf{a} - \mathbf{b} \times \mathbf{a} + \mathbf{b}|$$

$$= 2(\mathbf{a} \times \mathbf{b}) = 2|\mathbf{a}| |\mathbf{b}| \sin \theta$$

$$= 2 \times 2 \times 2\sin\theta = 8\sin\theta = 8\sqrt{1 - \cos^2\theta}$$

$$= 8\sqrt{1 - \left(\frac{\mathbf{a} \cdot \mathbf{b}}{\|\mathbf{a}\| \|\mathbf{b}\|}\right)^2}$$

$$= 8\sqrt{1 - \left(\frac{\mathbf{a} \cdot \mathbf{b}}{4}\right)^2} = 8\sqrt{1 - \left(\frac{\mathbf{a} \cdot \mathbf{b}}{16}\right)^2}$$

$$= \frac{8}{4}\sqrt{16 - (\mathbf{a} \cdot \mathbf{b})^2} = 2\sqrt{16 - (\mathbf{a} \cdot \mathbf{b})^2}$$

So,
$$AB = \hat{i} + 2\hat{k}$$
, $AC = 2\hat{i} + \hat{j} + \hat{k}$

and
$$\mathbf{AD} = 2\hat{\mathbf{i}} + 2\hat{\mathbf{j}} + 3\hat{\mathbf{k}}$$

Volume of tetrahedron =
$$\frac{1}{6} \begin{bmatrix} 1 & 0 & 2 \\ 2 & 1 & 1 \\ 2 & 2 & 3 \end{bmatrix}$$

$$= \frac{1}{6} \left| 1 (3-2) + 0 (6-2) + 2(4-2) \right|$$

$$=\frac{1}{6}(1+0+4)=\frac{5}{6}$$
 cubic units

123. (d) Let
$$\mathbf{a} = \hat{\mathbf{i}} - 2\hat{\mathbf{j}} + \hat{\mathbf{k}}$$
, $\mathbf{b} = \hat{\mathbf{i}} + \hat{\mathbf{j}} - 2\hat{\mathbf{k}}$ and $\mathbf{c} = -\hat{\mathbf{i}} + 2\hat{\mathbf{j}} + \hat{\mathbf{k}}$

Now,
$$\mathbf{b} \times \mathbf{c} = \begin{vmatrix} \hat{\mathbf{i}} & \hat{\mathbf{j}} & \hat{\mathbf{k}} \\ 1 & 1 & -2 \\ -1 & 2 & 1 \end{vmatrix} = 5\hat{\mathbf{i}} + \hat{\mathbf{j}} + 3\hat{\mathbf{k}}$$

Now,
$$\mathbf{a} \times (\mathbf{b} \times \mathbf{c}) = \begin{vmatrix} \hat{\mathbf{i}} & \hat{\mathbf{j}} & \hat{\mathbf{k}} \\ 1 & -2 & 2 \\ 5 & 1 & 3 \end{vmatrix} = -8\hat{\mathbf{i}} + 7\hat{\mathbf{j}} + 11\hat{\mathbf{k}}$$

Now, any vector perpendicular to \mathbf{a} and lying in the plane containing $\hat{\mathbf{i}} + \hat{\mathbf{j}} - 2\hat{\mathbf{k}}$ and $-\hat{\mathbf{i}} + 2\hat{\mathbf{j}} + \hat{\mathbf{k}}$ is $\pm (\mathbf{a} \times (\mathbf{b} \times \mathbf{c}))$.

:. Required unit vector =
$$\pm \frac{(-8\hat{\mathbf{i}} + 7\hat{\mathbf{j}} + 11\hat{\mathbf{k}})}{\sqrt{(-8)^2 + (7)^2 + (11)^2}}$$

$$= \pm \frac{(-8\hat{i} + 7\hat{j} + 11\hat{k})}{\sqrt{234}}$$

124. (d) Let the inverse element of 10 be e, then

$$a * e = 0$$

Therefore, 10 * e = 10 + e + 10e = 0

$$\Rightarrow$$
 $10 + 11e = 0$

$$\Rightarrow$$
 11 $e = -10$

$$\Rightarrow$$
 $e = \frac{-10}{11}$

125. (c) Under Multiplication Modulo 7, inverse of 2 is

$$2 \times 4 = 1 \pmod{7}$$

Hence,
$$2^{-1} = 4$$

Now,
$$2^{-1} \times 4 = 4 \times 4 = 16$$

Now,
$$16 = 2 \times 7 + 2$$

Hence dividing 16 by 7 gives a remainder 2,

Therefore, value of above multiplication mod is 2.

126. (d) The group (z, +) has infinitely many subgroups.

127. (c) Given,
$$3x \equiv 5 \pmod{7}$$

$$\Rightarrow 3x - 5 \equiv 0 \pmod{7} = \frac{7}{3x - 5}$$

$$\Rightarrow$$
 $3x-5=7P$, where $P \in Z$

$$\Rightarrow$$
 $x \equiv 4 \pmod{7}$

128. (c) Let
$$z = \sin\left(\frac{6\pi}{5}\right) + i\cos\left(1 + \cos\frac{6\pi}{5}\right)$$

Putting
$$\sin \frac{6\pi}{5} = r \cos \alpha$$
 ...(i)

and
$$1 + \cos \frac{6\pi}{5} = r \sin \alpha$$
 ...(ii)

On dividing Eq. (ii) by Eq. (i), we get

$$\tan \alpha = \frac{1 + \cos \frac{6\pi}{5}}{\sin \left(\frac{6\pi}{5}\right)} = \frac{2\cos^2 \frac{3\pi}{5}}{2\sin \frac{3\pi}{5}\cos \frac{3\pi}{5}}$$
$$= \cot \frac{3\pi}{5} = \tan \left(\frac{\pi}{2} - \frac{3\pi}{5}\right)$$

$$\tan \alpha = \tan \left(-\frac{\pi}{10} \right)$$

$$\therefore$$
 Argument to z is $\alpha = -\frac{\pi}{10}$

129. (c) We have,

$$\sum_{i=1}^{n} i^{k} = i + i^{2} + i^{3} + i^{4} + i^{5} + i^{6} + i^{7} + i^{8} + i^{9} + \dots$$

Now as,
$$t^4 = t^8 = t^{12} = ...t^{4n} = 1$$

and
$$i + i^2 + i^3 + i^4 = 0$$

 $= 0 + 0 + 0 + \dots$

So,
$$\sum_{n=1}^{n} i^{k} = i + i^{2} + i^{3} + i^{4} + i^{5} + i^{6} + \dots + i^{7} + i^{8} + i^{9} + \dots$$

= $i + i^{2} + i^{3} + i^{4} + (i + i^{2} + i^{3} + i^{4}) + (i + i^{2} + i^{3} + i^{4}) + \dots$

When we take n = 99 after 96th term, we will be left with $0 + i + i^2 + i^3 = -1$

So, for
$$n = 99$$

$$\Rightarrow 1 + \sum_{k=1}^{n} t^{k} = 0$$

130. (c) We have,

$$(-1 + \sqrt{-3})^{62} + (-1 - \sqrt{-3})^{62}$$

$$= 2^{62} \left[\left(\frac{-1 + \sqrt{3}i}{2} \right)^{62} + \left(\frac{-1 - \sqrt{3}i}{2} \right)^{62} \right]$$

$$= 2^{62} [\omega^{62} + \omega^{124}]$$

$$= 2^{62} [\omega + \omega^{2}]$$

$$= 2^{62} (-1) = -2^{62}$$

131. (b) We have,

$$\left|\frac{z-6i}{z+6i}\right| = 1$$
or
$$\left|z-6i\right| = \left|z+6i\right|$$
Let
$$z = x+iy$$
or
$$\left|x+iy-6i\right| = \left|x+iy+6i\right|$$

$$\left|x+(y-6)i\right| = \left|x+(y+6)i\right|$$

$$\Rightarrow \sqrt{x^2+(y-6)^2} = \sqrt{x^2+(y+6)^2}$$

$$\Rightarrow x^2+(y-6)^2 = x^2+(y+6)^2$$

$$\Rightarrow y^2+36-12y = y^2+36+12y$$

$$\Rightarrow 24y = 0$$

$$\Rightarrow y = 0$$

Hence, it is lie on the real axis.

132. (a) We have,

$$\sin[\cot^{-1}\{\cos(\tan^{-1}x)\}]$$

Now,
$$\cos(\tan^{-1} x) = \cos\left[\cos^{-1} \frac{1}{\sqrt{x^2 + 1}}\right]$$

$$= \frac{1}{\sqrt{x^2 + 1}}$$
[: $\cos(\cos^{-1} x) = x, \ \forall x \in [-1, \ 1]$]
So, $\cot^{-1} \left(\frac{1}{\sqrt{x^2 + 1}}\right) = \sin^{-1} \left(\frac{\sqrt{x^2 + 1}}{\sqrt{x^2 + 2}}\right)$
Thus, $\sin\left[\cot^{-1} \left(\frac{1}{\sqrt{x^2 + 1}}\right)\right] = \sin\left[\sin^{-1} \left(\frac{\sqrt{x^2 + 1}}{\sqrt{x^2 + 2}}\right)\right]$

$$= \frac{\sqrt{(x^2 + 1)}}{\sqrt{x^2 + 2}}$$
 [: $\sin(\sin^{-1} x) = x, \ \forall x \in [-1, \ 1]$

133. (c) Let
$$y = 1 + \alpha x$$
 [$f(x) = y$]

$$\Rightarrow x = \frac{y - 1}{\alpha}$$

$$\Rightarrow f^{-1}(x) = \frac{x - 1}{\alpha}$$

It is given that, $f(x) = f^{-1}(x)$

$$\Rightarrow 1 + \alpha x = \frac{x-1}{\alpha}$$

$$\Rightarrow \alpha + \alpha^2 x = x - 1$$

On compare the coefficients, we get

$$\alpha^2 = 1$$
 and $\alpha = -1$

$$\Rightarrow \alpha = -1$$

134. (c) Let x^r occurs in the expansion of $\left(x + \frac{1}{x}\right)^n$

$$\begin{split} T_{r+1} &= {}^{n}C_{p}x^{n-p}\bigg(\frac{1}{x}\bigg)^{p} \\ &= {}^{n}C_{p}x^{n-p}x^{-p} = {}^{n}C_{p}x^{n-2p} \\ \text{let} & n-2p = r \\ \Rightarrow & n-r = 2p \implies p = \frac{n-r}{2} \\ \text{So, coefficient of } x^{r} = {}^{n}C_{p} = \frac{n!}{p!(n-p)!} \end{split}$$

$$= \frac{n!}{\left(\frac{n-r}{2}\right)! \left(n - \frac{n-r}{2}\right)!}$$
$$= \frac{n!}{\left(\frac{n-r}{2}\right)! \left(\frac{n+r}{2}\right)!}$$

135. (c) We have,

$$\tan A - \tan B = x$$
and $\cot B - \cot A = y$

$$\Rightarrow \frac{1}{\tan B} - \frac{1}{\tan A} = y$$

$$\Rightarrow \frac{\tan A - \tan B}{\tan A \tan B} = y$$

$$\Rightarrow \tan A \tan B = \frac{x}{y}$$

$$\Rightarrow \cot A \cot B = \frac{y}{x}$$
Now, $\cot(A - B) = \frac{1 + \cot A \cot B}{\cot B - \cot A}$

$$= \frac{1 + \frac{y}{x}}{y} = \frac{x + y}{xy} = \frac{1}{y} + \frac{1}{x}$$

136. (a)
$$\cos^2 \frac{\pi}{12} + \cos^2 \frac{\pi}{4} + \cos^2 \frac{5\pi}{12}$$

$$= \cos^2 \frac{\pi}{12} + \cos^2 \frac{\pi}{4} + \cos^2 \left(\frac{\pi}{2} - \frac{\pi}{12}\right)$$

$$= \cos^2 \frac{\pi}{12} + \cos^2 \frac{\pi}{4} + \sin^2 \frac{\pi}{12}$$

$$= 1 + \cos^2 \frac{\pi}{4} = 1 + \left(\frac{1}{\sqrt{2}}\right)^2 = 1 + \frac{1}{2} = \frac{3}{2}$$

137. (a) $\because \sin \theta$, $\cos \theta$ and $\tan \theta$ are in GP.

So,
$$\cos^2 \theta = \sin \theta \cdot \tan \theta$$

$$\Rightarrow \cos^3 \theta = \sin^2 \theta$$

$$\Rightarrow \cot^3 \theta = \frac{1}{\sin \theta} = \csc \theta$$

Squaring both sides, we get

$$\cot^6 \theta = \csc^2 \theta$$

$$\Rightarrow$$
 $\cot^6 \theta = 1 + \cot^2 \theta$

$$\Rightarrow$$
 $\cot^6 \theta - \cot^2 \theta = 1$

138. (d) We have,

$$\frac{3x^2 - 2x + 4}{(x - 1)^6} = \frac{A_1}{x + 1} + \frac{A_2}{(x + 1)^2} + \frac{A_3}{(x + 1)^3} + \frac{A_4}{(x + 1)^4} + \frac{A_5}{(x + 1)^5} + \frac{A_6}{(x + 1)^6} \dots (i)$$

Now, put x = 0 in Eq. (i), we get

$$A_1 + A_2 + A_3 + A_4 + A_5 + A_6 = 4$$
 ...(ii)

If
$$A_1 + A_3 + A_5 = -8$$

and
$$A_2 + A_4 + A_6 = 12$$

satisfies the equation.

Hence, only option (i.e. -8, 12) satisfies the solution.

139. (d) We have,

$$\log_2(2^{x-1} + 6) + \log_2(4^{x-1}) = 5$$

$$\Rightarrow 2^{x-1} + 6)(2^{2x-2}) = 2^5$$
Let $y = 2^{x-1}$

$$\Rightarrow (y+6)y^2 = 2^5$$

$$\Rightarrow y^3 + 6y^2 - 32 = 0$$

$$\Rightarrow (y-2)(y^2 + 8y + 16) = 0$$
So, $y = 2$

$$2^{x-1} = 2^1$$

On comparing both sides, we get

$$x - 1 = 1$$
$$x = 2$$

140. (b) As,

$$(a+b+c+d)^2 = a^2 + b^2 + c^2 + d^2 + 2(ab+bc+ad+bc+bd+cd)$$

$$\Rightarrow a^2 + b^2 + c^2 + d^2 = (a+b+c+d)^2 - 2[ab+bc+ac+ad+bd+cd]$$

Now, as a, b, c, d are the roots of the equation. We have,

$$a+b+c+d = \frac{-2}{1} = -2$$

and
$$ab + ac + ad + bc + bd + cd = \frac{3}{1} = 3$$

We have,
$$1 + a^2 + b^2 + c^2 + d^2$$

= $1 + (-2)^2 - 2(3)$
= $1 + 4 - 6 = -1$

141. (b) We have,

$$c_1 x + c_3 x^3 + c_5 x^5 + \dots = \frac{1}{2} \{ (1+x)^n - (1-x)^n \}$$

$$\Rightarrow \int_0^1 (c_1 x + c_3 x^3 + c_5 x^5 + \dots) dx$$

$$= \frac{1}{2} \int_0^1 (1+x)^n - (1-x)^n dx$$

$$\Rightarrow \frac{c_1}{2} + \frac{c_3}{4} + \frac{c_5}{6} + \dots = \frac{2^n - 1}{n+1}$$

$$\log_{\sqrt{5}} \left(\frac{1}{4} + \frac{1}{4 \cdot 2} + \frac{1}{4} \left(\frac{1}{2} \right)^2 + \dots \right)$$

$$= (0.2)$$

$$\log_{\sqrt{5}} \left(\frac{1}{2} \right)$$

$$= (0.2)$$

$$= (0.2)^{\log \sqrt{5} \left(\frac{1}{2}\right)}$$

$$= \left(\frac{1}{5}\right)^{\log \sqrt{5} \left(\frac{1}{2}\right)} = \left(\frac{1}{2}\right)^{2\log_5 \frac{1}{5}}$$

$$= \frac{1}{2}^{-2\log_5 5} = \left(\frac{1}{2}\right)^{-2}$$

$$= (2^{-1})^{-2} = 2^2 = 4$$

143. (c) If set A and B has m elements, then the number of bijections from A to B is the total number of arrangements of n distinct items taken all at a time, i.e. m!.

144. (c) Let,
$$y = \sin^{-1}[x\sqrt{1-x} - \sqrt{x}\sqrt{1-x^2}]$$

$$= \sin^{-1}[x\sqrt{1-(\sqrt{x})^2} - \sqrt{x}\sqrt{1-x^2}]$$

$$= \sin^{-1}x - \sin^{-1}\sqrt{x}$$
[Using $\sin^{-1}x - \sin^{-1}y = \sin^{-1}[x\sqrt{1-y^2} - y\sqrt{1-x^2}]$

145. (b) We have,

$$\tan\theta + \tan 4\theta + \tan 7\theta = \tan\theta \tan 4\theta \tan 7\theta$$
$$\tan\theta + \tan 4\theta = \tan\theta \tan 4\theta \tan 7\theta - \tan 7\theta$$

$$\tan \theta + \tan 4\theta = -\tan 7\theta(1 - \tan \theta \tan 4\theta)$$

$$\frac{\tan\theta + \tan 4\theta}{1 - \tan\theta \tan 4\theta} = -\tan 7\theta$$

$$\tan(\theta + 4\theta) = -\tan 7\theta$$

$$\tan 5\theta = \tan(-7\theta)$$

$$\therefore 5\theta = -7\theta$$

$$12\theta = 0 \text{ or } 12\theta = n\pi$$

So,
$$\theta = \frac{n\pi}{12}, \forall n \in I$$

146. (b) The normal to the tangent will pass through the centre. Also, the intersection of the normal and tangent will give the point of contact.

Hence, cosider the equation of tangent

$$y = -\frac{n}{2} - 45$$

Here,
$$m = \frac{-1}{2}$$

Therefore, slope of the normal is 2.

Since, slope of normal and tangent are mutually perpendicular.

Therefore, equation of the normal at (1, -1) is

$$\frac{y-1}{x+1} = 2$$
 or $y-1 = 2x+2$

$$\Rightarrow$$
 $2x - y = -3$

Therefore, we have two equations 2x - y = -3

and
$$x + 2y + 9 = 0$$

Solving these two equations give us (x, y) = (-3, -3)

Hence, point of contact is (-3, -3).

147. (b) For given condition,

$$\frac{2g}{2g'} = \frac{2f}{2f'}$$

148. (b) Given, circles are $x^2 + y^2 = 4$ and

$$x^2 + y^2 - 4x + 2y - 4 = 0$$

i.e.
$$x^2 + y^2 = 4$$
 ...(i)

and
$$(x-2)^2 - 4 + (y+1)^2 - 1 - 4 = 0$$

$$\Rightarrow x^2 + y^2 = 4$$
 and $(x-2)^2 + (y+1)^2 = 9$...(ii)

Center and radius of circles (i) is

$$c_1 = (0, 0), r_1 = 2$$

and center and radii of circle (ii) is

$$c_2 = (2, -1), r_2 = 3$$

So, difference between c_1 and $c_2 = \sqrt{5}$

Now here,

$$1 = r_2 - r_1 < \sqrt{5} = c_1 c_2 < 5 = r_1 + r_2$$

$$r_2 - r_1 < c_1 c_2 < r_1 + r_2$$

Hence, there will be two common tangents.

149. (c) Length of tangent from $x^2 + y^2 + 2gx + 2fy + c_1 = 0$

To the circle
$$x^2 + y^2 + 2gx + 2fy + c_2 = 0$$

is
$$\sqrt{c_2-c_1}$$

Here,
$$c_2 = 4$$
 and $c_1 = 0$

So, required length =
$$\sqrt{4-0} = \sqrt{4} = 2$$

150. (c) Eccentricity for $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ is $b^2 = a^2(1 - e^2)$ and

$$\frac{x^2}{\frac{144}{25}} - \frac{y^2}{\frac{81}{25}} = 1 \text{ is}$$

$$e_1 = \frac{a_1^2 + b_1^2}{a_1^2}$$

So,
$$e_1 = \sqrt{1 + \frac{81}{144}} = \frac{15}{12}$$

Again, foci =
$$a_1e_1 = \frac{12}{5} \times \frac{15}{12} = 3$$

So, focus of hyperbola is (3, 0) = (ae, 0)

and focus of ellipse is (ae, 0) = (5a, 0)

As, this foci are same, so

$$5a = 3$$

$$e = \frac{3}{5}$$

So,
$$e^2 = 1 - \frac{b^2}{a^2} = 1 - \frac{b^2}{25}$$

$$\Rightarrow \frac{b^2}{25} = 1 - e^2 = 1 - \frac{9}{25}$$

$$\Rightarrow \frac{b^2}{25} = \frac{16}{25}$$

$$-16^2 - 16$$

151. (c) Given that, $\frac{2b^2}{a} = \frac{2b}{2}$

$$a = 2b$$

Now,
$$b^2 = a^2(1 - e^2)$$

$$b^2 = 4b^2(1 - e^2)$$

$$\frac{1}{4} = 1 - e^2$$

$$\Rightarrow e^2 = 1 - \frac{1}{4} = \frac{3}{4}$$

$$\Rightarrow e = \sqrt{\frac{3}{4}} = \frac{\sqrt{3}}{2}$$

152. (a) Given, equation of parabola is $x^2 + 10x - 16y + 25 = 0$

It can be rewritten as

$$(x+5)^2 = 16y$$
 ...(i)

Here a = 4 and vertex $\equiv (-5, 0)$

and focus $\equiv (-5, 4)$

So, y-coordinate of ends of latusrectum will be 4.

Putting in equation, we have

$$(x+5)^2 = 16 \times 4 = 64$$

$$\Rightarrow x+5 = \pm 8$$
So, $x = 3, -13$

Substituting x in Eq. (i), we get y = 4, 4

Hence, ends of latusrectum will be (3, 4) and (-13, 4).

153. (d) (a) We have,

$$f(x) = \cos |x| + |x|$$

$$= \begin{cases} \cos(-x) + (-x), & x < 0 \\ \cos(x) + x, & x \ge 0 \end{cases}$$

$$= \begin{cases} \cos x - x, & x < 0 \\ \cos x + x, & x \ge 0 \end{cases}$$

$$\therefore f'(x) = \begin{cases} -\sin x - 1, & x < 0 \\ -\sin x + 1, & x \ge 0 \end{cases}$$

$$f'(0^-) = -1$$
 and $f'(0^+) = 1$

$$\Rightarrow f'(0^-) \neq f'(0^+)$$

So, it is not differentiable at x = 0.

(b) We have,

$$f(x) = \cos|x| - |x|$$

$$= \begin{cases} \cos(-x) - (-x), & x < 0 \\ \cos(x) - x, & x \ge 0 \end{cases}$$

$$= \begin{cases} \cos x + x, & x < 0 \\ \cos x - x, & x \ge 0 \end{cases}$$

$$\therefore f'(x) = \begin{cases} -\sin x + 1, & x < 0 \\ -\sin x - 1, & x \ge 0 \end{cases}$$

$$\therefore f'(0^-) = 1 \text{ and } f'(0^+) = -1$$

$$\Rightarrow f'(0^-) \neq f'(0^+)$$

So, it is not differentiable at x = 0.

(c) We have,

$$f(x) = \sin |x| + |x|$$

$$= \begin{cases} \sin(-x) + (-x), & x < 0 \\ \sin(+x) + (+x), & x \ge 0 \end{cases}$$

$$= \begin{cases} -\sin x - x, & x < 0 \\ \sin x + x, & x \ge 0 \end{cases}$$

$$\therefore f'(x) = \begin{cases} -\cos x - 1, & x < 0 \\ \cos x + 1, & x \ge 0 \end{cases}$$

$$\therefore f'(0^{-}) = -1 - 1 = -2$$
and
$$f'(0^{+}) = 1 + 1 = 2 \implies f'(0^{-}) \ne f'(0^{+})$$

So, it is not differentiable at x = 0.

(d) We have,

$$f(x) = \sin |x| - |x|$$

$$= \begin{cases} \sin(-x) - (-x), & x < 0 \\ \sin x - x, & x \ge 0 \end{cases}$$

$$= \begin{cases} -\sin x + x, & x < 0 \\ \sin x - x, & x \ge 0 \end{cases}$$

$$\therefore f'(x) = \begin{cases} -\cos x + 1, & x < 0 \\ \cos x - 1, & x \ge 0 \end{cases}$$

$$\therefore f'(0^{-}) = -1 + 1 = -0$$

$$\text{and } f^{1}(0^{+}) = 1 - 1 = 0$$

$$\Rightarrow f'(0^{-}) = f'(0^{+})$$

So, it is differentiable at x = 0.

154. (d) We have,

Now,
$$\frac{dx}{dt} = a \left\{ -\sin t + \frac{1}{\tan \frac{t}{2}} \cdot \sec^2 \frac{t}{2} \cdot \frac{1}{2} \right\}$$
$$= a \left\{ -\sin t + \frac{1}{\sin t} \right\}$$
$$= a \left(\frac{1 - \sin^2 t}{\sin t} \right) = \frac{a \cos^2 t}{\sin t}$$
and
$$y = a \sin t$$
$$\frac{dy}{dt} = a \cos t$$
So,
$$\frac{dy}{dt} = \frac{dy}{dt}$$

So,
$$\frac{dy}{dx} = \frac{dy/dt}{dx/dt}$$
$$= \frac{a(\cos t \sin t)}{a \cos^2 t} = \tan t$$

$$\begin{bmatrix} 1 & \tan \theta \\ -\tan \theta & 1 \end{bmatrix}^{-1} = \frac{1}{1 + \tan^{2}\theta} \begin{bmatrix} 1 & -\tan \theta \\ \tan \theta & 1 \end{bmatrix}$$

$$\begin{bmatrix} \vdots \begin{bmatrix} a & b \\ c & d \end{bmatrix}^{-1} = \frac{1}{ad - bc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix} \end{bmatrix}$$

$$\text{Now,} \begin{bmatrix} 1 & -\tan \theta \\ \tan \theta & 1 \end{bmatrix} \begin{bmatrix} 1 & \tan \theta \\ -\tan \theta & 1 \end{bmatrix}^{-1} = \begin{bmatrix} a & -b \\ b & a \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 1 & -\tan \theta \\ \tan \theta & 1 \end{bmatrix} \begin{bmatrix} 1 & \tan \theta \\ -\tan \theta & 1 \end{bmatrix}^{-1} = \begin{bmatrix} a & -b \\ b & a \end{bmatrix}$$

$$\begin{bmatrix} 1 & -\tan \theta \\ \tan \theta & 1 \end{bmatrix} = \begin{bmatrix} a & -b \\ b & a \end{bmatrix}$$

$$\Rightarrow \frac{1}{1 + \tan^{2}\theta} \begin{bmatrix} 1 - \tan^{2}\theta & -2\tan \theta \\ 2\tan \theta & 1 - \tan^{2}\theta \end{bmatrix} = \begin{bmatrix} a & -b \\ b & a \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} \cos 2\theta & -\sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{bmatrix} = \begin{bmatrix} a & -b \\ b & a \end{bmatrix}$$

$$\therefore \qquad a = \cos 2\theta, b = \sin 2\theta$$

$$\begin{bmatrix} 1 & 2 \end{bmatrix}$$

156. (c) We have,
$$A = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$

$$A^{2} = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1+0 & 2+2 \\ 0+0 & 0+1 \end{bmatrix} = \begin{bmatrix} 1 & 4 \\ 0 & 1 \end{bmatrix}$$

$$A^{3} = A^{2} \times A \begin{bmatrix} 1 & 4 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1+0 & 2+4 \\ 0+0 & 0+1 \end{bmatrix} = \begin{bmatrix} 1 & 6 \\ 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} 1 & 2\times3 \\ 0 & 1 \end{bmatrix}$$

$$A^{n} = \begin{bmatrix} 1 & 2n \\ 0 & 1 \end{bmatrix}$$

157. (b) We have, α , β and γ are roots of equation

$$x^{3} + px + q = 0$$
Here, $\alpha + \beta + \gamma = 0$

$$\alpha\beta + \beta\gamma + \gamma\alpha = p$$

$$\alpha\beta\gamma = -q$$
Applying $C_{1} \rightarrow C_{1} + C_{2} + C_{3}$, we get
$$\begin{vmatrix} \alpha + \beta + \lambda & \beta & \gamma \\ \alpha + \beta + \lambda & \gamma & \alpha \\ \alpha + \beta + \lambda & \alpha & \beta \end{vmatrix} = (\alpha + \beta + \lambda)\begin{vmatrix} 1 & \beta & \gamma \\ 1 & \gamma & \alpha \\ 1 & \alpha & \beta \end{vmatrix}$$

Applying
$$R_2 o R_2 - R_1$$
, $R_3 o R_3 - R_1$, we get
$$(\alpha + \beta + \lambda) \begin{vmatrix} 1 & \beta & \gamma \\ 0 & \gamma - \beta & \alpha - \gamma \\ 0 & \alpha - \beta & \beta - \gamma \end{vmatrix}$$

$$= (\alpha + \beta + \lambda)[(\gamma - \beta)(\beta - \gamma) - (\alpha - \gamma)(\alpha - \beta)]$$

$$= 0 \times [(\gamma - \beta)(\beta - \gamma) - (\alpha - \gamma)(\alpha - \beta)] = 0$$

$$|\sin x \cos x \cos x|$$

$$|\cos x \sin x \cos x|$$

$$|\cos x \sin x \cos x|$$

$$|\cos x \cos x \sin x|$$

$$|\cos x \cos x \sin x|$$

$$|\cos x \cos x|$$

$$|\cos x \cos x \sin x|$$

$$|\cos x \cos x|$$

$$|2\cos x + \sin x \cos x \cos x|$$

$$|2\cos x + \sin x \cos x \cos x|$$

$$|2\cos x + \sin x \cos x \cos x|$$

$$|1 \cos x \cos x|$$

$$|2 \cos x + \sin x|$$

$$|1 \cos x \cos x|$$

$$|1 \cos x \cos x|$$

$$|2 \cos x + \sin x|$$

$$|1 \cos x \cos x|$$

$$|1 \cos x \cos$$

$$\begin{vmatrix} 0 & 0 & \sin x - \cos x \\ \Rightarrow (2\cos x + \sin x)[1 \cdot (\sin - \cos x)^2] = 0 \\ \Rightarrow (2\cos x + \sin x)(\sin x - \cos x)^2 = 0 \\ \Rightarrow 2\cos x = -\sin x \text{ or } \sin x = \cos x \\ \Rightarrow \tan x = -2 \text{ which is not possible as for } \\ -\frac{\pi}{4} \le x \le \frac{\pi}{4}, \text{ we get } -1 \le \tan x \le 1 \\ \text{or } \tan x = 1 \\ \text{So, } x = \frac{\pi}{4}. \text{ Hence, only one real root exist.}$$

159. (c) Prime factors of 450 is $2 \times 3 \times 3 \times 5 \times 5$.

Now, non-prime divisors will be combinations of these.

When two are multiplied,

...(i)

$$2 \times 3 = 6, 2 \times 5 = 10$$

 $3 \times 3 = 9, 3 \times 5 = 15, 5 \times 5 = 25$
When three are multiplied,
 $2 \times 3 \times 3 = 18, 2 \times 3 \times 5 = 30, 2 \times 5 \times 5 \times 50,$
 $3 \times 3 \times 5 = 45, 3 \times 5 \times 5 = 75$

When four are multiplied,

$$2 \times 3 \times 3 \times 5 = 90, 2 \times 3 \times 5 \times 5 = 150,$$

 $3 \times 3 \times 5 \times 5 = 225$

When five are multiplied,

$$2 \times 3 \times 3 \times 5 \times 5 = 450$$

Also, 1 is also a non-prime divisor.

So, sum of divisors

$$= 9 + 15 + 25 + 30 + 50 + 45 + 75 + 90$$

 $+150 + 225 + 450 + 1 = 1199$

160. (a)
$$\sum_{\substack{1$$

After 5! the number will have 0 at the one's place.

So, they will no effect the last digit of the total sum.

Now last digit of (2! + 3!) = 2 + 6 = 8

Last digit of (2! + 4!) = 2 + 4 = 6

Last digit of
$$\sum_{\substack{1$$

161. (b) Let
$$I = \int_{0}^{1} \frac{1}{\sqrt{1+x^4}} dx$$

We have,
$$0 \le x \le 1$$

$$0 \le x^4 \le 1$$

$$\Rightarrow$$
 $1 \le 1 + x^4 \le 2$

$$\Rightarrow$$
 $1 \le \sqrt{1 + x^4} \le \sqrt{2}$

$$\Rightarrow \frac{1}{\sqrt{2}} \le \frac{1}{\sqrt{1+x^4}} \le 1$$

$$\Rightarrow \int_{0}^{1} \frac{1}{\sqrt{2}} dx \int_{0}^{1} \frac{1}{\sqrt{1 + e^{4}}} dx \le \int_{0}^{1} 1 dx$$

$$\Rightarrow \frac{1}{\sqrt{2}} \le \int_0^1 \frac{1}{\sqrt{1+x^4}} dx \le 1$$

$$\therefore I \in \left[\frac{1}{\sqrt{2}}, 1\right]$$

162. (b) Let
$$I = \int_{-\pi/2}^{\pi/2} \log(\tan x) dx$$

$$\Rightarrow I = \int_{0}^{\pi/2} \log \tan \left(\frac{\pi}{2} - x \right) dx$$

$$\Rightarrow I = \int_{1}^{\pi/2} \log \cot x \, dx$$

$$\Rightarrow I = \int_{0}^{\pi/2} \log \frac{1}{\tan x} dx$$

$$\Rightarrow I = -\int_{0}^{\pi/2} \log \tan x \, dx$$

$$\rightarrow I = -I \rightarrow 2I = 0 \rightarrow I = 0$$

163. (b) Let
$$I = \int_{-2}^{2} (ax^3 + bx + c)dx$$
 ...(i)

$$= \int_{-2}^{2} (a(-2+2-x)^3 + b(-2+2)x + c)dx$$

$$\left[\because \int_a^b f(x)dx = \int_a^b f(a+b-x)dx\right]$$

$$I = \int_{-a}^2 (-ax^3 - bx + c)dx \qquad ...(ii)$$

$$2I = \int_{-2}^{2} 2c \, dx$$

$$I = 4c$$

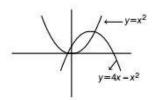
So, value of I depends on the value of c.

164. (b) Given equation of curves are $y = x^2$ and

$$y = 4x - x^2$$

$$y - 4 = -4 + 4x - x^2$$

$$y-4 = -(x^2-4x+4) = -(x-2)^2$$



Now, required area =
$$\int_{1}^{2} \{(4x - x^{2}) - x^{2}\} dx$$

$$= \int_{0}^{2} \{ (4x - 2x^{2}) dx$$

$$= \left[2x^2 - \frac{2}{3}x^3\right]_0^2$$

$$= \left\lceil \left(8 - \frac{16}{3} \right) - 0 \right\rceil$$

$$=\frac{24-16}{3}=\frac{8}{3}$$
 sq. units

165. (b) We have,
$$\frac{y}{x} \frac{dy}{dx} = \frac{1+y^2}{1+x^2}$$

$$\frac{y\,dy}{1+y^2} = \frac{x\,dx}{1+x^2}$$

$$\frac{2y\,dy}{1+u^2} = \frac{2x\,dx}{1+x^2}$$

Integrating both sides, we get

$$\int \frac{2y \, dy}{1 + y^2} = \int \frac{2x \, dx}{1 + x^2}$$

$$\ln(1+y^2) = \ln(1+x^2) + \ln c$$
$$1+y^2 = c(1+x^2)$$

Now,
$$y = 2$$
 at $x = 1$

So,
$$5 = c(2)$$

$$2c = 5$$

Therefore, $2(1+y^2) = 5(1+x^2)$

166. (d) We have,

$$\frac{dy}{dx} = (x+y)^2$$

Let
$$x + y = x$$

$$\Rightarrow \frac{dy}{dx} + 1 = \frac{dz}{dx} \Rightarrow \frac{dy}{dx} = \frac{dz}{dx} - 1$$

Now, given equation becomes

$$\frac{dz}{dx} - 1 = z^2 \implies \frac{dz}{dx} = 1 + z^2$$

$$dx = \frac{dz}{1 + z^2}$$

On integrating both sides, we get

$$\int dx = \int \frac{dz}{1+z^2}$$

$$\Rightarrow$$
 $c + x = \tan^{-1}(z)$

$$\Rightarrow$$
 $\tan^{-1} z = x + c$

$$\Rightarrow$$
 $\tan^{-1}(x+y) = x+c$

167. (a) Let
$$f(x) = \left(\frac{1}{x}\right)^{2x^2} = x^{-2x^2}$$

$$\log f(x) = -2x^2 \log x$$

$$\Rightarrow \frac{1}{f(x)}f'(x) = -4x\log x - \frac{2x^2}{x}$$

$$\Rightarrow f'(x) = x^{-2x^2} \quad [-4x \log x - 2x]$$

For maximum,

$$f'(x) = 0$$

$$\Rightarrow x^{-2x^2}[-4x\log x - 2x] = 0$$

$$\Rightarrow$$
 $-4x \log x - 2x = 0$

$$\Rightarrow \log x = -\frac{1}{2}$$

$$\Rightarrow$$
 $x = e^{-\frac{1}{2}}$

Again,
$$f''(x) = x^{-2x^2} [-4x \log x - 2x]^2$$

$$+x^{-2x^2}[-4\log x-4-2]$$

$$f''(e^{-\frac{1}{2}}) < 0$$

So, f(x) has maximum value at $x = e^{-\frac{1}{2}}$

$$\therefore \quad f_{\text{max}} = f(e^{-\frac{1}{2}}) = \left(\frac{1}{\frac{1}{\sqrt{e}}}\right)^{2\left(\frac{1}{\sqrt{e}}\right)^{2}} = (\sqrt{e})^{2\left(\frac{1}{e}\right)} = e^{1/e}$$

168. (a) Let the required numbers be x. Then,

$$f(x) = x - x^2$$

$$\Rightarrow f'(x) = 1 - 2x$$

For a local maxima or local minima, we must have

$$f'(x) = 0$$

$$\Rightarrow$$
 1 - 2x = 0

$$\Rightarrow$$
 $2x = 1 \Rightarrow x = \frac{1}{2}$

Now,
$$f''(x) = -2 < 0$$

So, $x = \frac{1}{2}$ is point of local maxima.

Hence, required numbers is $\frac{1}{2}$.

169. (c) Given, curve is
$$y = x \sin x$$
 ...(i)

At
$$x = \frac{\pi}{2}$$
, we have $y = \frac{\pi}{2}$

Slope of the tangent at $x = \frac{\pi}{2}$

From Eq. (i), we get

$$\frac{dy}{dx} = \sin x + x \cos x$$

$$\Rightarrow \frac{dy}{dr} = 1 \text{ at } \frac{\pi}{2}$$

Now, equation of tangent will be

$$x - \frac{\pi}{2} = y - \frac{\pi}{2}$$

$$\Rightarrow$$
 $x = y$

This will intersect X-axis at (0, 0).

So, the subtangent will be $=\frac{\pi}{2}-0=\frac{\pi}{2}$

170. (a) Let
$$I = \int \frac{10^{x/2}}{\sqrt{10^{-x} - 10^{x}}} dx$$

$$= \int \frac{10^{x/2}}{\sqrt{\frac{1}{10^{x}} - 10^{x}}} dx = \int \frac{10^{x/2} \cdot 10^{x/2}}{\sqrt{1 - (10^{x})^{2}}} dx$$

$$= \int \frac{10^{x}}{\sqrt{1 - (10^{x})^{2}}} dx$$

Put
$$10^x = t \Rightarrow 10^x \log 10 dx = dt$$

So,
$$I = \frac{1}{\log 10} \int \frac{dt}{\sqrt{1 - t^2}}$$

= $\frac{1}{\log 10} \sin^{-1}(t) + c = \frac{1}{\log 10} \sin^{-1}(10^x) + c$

$$\int e^x \left\{ \frac{1 + \sin x \cos x}{\cos^2 x} \right\} dx$$

$$= \int e^x \left\{ \frac{1}{\cos^2 x} + \frac{\sin x \cos x}{\cos^2 x} \right\} dx$$

$$= \int e^x (\sec^2 + \tan x) dx = \int e^x \{f'(x) + f(x)\} dx$$
[where $f(x) = \tan x$ and $f'(x) = \sec^2 x$]
$$= e^x f(x) + c = e^x \tan x + c$$

172. (d) We have,
$$\int \frac{x^2+1}{x^4+1} dx$$

Divide numerator and denominator by x^2 , we get

$$\int \frac{1 + \frac{1}{x^2}}{x^2 + \frac{1}{x^2}} dx = \int \frac{1 + \frac{1}{x^2}}{x^2 + \frac{1}{x^2} - 2 + 2} dx$$
$$= \int \frac{1 + \frac{1}{x^2}}{\left(x - \frac{1}{x}\right)^2 + 2} dx$$

Let
$$x - \frac{1}{x} = t$$

$$\left(1 + \frac{1}{x^2}\right) dx = dt = \int \frac{dx}{t^2 + 2}$$

$$= \frac{1}{\sqrt{2}} \tan^{-1} \left(\frac{t}{\sqrt{2}}\right) + c$$

$$= \frac{1}{\sqrt{2}} \tan^{-1} \left(\frac{x - \frac{1}{x}}{\sqrt{2}}\right) + c$$

$$= \frac{1}{\sqrt{2}} \tan^{-1} \left(\frac{x^2 - 1}{\sqrt{2}x}\right) + c$$

173. (a) Given, line segment is $x \cos \alpha + y \sin \alpha = p$

Therefore, it cuts the X-axis and Y-axis at points $(p \sec \alpha, 0)$ and $(0, p \csc \alpha)$.

Hence, the coordinate of the mid point are

$$\left(\frac{p\sec\alpha}{2}, \frac{p\csc\alpha}{2}\right)$$

Therefore,
$$x = \frac{p \sec \alpha}{2}$$
 and $y = \frac{p \csc \alpha}{2}$

or
$$\cos \alpha = \frac{p}{2x}$$
 and $\sin \alpha = \frac{p}{2y}$

$$\sin^2 \alpha + \cos^2 \alpha = 1$$

$$\left(\frac{p}{2x}\right)^2 + \left(\frac{p}{2y}\right)^2 = 1$$

$$\Rightarrow \frac{p^2}{4x^2} + \frac{p^2}{4y^2} = 1 \Rightarrow \frac{1}{4x^2} + \frac{1}{4y^2} = \frac{1}{p^2}$$

$$\Rightarrow \frac{1}{x^2} + \frac{1}{y^2} = \frac{4}{p^2} \Rightarrow x^{-2} + y^{-2} = 4p^{-2}$$

174. (c) If the line is inclined at angle 45° with the positive direction of the X-axis i.e. the points are situated at angle $\theta = 45^{\circ}$ from X-axis at a distance $r = 3\sqrt{2}$ from

The two points can be given by

 $(x_0 \pm r \cos \theta, y \pm r \sin \theta)$

The points are

point (4, -5).

$$(4+3\sqrt{2}\cos 45^{\circ}, -5+3\sqrt{2}\sin 45^{\circ})$$

$$=\left(4+3\sqrt{2}\frac{1}{\sqrt{2}},-5+3\sqrt{2}\times\frac{1}{\sqrt{2}}\right)=(7,-2)$$

and
$$(4-3\sqrt{2}\cos 45^\circ, -5-3\sqrt{2}\sin 45^\circ)$$

$$= \left(4 - 3\sqrt{2} \times \frac{1}{\sqrt{2}}, -5 - 3\sqrt{2} \times \frac{1}{\sqrt{2}}\right) = (1, -8)$$

Thus, the points are (1, -8) and (7, -2).

175. (c) The equation $ax^2 + 2hxy + by^2 = 0$ can be rewritten as

$$a + \frac{2hy}{x} + b\left(\frac{y}{x}\right)^2 = 0$$
 ...(i)

Consider, px + qy = 0

$$px = -qy \implies \frac{y}{x} = \frac{-p}{q}$$

Substituting in Eq. (i), we get

$$a+2h\left(-\frac{p}{q}\right)+b\left(\frac{-p}{q}\right)^2=0 \Rightarrow a-\frac{2hp}{q}+b\frac{p^2}{q^2}=0$$

$$\Rightarrow aq^2 - 2hpq + bp^2 = 0$$

176. (b) We have,
$$f(x) = \frac{\log_e(1 + ax) - \log_e(1 - bx)}{x}$$

$$= \lim_{x \to 0} \frac{\log_e(1 + ax) - \log_e(1 - bx)}{x} \qquad \left[\frac{0}{0} \text{ form}\right]$$

Applying L' Hospital rule

$$\lim_{x \to 0} \frac{\frac{a}{1+ax} + \frac{b}{1-bx}}{1} = \frac{\frac{a}{1} + \frac{b}{1}}{1} = a + b$$

177. (b) We have,

$$\lim_{n \to \infty} \frac{(1^2 + 2^2 + \dots + n^2) \sqrt[n]{n}}{(n+1)(n+10)(n+100)}$$

$$= \lim_{n \to \infty} \frac{n(n+1)(2n+n)}{6(n+1)(n+10)(n+100)} \left(\lim_{n \to \infty} \sqrt[n]{n}\right)$$

$$= \lim_{n \to \infty} \frac{2n^2 + n}{6(n+10)(n+100)} \qquad \dots$$

$$= \lim_{n \to \infty} \frac{2 + \frac{1}{n}}{6\left(1 + \frac{10}{n}\right)\left(1 + \frac{100}{n}\right)}$$

$$= \frac{2+0}{6(1+0)(1+0)}$$

$$= \frac{2}{6} = \frac{1}{3}$$

178. (c) Consider that there are m collinear points out of total n points in a plane. To construct a triangle we require 3 non-collinear points.

Hence, the number of triangles will be ${}^{n}C_{3} - {}^{m}C_{3}$.

Since, all the point in the above question are non-collinear, hence n=10 and m=0

Therefore, the total number of triangles are = ${}^{10}C_3$

$$=\frac{10\times9\times8}{3!}=\frac{90\times8}{6}=15\times8=120$$

179. (a) Angle traced by the hour hand in 12 h = 360° Anlge traced by it in 4 h 25 min, i.e.

$$4\frac{5}{12} h = \frac{53}{12} h$$
$$= \frac{360}{12} \times \frac{53}{12} = \frac{265}{2} = 132\frac{1^{\circ}}{2}$$

Angle traced by it in 25 min

$$=\frac{360^{\circ}}{60^{\circ}} \times 25 = 150^{\circ}$$

Now, required angle = $\left(150^{\circ} - 132\frac{1^{\circ}}{2}\right) = 17\frac{1^{\circ}}{2}$

180. (a)
$$x^2 + y^2 - 8x = 0$$

$$\Rightarrow 5^2 + (-7)^2 - 8 \times 5$$

$$\Rightarrow 25 + 49 - 40 = 34$$

$$\Rightarrow 34 > 0$$

Here, 34 > 0, so the points (5, -7) lies outside the