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COMEDK 2016 Question Paper with Solution

Consortium of Medical, Engineering and Dental Colleges of Karnataka
Under Graduate Entrance Test

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SOLVED PAPER – 2016 (COMEDK)

Instructions

. There are 180 questions in all. The number of questions in each section is as given below.

Sections No. of Questions Section I: Physics 1-60 Section II: Chemistry 61-120 Section III: Mathematics 121-180

- · All the questions are Multiple Choice Questions having four options out of which ONLY ONE is correct.
- · Candidates will be awarded 1 mark for each correct answer. There will be no negative marking for incorrect answer.
- Time allotted to complete this paper is 3 hrs.

PHYSICS

1. A simple pendulum has a period *T* inside a lift, when it is stationary. The lift is accelerated upwards with constant acceleration a. The period a. decreases b. increases

c. remains same

- d. becomes infinite
- 2. 90 dB sound is x times more intense than 40 dB sound, then x is

a. 5

b. 50

c. 105

d. 500

3. A star is moving away from the earth with speed v. Change in wavelength dλ observed on earth

a. \u00bbe /c

b. $\lambda v / (c + v)$

 $c. \lambda c/(c+v)$

4. An open pipe emits a fundamental frequency n when it emits the 3rd harmonic, then the pipe can accommodate

a. 2 nodes, 2 anti-nodes

b. 3 nodes, 4 anti-nodes

c. 3 nodes, 3 anti-nodes

d. 1 node, 2 anti-nodes

- In an adiabatic process.
 - a. temperature remains constant
 - b. pressure remains constant
 - c. volume remains constant
 - d. there is no transfer of heat
- 6. Carnot heat engine takes 300 J of heat from a source at 627°C and gives some part of it to sink at 27°C. Work done by engine in one cycle is

a. 200 J

b. 300 J

c. 150 J

7. 15/16th of a radioactive sample disintegrates in 2 h. Mean life of radioactive sample is approximately

a. 30 min

b. 43 min

c. 21 min

d. 15 min

8. Clear images of soft tissues can be well studied using

a. MRI

b. X-rays

c. ultrasonics

d. IR rays

9. Particles which are not composite and hence truly elementary are

a. mesons

b. protons

c. neutrons

d. leptons

	only, when all inp a. AND c. NOR n-type and p-type obtained by dopin with	e output will be in logic 0 state uts are in logic 1 state is called b. OR d. NAND semiconductors can be g pure silicon, respectively	20.	viewed un a. equally central of b. equally central v central v c. a few co	nder white li spaced bright dark spot spaced bright white spot loured rings v	in reflected s ght consists o and dark band and dark band with central dar with central wh	f s with s with k spot
12.		in it in $\beta = 50, R_L = 4 \text{ k}\Omega, R_i = 500\Omega.$	21.	light wave a. light wa b. speed of	es, because ves can travel light is more	e diffraction i through vacuu erse in nature	
	Power gain of the a , 2×10^4 c. 2×10^3	amplifier is $\mathbf{b.}\ 2 \times 10^2$ $\mathbf{d.}\ 2 \times 10^l$	22.	A calcite o		ced over a dot	
	During downward of spectral lines of a. 4 c. 2	ted from $n = 1$ to $n = 4$ state. I transitions, possible number observed in Balmer series is b. 3 d. 1		through the a. a single b. two statics. two dots d. one dot	ne calcite or stationary dot onary dots rotating abou rotating abou	t it one another t the other stati	
14.	IR region lies beto a. radiowaves and n b. microwaves and v c. visible and UV re d. UV rays and X-ra	nicrowave regions risible gion	23.	Critical ar		with it nedium is 45°. he surface of the b. 38° d. 54.7°	
15.	same potential dif	pha particle are subjected to ference V. Their de-Broglie $_{\alpha}$ will be in the ratio $\mathbf{b.}\ 2\sqrt{2}:1$	24.	through a		current is to er of resistanc t should be c. 50 G	
16.	c. 1:1Raman shift depera. incident wavelenb. incident intensity	gth	25.	like a tiny		ng loop of are nagnetic mom	
17.	c . resolving power c d . molecular energy ${}_{6}C^{14}$ and ${}_{7}N^{15}$ are a . isotopes	f the spectrograph used levels of the scatterer	26.	10 turns w currents 0	vith radii 0.2 0.2 A and 0.3	ar coils, each m and 0.4 m A respectivel lagnetic field	carry ly in
18.		experiment, intensity ratio at fringe is 9 : 1. Amplitudes of	27.	a. high retb. low rete	entivity and h ntivity and hi		
19.	fringe occurs direct Wavelength of light		28.	d. high retPower fac	ntivity and loventivity and loventivity and lot tor of a serie	ow coercivity es <i>L-C-R</i> circu	nit is
	a. d^2/D c. D^2/d	b . d / D d . 2d² / D		a. R c. R / Z		b. Z / R d. RZ	

An inductor 1H is connected across 220V, Ideal voltmeter connected as shown reads 50 Hz supply. Peak value of current is approximately a. 0.5 A b. 0.7 A c. 1 A d. 1.4 A Plane polarised light is passed through an analyser and the intensity of emerging light is reduced by 75%. Optical vibrations make an angle θ with the axis of analyser, then θ is b. 45° c. 30° 167 31. A charge 10nC is situated in a medium of a. 16 V b. 12 V relative permittivity 10. The potential due to c. 4 V d. 8 V this charge at a distance of 0.1 m is 40. When a charged particle moves perpendicular a. 900 V b. 90 V to a uniform magnetic field, then c. 9 V d 0 09 V a. its momentum changes and total energy is same Dielectric constant of a metal is b. Both momentum and its total energy remain the b. infinite a. zero c. finite d. unpredictable c. Both momentum and its total energy will change d. total energy changes but momentum remains **33.** Distance between the two point charges is increased by 20%. Force of interaction between the charges 41. 0.04 m of glass contains the same number of a. increases by 10% b. decreases by 20% waves as 0.05 m of water, when monochromatic d. decreases by 31% c. decreases by 17% light passes through them normally. Refractive index of water is 4/3. Refractive index of glass is 34. Potential energy of 2 charge 10 nC each a. 5/3 b. 5/4 c. 5/2 d. 4/5 separated by a distance of 0.09 m in air is a. 10 µJ b. 1 mJ 42. Critical angle will be maximum, when light c. 10 mJ d. 10 J travels from a. glass to air b. glass to water **35.** A metal plate of thickness d / 2 is introduced in c. water to air d. diamond to air between the plates of a parallel plate air capacitor with plate separation of d, then 43. A ray of light incident on one face of an capacity equilateral prism at 60° enters and leaves the a. decreases 2 times b. increases 2 times prism symmetrically. Refractive index of the c. remains same d. becomes zero prism material is a. 1.5 b 169 d. 1.8 c. 1.73 36. Specific resistance of a conductor material increases with **44.** In the spectrum of visible light produced by a a. increase with area of cross-section prism dispersion is b. decrease in length a. uniform throughout the spectrum c. decrease in area of cross-section b. maximum in the middle decreases on either sides d. increases with temperature c. maximum towards yellow maximum towards violet The resistance of mercury at 4.2 K is **45.** Convex lens of focal length f made of glass of b. greater than at lab temperature refractive index 1.5 is immersed in water of c. same as that of lab temperature refractive index 4/3. Focal length is d. almost zero a. f b. greater than f c. less than f d - f38. Temperature coefficient of resistance of platinum is 4×10^{-3} / K at 20°C. Temperature at 46. Two co-axial lenses of power + 4D and - 2D are

placed in contact. The focal length of

b. 0.25 m

d. - 0.5 m

combination is

a. 0.5 m

c. 0.16 m

which increase in resistance of platinum is 10%

b. 70°C

d. 100°C

its value at 20°C is

a. 25°C

c. 45°C

acting at a point is equal to three times their it is a. heated product. Angle between them is a. 30° b. placed in a time varying magnetic field c. 60° d. 90° c. placed in an electric field placed in a uniform magnetic field 55. With the addition of impurities, surface tension 48. Transformer works on 220 V and its efficiency is of a liquid a. increases 80%. If output power is 8 kW, primary current is approximately b. decreases a. 35 A b. 18 A c. remains constant c. 22 A d. 45 A d. may increase or decrease depending on impurities 56. Viscosity decreases with increase in 49. Quality factor of a series L-C-R circuit decreases from 3 to 2. Resonant frequency is temperature is the reason for 600 Hz. Change in bandwidth is (i) hot water moving faster than cold water. b. 100 Hz increase a. zero (ii) more viscous oils are used in motorcars during c. 100 Hz decrease d. 300 Hz increase summer than in winter a. Only (i) is correct b. Only (ii) correct 50. A stone dropped from the top of the tower c. Both are correct d. Both are incorrect reaches ground in 4 s. Height of the tower is $(g = 10 \text{ m} / \text{s}^2)$ 57. Moment of momentum of an electron revolving a. 20 m b. 40 m in second Bohr orbit of hydrogen is c. 60 m d. 80 m a. 2 πh b. h / 2n d. 2h / 3n c. h / n 51. Liquid crystal phase which are more close to the solid than to liquid is 58. The existence of excitation and ionisation a. Nematic b. Smectic energies in an atom is an evidence for c. Lyotropic d. Cholesteric a. stability of an atom b. electrical neutrality of an atom 52. If the earth shrinks in its size (radius) mass c. small size of the atom remaining the same, the value of g on its surface d. stationary orbits in an atom will a. increase b. decrease Work function of a photosensitive metal is 3 eV. c. remains same d. reduce to zero The wavelength of incident radiations which can just eject photoelectrons from the metal is 53. Two rods of same area of cross-section and a. 600 nm **b.** 510 nm lengths and conductivities K_1 and K_2 are c. 414 nm d. 378 nm connected in series. Then in steady state, conductivity of the combination is 60. Three identical capacitors are first connected in series and then in parallel. The ratio of effective $a.(K_1 + K_2)/(K_1K_2)$ **b.** $2K_1K_2/(K_1+K_2)$ capacitances in the two cases is $c.(K_1 + K_2)/2$ a. 9:1 b. 3:1

c. 1:3

54. The square of the resultant of two equal forces

d. 1:9

Eddy currents are produced in a material, when

 $d. K_1 K_2 / (K_1 + K_2)$

CHEMISTRY

01.	oily liquid on heating w potassium hydroxide so product with acetic anh drug was obtained. The	ith bromine and lution. On shaking the ydride, an antipyretic reactions indicate that	 a. anode to cathod b. cathode to anode c. anode to cathode 	e through the external circuit. e through the external circuit. e through the solution. e through the solution.
	the starting compound a. acetamide c. aniline	b. nitrobenzened. benzamide	sodium metal in	dure of two alkyl halides with dry ether, 2-methyl propane e alkyl halides are
62.	The silver salt of a fatty alkyl halide gives an a. ether	acid on refluxing with a	a. chloromethane a b. chloromethane a	
	c. acid	d. ester	d. 2-chloropropane	
63.	Pick out the one which family	does not belong to the	72. Which of the folloride is	owing statements about s incorrect?
	a. ptyalin	b. lipase	a. It is a lachrymat	tory liquid and answers Beilstein's
	c. pepsin	d. cellulose	test.	
64.	reaction. c. Saponification of Cl reaction.		nitrate. c. It is less reactive d. It can be oxidise copper nitrate so r 73. The main product	e precipitate with alcoholic silver e than alkyl halides. ed to benzaldehyde by boiling with olution. et obtained when a solution of e reacts with mercuric
			a. HgCO ₃	b. HgCO ₃ , Hg(OH) ₂
65.	The diameter of colloid a, 10 ³ m to 10 ⁻³ m	al particle ranges from	c. Hg(OH) ₂	d. HgCO ₃ , HgO
	b. 10 ⁻³ m to 10 ⁻⁶ m c. 10 ⁻⁶ m to 10 ⁻⁹ m d. 10 ⁻⁹ m to 10 ⁻¹² m		74. In the electrothe displaced by silic a. phosphorus	rmal process, the compound a from calcium phosphate is b. phosphorus pentoxide
66.	The number of 2p electr	ons having spin quantu	#40	1990 - 19
	number $s = -1/2$ are a. 2 b. 3	c. 6 d. 0	25°C is 890 kJ. T	combustion of methane at he heat liberated when 3.2 g
67.	Pick out the alkane whi	ch differs from the other	a. – 890 kJ	b. 178 kJ
	members of the group.		c. 445 kJ	d. 278 kJ
	a. 2-methyl butane	b. 2, 2-dimethyl butaned. Pentane	Management of Management	TE STATE OF THE ST
68.	ammonia are present. T	of hydrogen gas are l. At equilibrium 34 g of	carbon dioxide gavolume of carbon a. 4 dm³ c. 2 dm³	l temperature of 4 dm ³ of as are doubled. Then, the dioxide gas would be b. 8 dm ³ d. 3 dm ³
	a. 1, 1, 2	b. 2, 1, 2		s dissolved in concentrated
	c. 1, 2, 2	d. 2, 2, 1		opper nitrate solution on we 5g of its oxide. The
69.	A process is taking plac and pressure. Then,		a anni a al anni anni al-	
	\mathbf{a} . $\Delta H = 0$	$b. \ \Delta S = 0$	c. 23	d. 32
	$c. \Delta H = \Delta E$	$d. \Delta H = T\Delta S$		
	AND SERVICE			



- 97. In a mixture of acetic acid and sodium acetate the ratio of concentrations of the salt to the acid is increased ten times. Then the pH of the solution
 - a. decreases ten fold
- b. increases ten fold
- c. increases by one
- d. decreases by one
- 98. When a mixture of methane and oxygen is passed through heated molybdenum oxide, the main product formed is
 - a. methanol
- b. methanal
- c. methanoic acid
- d. ethanal
- **99.** Benzene can be obtained by heating either benzoic acid with *X* or phenol with *Y*. *X* and *Y* are respectively
 - a. zinc dust and sodium hydroxide
 - b. soda lime and copper
 - c. zinc dust and soda lime
 - d. soda lime and zinc dust
- 100. An organic compound is boiled with alcoholic potash. The product is cooled and acidified with HCl. A white solid separates out. The starting compound may be
 - a. ethyl acetate
- b. methyl acetate
- c. ethyl benzoate
- d. ethyl formate
- 101. In qualitative analysis, in order to detect second group basic radical, H₂S gas is passed in the presence of dilute HCl to
 - a. decrease the dissociation of H2S
 - b. increase the dissociation of salt solution
 - c. increase the dissociation of H2S
 - d. decrease the dissociation of salt solution
- 102. Aluminium displaces hydrogen from dilute HCl, whereas silver does not. The emf of a cell prepared by combining Al / Al³⁺ and Ag / Ag⁺ is 2.46 V. The reduction potential of silver electrode is + 0.80 V. The reduction potential of aluminium electrode is
 - a. 3.26 V
- **b.** 1.66V
- c. + 1.66 V
- d. 3.26 V
- 103. The first fraction obtained during the fractionation of petroleum is
 - a. gasoline
- b. diesel oil
- c. hydrocarbon gases
- d. kerosene oil
- 104. Which of the following compounds gives trichloromethane on distilling with bleaching powder?
 - a. Ethanol
- b. Methanol
- c. Methanal
- d. Phenol

- 105. Benzoin is
 - a. α-hydroxy aldehyde
 - b. α-hydroxy ketone
 - c. compound containing an aldehyde and a ketonic group
 - d. α, β- unsaturated acid
- 106. The velocity constant of a reaction at 290 K was found to be 3.2 × 10⁻³ s⁻¹. When the temperature is raised to 310 K, it will be about
 - a. 9.6×10^{-3}
- **b.** 1.28×10^{-2}
- c. 6.4 × 10⁻³
- d. 3.2 × 10⁻⁴
- Select the pK_a value of the strongest acid from the following.
 - a. 2.0
- b. 4.5
- c. 1.0
- **d.** 3.0
- 108. Pick out the unsaturated fatty acid from the following
 - a. oleic acid
- b. palmitic acid
- c. stearic acid
- d. laurie acid
- 109. Nylon is not a
 - a. copolymer
- homopolymer
- ${m c}$. condensation polymer
- d. polyamide
- 110. The coaltar fraction which contains phenol is
 - a. heavy oil
- b. light oil
- c. middle oil
- d. green oil
- 111. The compounds A and B are mixed in equimolar proportion to form the products,
 - $A + B \rightleftharpoons C + D$. At equilibrium, one-third of A and B are consumed. The equilibrium constant for the reaction is
 - a. 2.5
- b. 0.25
- c. 0.5
- d. 4.0
- 112. In froth floatation process for the purification of ores, the particles of ore float because
 - a. they are insoluble
 - b. they bear electrostatic charge
 - c. their surface is not easily wetted by water
 - d. they are light
- 113. Which of the following statements about amorphous solids is incorrect?
 - a. There is no orderly arrangement of particles.
 - b. They are rigid and incompressible.
 - c. They melt over a range of temperature.
 - d. They are anisotropic.
- 114. Hydrogen diffuses six times faster than gas A. The molar mass of gas A is
 - a. 24
- **b.** 36
- c. 72
- d. 6

- 115. Dulong and Petit's law is valid only for
 - a. gaseous elements
- b. solid elements
- c. metals
- d. non-metals
- 116. Identify the gas which is readily adsorbed by activated charcoal
 - a. H2
- b. O. d. SO.
- c. N,
- 117. If the distance between Na and Cl ions in sodium chloride crystal is x pm, the length of the edge of the unit cell is
 - $a \cdot \frac{x}{2}$ pm
- **b.** 2x pm
- c. 4r pm
- $d.\frac{x}{4}$ pm
- 118. Which of the following statements is incorrect?
 - a. In K4[Fe(CN)6] the ligand has satisfied both primary and secondary valencies of ferrous ion.

- b. In [Cu(NH3)4]SO4, the ligand has satisfied only the secondary valency of copper.
- c. In K₃[Fe(CN)₆], the ligand has satisfied only the secondary valency of ferric ion.
- d. In K₃[Fe(CN)₆], the ligand has satisfied both primary and secondary valencies of ferric ion.
- 119. 2-acetoxy benzoic acid is used as an
 - a. antiseptic
 - b. antipyretic
 - c. antimalarial
 - d. antidepressant
- 120. A nucleoside on hydrolysis gives
 - a. an aldopentose and a heterocyclic base
 - b. an aldopentose and orthophosphoric acid
 - c. a heterocyclic base and orthophosphoric acid
 - an aldopentose, a heterocyclic base and orthophosphoric acid

MATHEMATICS

- **121.** If $A = \{a, b, c\}$, $B = \{b, c, d\}$ and $C = \{a, d, c\}$,
 - then $(A B) \times (B \cap C) =$ $a. \{(a, c), (a, d), (b, d)\}$
 - **b.** $\{(c, a), (d, a)\}$
 - $c. \{(a, b), (c, d)\}$
 - $d.\{(a,c),(a,d)\}$
- **122.** The function $f: X \to Y$ defined by $f(x) = \sin x$ is one-one but not onto if X and Y are respectively,
 - $a \cdot \left[\frac{-\pi}{2}, \frac{\pi}{2}\right]$ and [-1, 1] $b \cdot \left[0, \frac{\pi}{2}\right]$ and [-, 1, 1]
 - c. [0, \pi] and [0, 1]
- **123.** If $\log_4 2 + \log_4 4 + \log_4 16 + \log_4 x = 6$, then x =
 - a. 32
- c. 4
- **124.** If $S_n = \frac{1}{6 \cdot 11} + \frac{1}{11 \cdot 16} + \frac{1}{16 \cdot 21} + \dots \text{ to } n \text{ terms,}$

 - then $6S_n = a \cdot \frac{1}{(5n+6)}$
- b. $\frac{(2n-1)}{5n+6}$ d. $\frac{5n-4}{5n+6}$

- 125. The remainder obtained when
 - $(1!)^2 + (2!)^2 + (3!)^2 + \dots + (100!)^2$ is divided by 102 is
 - a. 14
- b. 17
- c. 28
- d. 27

- **126.** If $(p \land \neg r) \rightarrow (\neg p \lor q)$ is false, then the truth values of p, q and r are respectively
 - a. T, F and T
- b. F. T and T
- c. F. F and T
- d. T. F and F
- 127. If α , β and γ are the roots of the equation

$$x^3 - 8x + 8 = 0$$
, then $\Sigma \alpha^2$ and $\Sigma \frac{1}{\alpha \beta}$ are

- respectively is equal to
- a. 16 and 0
- b. 16 and 0
- c. 16 and 8
- d. 0 and 16
- 128. The gcd of 1080 and 675 is
 - a. 125
- b. 225
- c. 135
- d. 145
- **129.** If $a \mid (b + c)$ and $a \mid (b c)$, where $a, b, c \in N$, then
 - $a. c^2 \equiv a^2 \pmod{b^2}$ $b. a^2 \equiv b^2 \pmod{c^2}$

 - $c. a^2 + c^2 = b^2$
 - $d. b^2 \equiv c^2 \pmod{a^2}$
- **130.** If a, b and $c \in N$, which one of the following is not true?
 - $a. a \mid b \text{ and } a \mid c \Rightarrow a \mid b + c$
 - **b.** $a \mid b + c \Rightarrow a \mid b \text{ and } a \mid c$
 - $c. a \mid b \text{ and } b \mid c \Rightarrow a \mid c$
 - d. $a \mid b$ and $a \mid c \Rightarrow a \mid 3b + 2c$

131. If
$$2A + 3B = \begin{bmatrix} 2 & -1 & 4 \\ 3 & 2 & 5 \end{bmatrix}$$
 and
$$A + 2B = \begin{bmatrix} 5 & 0 & 3 \\ 1 & 6 & 2 \end{bmatrix}$$
, then $B = \begin{bmatrix} a & 1 & 2 \\ 1 & 10 & 1 \end{bmatrix}$
$$b \cdot \begin{bmatrix} 8 & 1 & -2 \\ -1 & 10 & -1 \end{bmatrix}$$

$$c \cdot \begin{bmatrix} 8 & 1 & 2 \\ -1 & 10 & -1 \end{bmatrix}$$

$$d \cdot \begin{bmatrix} 8 & -1 & 2 \\ -1 & 10 & -1 \end{bmatrix}$$

132. If $O(A) = 2 \times 3$, $O(B) = 3 \times 2$, and $O(C) = 3 \times 3$. which one of the following is not defined? a. C(A + B')b. C(A+B')'

d.CB + A'

 \mathbf{d} , a + b + ab

- **133.** If $A = \begin{bmatrix} 1 & -3 \\ 2 & k \end{bmatrix}$ and $A^2 4A + 10I = A$, then k = 1**b.** 4 and not 1 a. 1 or 4 c. - 4
- **134.** The value of $\begin{vmatrix} x+y & y+z & z+x \\ x & y & z \\ x-y & y-z & z-x \end{vmatrix} =$
 - a. 0 **b.** $(x + y + z)^3$ c. $2(x+y+z)^3$ **d.** $2(x+y+z)^2$

 $c_* a^2 + b^2$

c. BAC

- 135.On the set Q of all rational numbers the operation * which is both associative and commutative is given by a * b =a. 2a + 3b
- **136.** In the group $G = \{1, 5, 7, 11\}$ under multiplication modulo 12, the solution of $7^{-1} \times (x \times 11) = 5$ is x =
 - c. 1 d. 5
- 137. A subset of the additive group of real numbers which is not a sub group, is a.(0, +)
- c. (Z, +) $d.(\{0\}, +)$ **138.** If $\mathbf{p} = \hat{\mathbf{i}} + \hat{\mathbf{j}}$, $\mathbf{q} = 4\hat{\mathbf{k}} - \hat{\mathbf{j}}$ and $\mathbf{r} = \hat{\mathbf{i}} + \hat{\mathbf{k}}$, then the unit vector in tile direction of 3p + q - 2r is $\mathbf{a} \cdot \hat{\mathbf{i}} + 2\hat{\mathbf{j}} + 2\hat{\mathbf{k}}$ **b.** $\frac{1}{3}(\hat{\mathbf{i}} - 2\hat{\mathbf{j}} + 2\hat{\mathbf{k}})$

c.
$$\frac{1}{3}(\hat{\mathbf{i}} - 2\hat{\mathbf{j}} - 2\hat{\mathbf{k}})$$

d. $\frac{1}{3}(\hat{\mathbf{i}} + 2\hat{\mathbf{j}} + 2\hat{\mathbf{k}})$

- 139. If a and b are the two vectors such that $|\mathbf{a}| = 3\sqrt{3}, |\mathbf{b}| = 4 \text{ and } |\mathbf{a} + \mathbf{b}| = \sqrt{7}, \text{ the angle}$ between a and b is a. 150° b. 30° c. 60° d. 120°
- 140. If a is vector perpendicular to both b and c, then $\mathbf{a} \cdot \mathbf{a} \cdot (\mathbf{b} \times \mathbf{c}) = 0$ $\mathbf{b} \cdot \mathbf{a} \times (\mathbf{b} \times \mathbf{c}) = 0$ $\mathbf{c.} \ \mathbf{a} \times (\mathbf{b} + \mathbf{c}) = 0$ d. a + (b + c) = 0
- 141. If the area of the parallelogram with a and b as two adjacent sides is 15 sq units, then the area of the parallelogram having 3a + 2b and a + 3bas two adjacent sides in sq units is a. 45 b. 75 c. 105 d. 120
- 142. The locus of the point which moves such that the ratio of its distances from two fixed points in the plane is always a constant k(<1) is a. circle b. straight line c. ellipse d. hyperbola
- **143.** If the lines x + 3y 9 = 0, 4x + by 2 = 0 and 2x - y - 4 = 0 are concurrent, then b =a. 0 b. 1 c. 5 d. - 5
- **144.** The lines represented by $ax^2 + 2hxy + by^2 = 0$ are perpendicular to each other if a.h = 0 $b. h^2 = ab$ $d. h^2 = a + b$ c. a + b = 0
- **145.** The equation of the circle having x y 2 = 0and x - y + 2 = 0 as two tangents and x + y = 0 as a diameter is $a. x^2 + y^2 = 1$ **b.** $x^2 + y^2 = 2$ $c. x^2 + y^2 - 2x + 2y - 1 = 0$ $d. x^2 + y^2 + 2x - 2y + 1 = 0$
- 146. If the length of the tangent from any point on the circle $(x-3)^2 + (y+2)^2 = 5r^2$ to the circle $(x-3)^2 + (y+2)^2 = r^2$ is 16 units, then the area between the two circles in sq units is a. 16 π b. 8 m c. 4 π d. 32 π
- **147.** The circles $ax^2 + ay^2 + 2g_1x + 2f_1y + c_1 = 0$ and $bx^2 + by^2 + 2g_2x + 2f_2y + c_2 = 0$ $(a \neq 0 \text{ and } b \neq 0)$ cut orthogonally if $\mathbf{a} \cdot g_1 g_2 + f_1 f_2 = c_1 + c_2$ **b.** $b g_1 g_2 + a f_1 f_2 = b c_1 + a c_2$ $\mathbf{c}.\ g_1g_2 + f_1f_2 = b\ c_1 + a\ c_2$ **d.** $g_1g_2 + f_1f_2 = a c_1 + b c_2$

148.	The equation of the common tangent of the two
	touching circles, $y^2 + x^2 - 6x - 12y + 37 = 0$ and
	$x^2 + y^2 - 6y + 7 = 0$ is

$$\boldsymbol{a.}\;\boldsymbol{x}+\boldsymbol{y}+\boldsymbol{5}=0$$

b.
$$x + y - 5 = 0$$

$$c. x - y + 5 = 0$$

$$d. x - y - 5 = 0$$

149. The equation of the parabola with vertex at (-1, 1) and focus (2, 1) is

$$a. y^2 - 2y - 12x + 13 = 0$$

b.
$$y^2 - 2y - 12x + 11 = 0$$

$$c. x^2 + 2x - 12y + 13 = 0$$

$$c. x + 2x - 12y + 13 = 0$$

 $d. y^2 - 2y - 12x - 11 = 0$

150. The equation of the line which is tangent to both the circle
$$x^2 + y^2 = 5$$
 and the parabola $y^2 = 40x$ is

$$a. 2x + y + 5 = 0$$

b.
$$2x - y - 5 = 0$$

$$c. 2x - y + 5 = 0$$

d.
$$2x - y \pm 5 = 0$$

151.
$$x = 4(1 + \cos \theta)$$
 and $y = 3(1 + \sin \theta)$ are the parametric equations of

a.
$$\frac{(x-4)^2}{16} + \frac{(y-3)^2}{9} = 1$$

b. $\frac{(x-4)^2}{16} - \frac{(y-3)^2}{9} = 1$

b.
$$\frac{(x-4)^2}{16} - \frac{(y-3)^2}{9} = 1$$

$$c \cdot \frac{(x+4)^2}{16} + \frac{(y+3)^2}{9} = 1$$

$$d. \frac{(x-3)^2}{9} + \frac{(y-4)^2}{16} = 1$$

152. If the distance between the foci and the distance between the directrices of the hyperbola

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$
 are in the ratio 3:2, then $a:b$ is

a.
$$2:1$$

c. $\sqrt{3}:\sqrt{2}$

c.
$$\sqrt{3}:\sqrt{2}$$
 d. $\sqrt{2}$

153.The ellipse $\frac{x^2}{25} + \frac{y^2}{16} = 1$ and the hyperbola

$$\frac{x^2}{25} - \frac{y^2}{16} = 1$$
 have in common

- a. centre and vertices only
- b. centre, foci and vertices
- c. centre, foci and directrices
- d. centre only

154. If $\sec \theta = m$ and $\tan \theta = n$, then

$$\frac{1}{m}\bigg[(m+n)+\frac{1}{(m+n)}\bigg]=$$

155. The value of
$$\frac{\sin 85^{\circ} - \sin 15^{\circ}}{\cos 65^{\circ}} =$$

a. 0 **b.** 1 **c.** -1

156. From an aeroplane flying, vertically above a horizontal road, the angles of depression of two consecutive stones on the same side of the aeroplane are observed to be 30° and 60° respectively. The height at which the aeroplane is flying in km, is

b.
$$\frac{2}{\sqrt{3}}$$
 c. $\frac{\sqrt{3}}{2}$ **d.** $\frac{4}{\sqrt{3}}$

$$d. \frac{4}{\sqrt{3}}$$

157. If the angles of a triangle are in the ratio 3:4:5, then the sides are in the ratio

b. 2:
$$\sqrt{3}$$
: $\sqrt{3}$ + 1

c.
$$\sqrt{2}: \sqrt{6}: \sqrt{3}+1$$

d. 2:
$$\sqrt{6}$$
: $\sqrt{3}$ + 1

158. If
$$\cos^{-1} x = \alpha$$
, $(0 < x < 1)$ and

sin⁻¹
$$(2x\sqrt{1-x^2}) + \sec^{-1}\left(\frac{1}{2x^2-1}\right) = \frac{2\pi}{3}$$
, then

$$\tan^{-1}(2x) =$$
 $a.\frac{\pi}{2}$
 $b.\frac{\pi}{3}$
 $c.\frac{\pi}{4}$
 $d.\frac{\pi}{6}$

$$c.\frac{\pi}{4}$$

$$d.\frac{\pi}{6}$$

159. If a > b > 0, then the value of

$$\tan^{-1}\left(\frac{a}{b}\right) + \tan^{-1}\left(\frac{a+b}{a-b}\right)$$
 depends on

c. b and not a

d. both a and b

160. Which one of the following equations has no solution?

$$a \cdot \sqrt{3} \sin \theta - \cos \theta = 2$$

b.
$$\cos \theta + \sin \theta = \sqrt{2}$$

$$c$$
. $\csc \theta \cdot \sec \theta = 1$

$$d$$
. $cosec \theta - sec \theta = cosec \theta \cdot sec \theta$

161. The complex number
$$\frac{(-\sqrt{3}+3i)(1-i)}{(3+\sqrt{3}i)(i)(\sqrt{3}+\sqrt{3}i)}$$

when represented in the Argand diagram lies

- a. on the X-axis (Real axis)
- b. on the Y-axis (Imaginary axis)
- c. in the first quadrant
- d. in the second quadrant

162. If
$$2x = -1 + \sqrt{3}i$$
, then the value of

$$(1-x^2+x)^6-(1-x+x^2)^6=$$

163. The modulus and amplitude of $(1 + i\sqrt{3})^8$ are

d. 32

respectively
a. 256 and
$$\frac{8\pi}{3}$$

b. 2 and $\frac{2\pi}{3}$
c. 256 and $\frac{2\pi}{3}$
d. 256 and $\frac{\pi}{3}$

c. 256 and
$$\frac{2\pi}{3}$$

d. 256 and
$$\frac{\pi}{3}$$

164. The value of
$$\lim_{x\to 0} \frac{5^x - 5^{-x}}{2x} =$$

a. If a function
$$f(x)$$
 is continuous at $x = a$, then $\lim_{x \to a} f(x)$ exists.

b. If
$$f(x)$$
 and $g(x)$ are differentiable at $x = a$, then $f(x) + g(x)$ is also differentiable at $x = a$.

c. If
$$f(x)$$
 is continuous at $x = a$, then it is differentiable at $x = a$.

d. If
$$f(x)$$
 is not continuous at $x = a$, then it is not differentiable at $x = a$.

166. If
$$y = 1 + \frac{1}{x} + \frac{1}{x^2} + \frac{1}{x^3} + \dots \infty$$
 with $|x| > 1$, then

$$\frac{dy}{dx} =$$

a.
$$\frac{-y^2}{x^2}$$
 b. $\frac{y^2}{x^2}$ c. x^2y^2 d. $\frac{x^2}{y^2}$

$$b.\frac{y^2}{r^2}$$

$$c. x^2y^2$$

$$d. \frac{x^2}{u^2}$$

167. If
$$f(x)$$
 and $g(x)$ are two functions with

$$g(x) = x - \frac{1}{x}$$
 and $fog(x) = x^3 - \frac{1}{x^3}$, then $f'(x) =$

$$a. 3x^2 + \frac{3}{x^4}$$

b.
$$1 + \frac{1}{r^2}$$

$$c. x^2 - \frac{1}{x^2}$$

d.
$$3x^2 - 3$$

168. The derivative of
$$a^{\sec x}$$
 w.r.t. $a^{\tan x}(a > 0)$ is
a. $a^{\sec x - \tan x}$ **b.** $\sin x a^{\sec x - \tan x}$
c. $\sin x a^{\tan x - \sec x}$ **d.** $\sec x a^{\sec x - \tan x}$

169. If
$$\sin(x+y) + \cos(x+y) = \log(x+y)$$
, then $\frac{d^2y}{dx^2} =$

$$d.\frac{-y}{x}$$

170. If
$$f(x)$$
 is a function such that $f''(x) + f(x) = 0$ and $g(x) = [f(x)]^2 + [f'(x)]^2$ and $g(3) + 8$, then

$$g(8) = a.8$$

171. If the curve
$$y = 2x^3 + ax^2 + bx + c$$
 passes through the origin and the tangents drawn to it at $x = -1$ and $x = 2$ are parallel to the *X*-axis, then the values of a , b and c are respectively,

$$c. - 3, -12$$
 and 0

173. The tangent and the normal drawn to the curve
$$y = x^2 - x + 4$$
 at $P(1, 4)$ cut the X-axis at A and B respectively. If the length of the subtangent drawn to the curve at P is equal to the length of the subnormal, then the area of the ΔPAB in square units is,

174.
$$\int \frac{(x^3 + 3x^2 + 3x + 1)}{(x+1)^5} dx =$$

$$b. \log(x+1) + c$$

$$c. \frac{1}{\pi} \log(x+1) + c$$

a.
$$\tan^{-1} x + c$$

b. $\log(x+1) + c$
c. $\frac{1}{5} \log(x+1) + c$
d. $-\frac{1}{(x+1)} + c$

$$175. \int \frac{\csc x}{\cos^2 \left(1 + \log \tan \frac{x}{2}\right)} dx =$$

$$a - \tan[1 + \log \tan x / 2] + c$$

b.
$$\sec^2[1 + \log \tan x/2] + c$$

c.
$$tan[1 + log tan x/2] + c$$

d.
$$\sin^2[1 + \log \tan x/2] + c$$

176.
$$\int \frac{dx}{x\sqrt{x^6 - 16}}$$

$$a \cdot \sec^{-1}\left(\frac{x^3}{4}\right) + a$$

a.
$$\sec^{-1}\left(\frac{x^3}{4}\right) + c$$
 b. $\frac{1}{12}\sec^{-1}\left(\frac{x^3}{4}\right) + c$

$$c \cdot \cosh^{-1}\left(\frac{x^3}{4}\right) + c$$

c.
$$\cosh^{-1}\left(\frac{x^3}{4}\right) + c$$
 d. $\frac{1}{3}\sec^{-1}\left(\frac{x^3}{4}\right) + c$

177. If
$$I_1 = \int_0^{\pi/2} x \sin x \ dx$$
 and $I_2 = \int_0^{\pi/2} x \cos x \ dx$, then

which one of the following is true?

$$a. I_1 = I$$

b.
$$I_1 + I_2 = 0$$

$$c. I_1 = \frac{\pi}{2} I_2$$

$$d. I_1 + I_2 = \frac{\pi}{2}$$

178. If
$$f(x)$$
 is defined in $[-2, 2]$ by $f(x) = 4x^2 - 3x + 1$

and
$$g(x) = \frac{f(-x) - f(x)}{(x^2 + 3)}$$
, then $\int_{-\infty}^{2} g(x) dx =$

$$c. - 48$$

179. The area enclosed between the parabola
$$y = x^2 - x + 2$$
 and the line $y = x + 2$ in sq units =

$$a.\frac{4}{3}$$
 $b.\frac{2}{3}$

b.
$$\frac{2}{3}$$

$$c.\frac{1}{3}$$

d.
$$\frac{8}{3}$$

180. The solution of the differential equation
$$e^{-x}(y+1) dy + (\cos^2 x - \sin 2x)y(dx) = 0$$
 subjected to the condition that $y = 1$, when $x = 0$ is

$$a.(y+1) + e^x \cos^2 x = 2$$

$$b. y + \log y = e^x \cos^2 x$$

$$c. \log(y+1) + e^x \cos^2 x = 1$$

$$d. y + \log y + e^x \cos^2 x = 2$$

ANSWERS

Physics

2. (c)	3. (a)	4. (b)	5. (d)	6. (a)	7. (b)	8. (a)	9. (d)	10. (d)
12. (a)	13. (c)	14. (b)	15. (b)	16. (a)	17. (c)	18. (c)	19. (a)	20. (a)
22. (d)	23. (d)	24. (b)	25. (d)	26. (b)	27. (a)	28. (c)	29. (c)	30. (c)
32. (b)	33. (d)	34. (a)	35. (b)	36. (d)	37. (d)	38. (c)	39. (d)	40. (a)
42. (b)	43. (c)	44. (d)	45. (b)	46. (a)	47. (b)	48. (d)	49. (b)	50. (d)
52. (a)	53. (b)	54. (c)	55. (d)	56. (c)	57. (c)	58. (a)	59. (c)	60. (d)
62. (d)	63. (d)	64. (b)	65. (c)	66. (b)	67. (b)	68. (a)	69. (a)	70. (a)
72. (c)	73. (d)	74. (b)	75. (b)	76. (a)	77. (d)	78. (c)	79. (d)	80. (c)
82. (c)	83. (c)	84. (c)	85. (d)	86. (d)	87. (d)	88. (a)	89. (d)	90. (b)
92. (b)	93. (c)	94. (d)	95. (b)	96. (b)	97. (c)	98. (b)	99. (d)	100. (c)
102. (b)	103. (c)	104. (a)	105. (b)	106. (b)	107. (c)	108. (a)	109. (b)	110. (c)
	12. (a) 22. (d) 32. (b) 42. (b) 52. (a) 1Ty 62. (d) 72. (c) 82. (c) 92. (b)	12. (a) 13. (c) 22. (d) 23. (d) 32. (b) 33. (d) 42. (b) 43. (c) 52. (a) 53. (b) Try 62. (d) 63. (d) 72. (c) 73. (d) 82. (c) 83. (c) 92. (b) 93. (c)	12. (a) 13. (c) 14. (b) 22. (d) 23. (d) 24. (b) 32. (b) 33. (d) 34. (a) 42. (b) 43. (c) 44. (d) 52. (a) 53. (b) 54. (c) try 62. (d) 63. (d) 64. (b) 72. (c) 73. (d) 74. (b) 82. (c) 83. (c) 84. (c) 92. (b) 93. (c) 94. (d)	12. (a) 13. (c) 14. (b) 15. (b) 22. (d) 23. (d) 24. (b) 25. (d) 32. (b) 33. (d) 34. (a) 35. (b) 42. (b) 43. (c) 44. (d) 45. (b) 52. (a) 53. (b) 54. (c) 55. (d) try 62. (d) 63. (d) 64. (b) 65. (c) 72. (c) 73. (d) 74. (b) 75. (b) 82. (c) 83. (c) 84. (c) 85. (d) 92. (b) 93. (c) 94. (d) 95. (b)	12. (a) 13. (c) 14. (b) 15. (b) 16. (a) 22. (d) 23. (d) 24. (b) 25. (d) 26. (b) 32. (b) 33. (d) 34. (a) 35. (b) 36. (d) 42. (b) 43. (c) 44. (d) 45. (b) 46. (a) 52. (a) 53. (b) 54. (c) 55. (d) 56. (c) try 62. (d) 63. (d) 64. (b) 65. (c) 66. (b) 72. (c) 73. (d) 74. (b) 75. (b) 76. (a) 82. (c) 83. (c) 84. (c) 85. (d) 86. (d) 92. (b) 93. (c) 94. (d) 95. (b) 96. (b)	12. (a) 13. (c) 14. (b) 15. (b) 16. (a) 17. (c) 22. (d) 23. (d) 24. (b) 25. (d) 26. (b) 27. (a) 32. (b) 33. (d) 34. (a) 35. (b) 36. (d) 37. (d) 42. (b) 43. (c) 44. (d) 45. (b) 46. (a) 47. (b) 52. (a) 53. (b) 54. (c) 55. (d) 56. (c) 57. (c) try 62. (d) 63. (d) 64. (b) 65. (c) 66. (b) 67. (b) 72. (c) 73. (d) 74. (b) 75. (b) 76. (a) 77. (d) 82. (c) 83. (c) 84. (c) 85. (d) 86. (d) 87. (d) 92. (b) 93. (c) 94. (d) 95. (b) 96. (b) 97. (c)	12. (a) 13. (c) 14. (b) 15. (b) 16. (a) 17. (c) 18. (c) 22. (d) 23. (d) 24. (b) 25. (d) 26. (b) 27. (a) 28. (c) 32. (b) 33. (d) 34. (a) 35. (b) 36. (d) 37. (d) 38. (c) 42. (b) 43. (c) 44. (d) 45. (b) 46. (a) 47. (b) 48. (d) 52. (a) 53. (b) 54. (c) 55. (d) 56. (c) 57. (c) 58. (a) 1Try 62. (d) 63. (d) 64. (b) 65. (c) 66. (b) 67. (b) 68. (a) 72. (c) 73. (d) 74. (b) 75. (b) 76. (a) 77. (d) 78. (c) 82. (c) 83. (c) 84. (c) 85. (d) 86. (d) 87. (d) 88. (a) 92. (b) 93. (c) 94. (d) 95. (b) 96. (b) 97. (c) 98. (b)	12. (a) 13. (c) 14. (b) 15. (b) 16. (a) 17. (c) 18. (c) 19. (a) 22. (d) 23. (d) 24. (b) 25. (d) 26. (b) 27. (a) 28. (c) 29. (c) 32. (b) 33. (d) 34. (a) 35. (b) 36. (d) 37. (d) 38. (c) 39. (d) 42. (b) 43. (c) 44. (d) 45. (b) 46. (a) 47. (b) 48. (d) 49. (b) 52. (a) 53. (b) 54. (c) 55. (d) 56. (c) 57. (c) 58. (a) 59. (c) Try 62. (d) 63. (d) 64. (b) 65. (c) 66. (b) 67. (b) 68. (a) 69. (a) 72. (c) 73. (d) 74. (b) 75. (b) 76. (a) 77. (d) 78. (c) 79. (d) 82. (c) 83. (c) 84. (c) 85. (d) 86. (d) 87. (d) 88. (a) 89. (d) 92. (b) 93. (c) 94. (d) 95. (b) 96. (b) 97. (c) 98. (b) 99. (d)

Mathematics

112. (c)

113. (d)

114. (c)

111. (b)

121. (d)	122. (b)	123. (a)	124. (c)	125. (b)	126. (d)	127. (a)	128. (c)	129. (d)	130. (c)
131. (c)	132. (a)	133. (a)	134. (a)	135. (d)	136. (c)	137. (b)	138. (d)	139. (a)	140. (b)
141. (c)	142. (c)	143. (d)	144. (c)	145. (b)	146. (*)	147. (*)	148. (d)	149. (d)	150. (a)
151. (a)	152. (d)	153. (a)	154. (d)	155. (b)	156. (c)	157. (d)	158. (b)	159. (a)	160. (c)
161. (b)	162. (a)	163. (c)	164. (d)	165. (c)	166. (a)	167. (*)	168. (b)	169. (c)	170. (a)
171. (c)	172. (b)	173. (a)	174. (d)	175. (c)	176. (b)	177. (d)	178. (b)	179. (a)	180. (d)

116. (d)

117. (b)

118. (d)

119. (b)

120. (a)

115. (b)

Note (*) None of the option is correct.

HINTS & SOLUTIONS

Physics

1. (a) The time period of a pendulum is given by

$$T = \frac{1}{2\pi} \sqrt{\frac{l}{g}}$$

When a lift containing a simple pendulum is accelerated upwards with acceleration a, then its time period becomes

$$T' = \frac{1}{2\pi} \sqrt{\frac{l}{(g+a)}}$$

Clearly, $T' \angle T$

Hence, its time period decreases.

2. (c) The level of sound is given by

$$L = 10 \log \left(\frac{I}{I_0} \right) dB$$

Let for 40 dB sound intensity be I and for 90dB sound intensity be I_x , then

$$40 = 10 \log \left(\frac{I}{I_0}\right)$$

$$\Rightarrow \log \left(\frac{I}{I_0}\right) = 4 \qquad ...(i)$$
and
$$90 = 10 \log \left(\frac{I_x}{I_0}\right)$$

$$\Rightarrow \log \left(\frac{I_x}{I_0}\right) = 9$$
Given,
$$I_x = xI$$

$$\Rightarrow \log \left(\frac{xI}{I_0}\right) = 9$$
or
$$\log x + \log \left(\frac{I}{I_0}\right) = 9$$

$$\Rightarrow \log x + 4 = 9 \qquad \text{[from Eq. (i)]}$$

$$\Rightarrow \log x = 5 \Rightarrow x = 10^5$$

(a) The Doppler shift in wavelength of light from star is given by

$$d\lambda = \frac{\lambda v}{c}$$

 (b) For third harmonic, n = 3. So, for an open pipe, the propagation of waves can be shown as



- ∴ Nodes = 3 and anti-nodes = 4
- (d) In an adiabatic process, there is no transfer of heat takes place between a thermodynamic system and its surroundings.

6. (a) The efficiency of a Carnot engine is given by

$$\eta = 1 - \frac{T_2}{T_1}$$
Given, $T_1 = 627^{\circ}\text{C} = 627 + 273 = 900 \text{ K}$
and $T_2 = 27^{\circ}\text{C} = 27 + 273 = 300 \text{ K}$

$$\Rightarrow \qquad \eta = 1 - \frac{300}{900} = \frac{600}{900} = \frac{2}{3}$$
Also, $\eta = \frac{\text{Work done}}{\text{Heat taken}}$

$$\Rightarrow \text{Work done} = \eta \times \text{Heat taken}$$

$$= \frac{2}{3} \times 300 = 200 \text{ J}$$

 (b) The undecayed nuclei in a radioactive sample are given by

given by
$$N = N_0 \left(\frac{1}{2}\right)^{\frac{t}{h_{1/2}}}$$
Given,
$$N = N_0 - \frac{15}{16}N_0 = \frac{1}{16}N_0, t = 2h$$

$$\Rightarrow \frac{N_0}{16} = N_0 \left(\frac{1}{2}\right)^{\frac{2}{h_{1/2}}}$$

$$\Rightarrow \left(\frac{1}{2}\right)^{\frac{2}{h_{1/2}}} = \frac{1}{16} = \left(\frac{1}{2}\right)^4$$

$$\Rightarrow \frac{2}{t_{t/2}} = 4 \Rightarrow t_{1/2} = \frac{1}{2}h = 30 \text{ min}$$

$$\therefore \text{ Mean life}, \quad \tau = 1.44t_{1/2}$$

∴ Mean life,
$$\tau = 1.44t_{1/2}$$

= 1.44 × 30 = 43.2 min ≈ 43 min

- (a) MRI (magnetic resonance imaging) gives a detailed image of soft tissues like in brain.
- (d) Of these leptons are truly elementary particles. While rest are composed of quarks, so they are composite particles.
- 10. (d) The output of NAND gate is as shown in the table below

In	Input			
A	В	Υ		
0	0	1		
0	1	1		
1	0	1		
1	1	0		

Thus, it will give logic 0 only when both inputs are in logic 1 state.

 (c) n - type semiconductor has electrons as majority charge carriers. So, they are obtained by doping with pentavalent atoms like phosphorous, arsenic, etc. p-type semiconductor has holes as majority charge carriers. So, they are obtained by doping with trivalent atoms like aluminium, boron, indium, etc.

12. (a) Given, current gain, $\beta = 50$

Input resistance, $R_i = 500 \,\Omega$

Output resistance, $R_L = 4 \text{ k} \Omega = 4000 \Omega$

Voltage gain = Current gain $\times \frac{R_L}{R_c}$

$$=50 \times \frac{4000}{500} = 400$$

Power gain = Current gain × Voltage gain $=50 \times 400 = 2 \times 10^4$

- 13. (c) In Balmer series, the electrons moves to n = 2 state So, possible transitions are $4 \rightarrow 2$, $3 \rightarrow 2$.
 - .. Number of spectral lines are 2.
- 14. (b) The IR region lies between microwave and visible region of electromagnetic spectrum.
- 15. (b) The de-Broglie wavelength of a particle is given by

$$\lambda = \frac{h}{mv} = \frac{h}{p}$$

The momentum of proton.

$$p_p = \sqrt{2mE} = \sqrt{2meV}$$

Similarly, for a - particle,

$$p_{\alpha} = \sqrt{2 \times 4m \times 2e \times V}$$

$$=\sqrt{16meV}$$

$$\frac{\lambda_p}{\lambda_\alpha} = \frac{p_\alpha}{p_p} = \frac{\sqrt{16meV}}{\sqrt{2meV}} = \sqrt{8}$$
$$= 2\sqrt{2}:1$$

- 16. (a) Raman scattering is an inelastic scattering of a photon by molecules which are excited to higher vibrational or rotational energy level. Raman shift depends on the wavelength of incident radiation.
- 17. (c) In $_{6}C^{14}$, number of neutrons = 14 6 = 8In $_{7}N^{15}$, number of neutrons = 15 - 7 = 8These are the examples of isotones.
- 18. (c) Given, $\frac{I_{\text{max}}}{I_{\text{min}}} = \frac{9}{1}$

As we know,

As we know,
$$\frac{I_{\text{max}}}{I_{\text{min}}} = \frac{(a_1 + a_2)^2}{(a_1 - a_2)^2} = \frac{9}{1}$$

$$\Rightarrow \frac{a_1 + a_2}{a_1 - a_2} = \frac{3}{1}$$

$$\Rightarrow a_1 + a_2 = 3a_1 - 3a_2$$

$$\Rightarrow a_1 = 2a_2$$
or
$$\frac{a_1}{a_2} = 2:1$$

19. (a) For dark fringe, path difference,

$$\Delta x = \left(n + \frac{1}{2}\right)\lambda$$

 \Rightarrow

$$\Delta x = \frac{dy}{D} \implies \frac{dy}{D} = \left(n + \frac{1}{2}\right)\lambda$$

For 1st dark fringe at directly opposite point of slit $n = 0, y = \frac{d}{2}$

$$\Rightarrow \frac{d\left(\frac{d}{2}\right)}{D} = \frac{\lambda}{2} \Rightarrow \lambda = \frac{d^2}{D}$$

- 20. (a) Newton's rings are fringes of equal thickness. These circular fringes were discovered by Newton, hence called Newton's rings. These rings are formed with equally spaced bright and dark band with central spot as dark.
- 21. (d) Diffraction pattern using light is difficult to observe in daily life because wavelength of light is very small.
- 22. (d) When a calcite crystal is placed over a dot on a piece of paper, one will observe two dots from above. If the crystal is rotated, then the dot produced by emergent ray will rotate around the stationary dot, which sometimes coincide with it.
- 23. (d) According to Brewster's law,

$$\Rightarrow \mu = \tan i_p$$

At critical angle, $\mu = \frac{1}{\sin i_C} = \frac{1}{\sin 45^\circ}$

$$\Rightarrow \mu = \sqrt{2}$$

$$\therefore \qquad \sqrt{2} = \tan i_p$$

$$\Rightarrow i_n = \tan^{-1} \sqrt{2} = 54.7^{\circ}$$

24. (b) For shunt resistance connected to galvanometer, current is given by

$$I_g = \left(\frac{S}{S+G}\right)I$$

$$\frac{2}{100}I = \left(\frac{S}{S+G}\right)I$$

$$\Rightarrow$$
 S+G=508

$$\Rightarrow S + G = 50S$$
or
$$S = \frac{G}{49}$$

25. (d) Magnetic moment of a coil of area A carrying current I is given by

$$M = IA$$

$$\Rightarrow$$
 Current, $I = \frac{M}{A}$

26. (b) The magnetic field at the centre of a circular coil carrying current I is given by

$$B = \frac{\mu_0 nI}{2R}$$

where, n = number of turns.

For coil 1,
$$B_1 = \frac{\mu_0 \times 10 \times 0.2}{2 \times 0.2} = 5 \,\mu_0$$

$$\begin{aligned} &\text{For coil 1, } B_1 = \frac{\mu_0 \times 10 \times 0.2}{2 \times 0.2} = 5 \, \mu_0 \\ &\text{For coil 2, } B_2 = \frac{\mu_0 \times 10 \times 0.3}{2 \times 0.4} = \frac{15}{4} \mu_0 \end{aligned}$$

∴ Net magnetic field,

$$B = B_1 - B_2 = 5\mu_0 - \frac{15}{4}\mu_0 = \frac{5}{4}\mu_0$$

- 27. (a) Permanent magnet should have high retentivity to persist magnetism on removal of magnetic field. It should also have high coercivity, so that the magnetism is not lost by external magnetic field.
- 28. (c) The power factor is the cosine of phase angle between voltage and current. For L -C-R circuit, it is given by

$$\cos \phi = \frac{R}{Z}$$

where, Z = impedance of circuit.

29. (c) Given, L = 1 H, V = 220 V, f = 50 Hz

Peak value of current
$$I_0 = \frac{V_0}{X_L} = \frac{V_0}{\omega L}$$

$$\Rightarrow I_0 = \frac{\sqrt{2V}}{2\pi f L} = \frac{\sqrt{2} \times 220}{2 \times \pi \times 50 \times 1} \approx 1 \text{ A}$$

30. (c) Let I_0 be the intensity of light incident on polariser.

On passing through polariser, it gets reduced to $\frac{I_0}{2}$.

So, according to law of Malus,
$$I = \frac{I_0}{2} \cos^2 \theta$$
Given,
$$I = \frac{75}{100} \times \frac{I_0}{2} = \frac{3I_0}{8}$$

$$\therefore \qquad \frac{3I_0}{8} = \frac{I_0}{2} \cos^2 \theta \quad \Rightarrow \quad \cos \theta = \frac{\sqrt{3}}{2}$$

$$\Rightarrow \qquad \theta = 30^\circ$$

31. (b) Potential due to a point charge at a distance r is given by

$$V = \frac{1}{4\pi\varepsilon_0\varepsilon_r} \times \frac{q}{r}$$

Given, $q = 10 \text{ nC} = 10 \times 10^{-9} \text{ C}$,

$$\varepsilon_r = 10, r = 0.1 \text{ m}$$

$$\Rightarrow V = \frac{9 \times 10^9 \times 10 \times 10^{-9}}{10 \times 0.1} = 90 \text{ V}$$

- 32. (b) Permittivity of metal is very high, so its dielectric constant is infinite.
- 33. (d) Force between two point charges is given by

$$F = \frac{kq_1q_2}{e^2}$$

When
$$r' = r + 20\%$$
 of $r = 1.2r$, then
$$F' = \frac{kq_1q_2}{(1.2r)^2} = \frac{kq_1q_2}{1.44r^2} = \frac{F}{1.44}$$

Percentage decrease in force = $\frac{F - F'}{F} \times 100$

$$= \frac{F - \frac{F}{1.44}}{F} \times 100 = \frac{0.44}{1.44} \times 100 = 31\%$$

34. (a) Given $q_1 = q_2 = 10 \text{ nC} = 10 \times 10^{-9} \text{C}$

$$r = 0.09 \text{ m}$$

Potential energy of two point charges is given by

$$U = \frac{1}{4\pi\epsilon_0} \times \frac{q_1 q_2}{r}$$

$$= 9 \times 10^9 \times \frac{10 \times 10^{-9} \times 10 \times 10^{-9}}{0.09} = 10^{-5} \text{ J}$$

35. (b) Given,
$$t = \frac{d}{2}$$

The capacitance is given by $C = \frac{\varepsilon_0 A}{d}$

$$C = \frac{\varepsilon_0 A}{d}$$

For dielectric medium between plates,

$$C' = \frac{\varepsilon_0 A}{d - t + \frac{t}{K}}$$

For metal, K = infinity

$$\Rightarrow C' = \frac{\varepsilon_0 A}{d - \frac{d}{2}} = \frac{2\varepsilon_0 A}{d} = 2C$$

Hence, capacitance increases 2 times.

- 36. (d) The specific resistance is the property of material which does not depend on its geometry. It increases with increase in temperature.
- 37. (d) At 4.2 K, the resistance of mercury suddenly drops to zero and behaves as a super conductor at this temperature (called critical temperature).
- 38. (c) Given, $\alpha_r = 4 \times 10^{-3} / \text{ K}$, $T_1 = 20 \text{ °C}$

Final resistance, $R_2 = R + 10\%R = 1.1R$

We know that, $\Delta R = \alpha_r R \Delta T$

$$\Rightarrow$$
 1.1R - R = 4×10⁻³×R×(T₂ - 20)

$$\Rightarrow$$
 0.1 = 4×10⁻³×(T_2 - 20)

$$\Rightarrow$$
 $T_2 = 25 + 20 = 45$ °C

39. (d) Here, 6Ω and 12Ω resistors are in parallel combination, so their equivalent resistance, $R_{\text{eq}} = \frac{6 \times 12}{6 + 12} = \frac{72}{18} = 4 \Omega$

$$R_{eq} = \frac{6 \times 12}{6 \times 12} = \frac{72}{18} = 4 \Omega$$

Now, $R_{\rm eq}$ and 4Ω are in series, so total resistance,

$$R_{*} = 4 + 4 = 8\Omega$$

 $R_t = 4 + 4 = 8\Omega$ Emf of battery, E = 16 V

$$\therefore$$
 Reading of voltmeter, $V' = \frac{4}{R} \times E = \frac{4 \times 16}{8} = 8V$

40. (a) When a charged particle moves in a uniform magnetic field normally, then a magnetic force acts on it. Due to this force, it will move in a circular path.

At every point of circle, its velocity changes direction. So, its momentum also changes but the total energy will remain same.

41. (a) If n be the number of waves, then wavelength of light in glass, $\lambda_g = \frac{0.04}{100}$

and wavelength of light in water, $\lambda_w = \frac{0.05}{n}$

Speed of light in glass, $v_g = \lambda_g \times f = \frac{0.04f}{r}$

where, f = frequency of light.

Similarly, speed of light in water, $v_w = \lambda_w \times f = \frac{0.05 f}{n}$

Relative refractive index

$$= \frac{\mu_w}{\mu_g} = \frac{v_g}{v_w} = \frac{0.04f}{n} \times \frac{n}{0.05f} = \frac{4}{5}$$
$$\Rightarrow \mu_g = \frac{5}{4} \times \mu_w = \frac{5}{4} \times \frac{4}{3} = \frac{5}{3}$$

42. (b) The critical angle between two media is given by

$$i_c = \sin^{-1}\left(\frac{\mu_1}{\mu_2}\right)$$

As we know that, $\mu_{air} = 1$, $\mu_{water} = 1.33$, $\mu_{glass} = 1.5$ and $\mu_{diamond} = 2.4.$

From given values, $\frac{\mu_1}{\mu_2}$ is maximum for water-glass

interface. So, critical angle will also be maximum, when light travels from glass to water.

43. (c) Given, angle of prism, A = 60°

As, the ray of emergence is symmetrical to incident ray. So, the angle of minimum deviation, $D_m = 60^{\circ}$.

 $\therefore \text{ Refractive index of prism, } \mu = \frac{\sin\left(\frac{A + D_m}{2}\right)}{\sin\left(\frac{A}{2}\right)}$

$$= \frac{\sin\left(\frac{60^\circ + 60^\circ}{2}\right)}{\sin\left(\frac{60^\circ}{2}\right)} = \frac{\sin 60^\circ}{\sin 30^\circ}$$
$$= \frac{\sqrt{3}}{2} \times \frac{2}{1} = \sqrt{3} = 1.73$$

- 44. (d) In the spectrum of visible light produced by a prism, the violet light have minimum wavelength. So, the dispersion will be maximum towards violet.
- 45. (b) Given, $\mu_g = 15$, $\mu_w = \frac{4}{3}$

From lens Maker's formula

$$\frac{1}{f} = (\mu_g - 1) \left(\frac{1}{R_1} - \frac{1}{R_2} \right)$$

$$\Rightarrow \frac{1}{R_1} - \frac{1}{R_2} = \frac{1}{f(\mu_g - 1)} \qquad ...(i)$$

When lens is immersed in water, then

$$\frac{1}{f'} = \left(\frac{\mu_g}{\mu_w} - 1\right) \left(\frac{1}{R_1} - \frac{1}{R_2}\right)
= \left(\frac{\mu_g}{\mu_w} - 1\right) \frac{1}{f(\mu_g - 1)}$$
 [using Eq. (i)]
$$\frac{f}{f'} = \left(\frac{15}{4/3} - 1\right) \times \frac{1}{(15 - 1)}
= \left(\frac{9}{8} - 1\right) \times 2 = \frac{1}{4}$$

f' = 4f or f' > f

 \therefore The focal length of lens is greater than f in water.

46. (a) The focal length of combination of two lenses,

$$\frac{1}{f} = \frac{1}{f_1} + \frac{1}{f_2} = \frac{1}{(1/4)} + \frac{1}{(-1/2)} \qquad \left(\because f = \frac{1}{P} \right)$$
$$= 4 - 2 = 2$$

- 47. (b) Eddy currents are produced in a material, when it is placed in a time varying magnetic field. It is based on the Faraday's law of etectromagnetic induction.
- 48. (d) Given, $V_p = 220 \text{ V}, \eta = 80\% = 0.8$

$$P_0 = 8 \,\mathrm{kW} = 8000 \,\mathrm{W}$$

Efficiency of transformer, $\eta = \frac{\text{Output power}}{\text{Input power}}$

$$\Rightarrow \qquad \eta = \frac{P_o}{P_i} \Rightarrow 0.8 = \frac{8000}{P_i}$$

$$\Rightarrow \qquad \qquad P_i = \frac{8000}{0.8} = 10000$$

$$\Rightarrow$$
 $V_n I_n = 100000$

$$\Rightarrow V_p I_p = 10000$$
or
$$I_p = \frac{10000}{220} = 45.5 \text{ A} \approx 45 \text{ A}$$

$$I_p = \frac{10000}{220} = 45.5 \text{ A} \approx 45 \text{ A}$$

49. (b) Given, $f_0 = 600 \text{ Hz}, Q_1 = 3, Q_2 = 2$

The bandwidth in L-C-R circuit,

$$\beta = \frac{f_0}{O}$$

As, quality factor decreases, bandwidth increases.

This increase in bandwidth is given by

$$\Delta\beta = \beta_2 - \beta_1 = \frac{f_0}{Q_2} - \frac{f_0}{Q_1} = f_0 \left(\frac{1}{Q_2} - \frac{1}{Q_1} \right)$$
$$= 600 \left(\frac{1}{2} - \frac{1}{3} \right) = 100 \text{ Hz}$$

50. (d) Given, t = 4 s, u = 0, $g = 10 \text{ ms}^{-2}$

Using equation of motion,

$$h = ut + \frac{1}{2}gt^2 = \frac{1}{2}gt^2 = \frac{1}{2} \times 10 \times (4)^2 = 80 \text{ m}$$

51. (b) In liquid crystal phases, there are 4 types of phases as Nematic, Smectic, Cholesteric and Discotic. Of these, Smectic phase is more close to solid than to liquid.

52. (a) The acceleration due to gravity at earth's surface is given by

$$g = \frac{GM}{R^2}$$

$$\Rightarrow$$
 $g \propto \frac{1}{R^2}$

so, as the radius of earth decreases or the earth shrinks in size, the value of g increases.

53. (b) The thermal resistance of a rod is given by

$$R = \frac{l}{KA}$$

As, length and area of two rods are same, then in series combination.

$$\Rightarrow \frac{R = R_1 + R_2}{\frac{2l}{K_s A}} = \frac{l}{K_1 A} + \frac{l}{K_2 A}$$

$$\Rightarrow \frac{2}{K_s} = \frac{1}{K_1} + \frac{1}{K_2} = \frac{K_1 + K_2}{K_1 K_2}$$

$$\Rightarrow K_s = \frac{2K_1 K_2}{K_1 + K_2}$$

54. (c) Let F_1 and F_2 be the two forces acting at a point, then their resultant,

$$\begin{aligned} F_R &= \sqrt{F_1^2 + F_2^2 + 2F_1F_2\cos\theta} \\ \text{Given,} & F_1 &= F_2 &= F \\ \Rightarrow & F_R &= \sqrt{2F^2 + 2F^2\cos\theta} \\ \Rightarrow & F_R^2 &= 2F^2(1 + \cos\theta) \end{aligned} \qquad ...(i)$$

As per question,

As per question,

$$F_R^2 = 3F_1F_2 = 3F^2$$

$$\Rightarrow 2F^2(1 + \cos \theta) = 3F^2 \quad [\text{using Eq. (i)}]$$

$$\Rightarrow 1 + \cos \theta = \frac{3}{2}$$

$$\Rightarrow \cos \theta = \frac{1}{2} \text{ or } \theta = 60^\circ$$

55. (d) The addition of impurities in a liquid may increase or decrease the surface tension of liquid depending on the nature of impurities.

If the impurities are highly soluble in liquid, then it will increase the surface tension. But if it is less soluble in liquid, then it will decrease the surface tension of liquid.

- 56. (c) The viscosity decreases with increase in temperature. Due to this reason, the hot water moves faster than cold water. Since in summer temperature is high, so more viscous oils are used in motorcars.
- 57. (c) Moment of momentum of an electron in nth orbit is given by

$$L = \frac{nh}{2\pi}$$

For an electron in second Bohr orbit,
$$n = 2$$

$$\therefore L = \frac{2h}{2\pi} = \frac{h}{\pi}$$

58. (a) The excitation energy is the minimum energy required to excite an electron from ground state of atom to any of its excited state and ionisation energy is the amount energy needed to remove an electron from

So, lesser the excitation energy and more the ionisation energy, more the stability of atom.

(c) Given, work function, \$\phi = 3 eV

$$\lambda = \frac{hc}{\phi} = \frac{1242}{\phi} = \frac{1242}{3} = 414 \text{ nm}$$

60. (d) The equivalent capacitance of three capacitors connected in series is given by

$$\frac{1}{C_s} = \frac{1}{C_1} + \frac{1}{C_2} + \frac{1}{C_3}$$

Given,
$$C_1 = C_2 = C_3 = C$$

Given,
$$C_1 = C_2 = C_3 = C$$

$$\frac{1}{C_s} = \frac{3}{C} \text{ or } C_s = \frac{C}{3}$$

Similarly, for parallel combination,

$$C_p = C + C + C = 3C$$

∴ Ratio of equivalent capacitance,

$$\frac{C_s}{C_p} = \frac{C/3}{3C} = \frac{1}{9} \text{ or } 1:9$$

Chemistry

61. (d) An organic compound gives oily liquid on heating with bromine and potassium hydroxide solution. On shaking with acetic anhydride, an antipyretic drug acetanilide obtained is benzamide.

$$\begin{array}{c} \text{C}_6\text{H}_5\text{--CONH}_2 \xrightarrow{\text{Br}_2\text{/KOH}} \text{C}_6\text{H}_5\text{NH}_2 \\ \\ \text{Benzamide} & \downarrow \text{(CH}_3\text{CO)}_2\text{O} \\ \\ \text{C}_6\text{H}_5\text{NHCOCH}_3 \\ \\ \text{Acctanilish} \end{array}$$

62. (d) Silver salt of fatty acid on refluxing with an alkyl halide gives an ester.

$$\begin{array}{ccc} CH_{3}COOAg & + C_{2}H_{5}Br \longrightarrow CH_{3}COOC_{2}H_{5} \\ \text{Silver salt of fatty acid} & Alkyl halide & Ester \\ \end{array}$$

+ AgBr

- 63. (d) Pepsin, ptyalin, lipase are all enzymes used for the breaking down of nutrients, while cellulose is a polysaccharide.
- 64. (b) Combination of H₂ and Br₂ to give HBr, is second order reaction.

$$H_2 + Br_2 \longrightarrow 2HBr$$

Rate law expression, $r = k[H_2][Br_2]$

- .. Order w.r.t. H2 and Br2 is one.
- .: Overall order = 1 + 1 = 2
- **65.** (c) The diameter of colloidal particle ranges from 10^{-6} m to 10^{-9} m.
- 66. (b) The 2p-orbital has electronic configuration as follows

11 11 11

- \therefore Three electrons are with -1/2 spin quantum number and other three electrons are with +1/2 spin quantum number.
- 67. (b) The molecular formula of 2-methyl butane, 2,2-dimethyl propane and pentane is same i.e. (C₅H₁₂). They are structural isomers.

∴ Mass of N₂ left = 56 - 28 = 28 g

∴ Moles of N₂ left =
$$\frac{28}{28}$$
 = 1 mole

Mass of H_2 left = 8 - 6 = 2 g

$$\therefore$$
 Moles of H₂ left = $\frac{2}{2}$ = 1 mole

Moles of ammonia = $\frac{34}{17}$ = 2 moles

- 69. (a) For constant pressure and temperature process, ΔH and $\Delta U = 0$
- 70. (a) In a galvanic cell, the electron flow from anode to cathode through the external circuit.

 (c) The mixture of 2-chloropropane and chloromethane on treating with sodium metal in dry ether gives 2-methyl propane i.e.,

$$\begin{array}{c} \operatorname{CH_3} \\ | \\ \operatorname{CH_3} - \operatorname{CH} - \operatorname{Cl} + \operatorname{Cl} - \operatorname{CH_3} \xrightarrow{2\operatorname{Na}} \\ \text{2-chloropropane} & \operatorname{Chloromethane} & \operatorname{CH_3} \\ | \\ \operatorname{CH_3} - \operatorname{CH} - \operatorname{CH_3} + 2\operatorname{NaCl} \\ \text{2-methylpropane} & \end{array}$$

- 72. (c) Benzyl chloride is more reactive than alkyl halides as benzyl carbocation is stabilised by resonance. Hence, it easily gives nucleophilic substitution reaction.
- 73. (d) The main product obtained when sodium carbonate reacts with mercuric chloride is mercuric oxide.

$$HgCl_2 + Na_2CO_3 \longrightarrow HgO + CO_2 + 2NaCl \text{ or}$$

 $HgCO_3 + 2NaCl$

74. (b) In a electrothermal process, the compound displayed by silica from calcium phosphite is phosphorus pentoxide as follows:

$$2 \text{ Ca}_3(\text{PO}_4)_2 + 6 \text{ SiO}_2 \longrightarrow 6 \text{CaSiO}_3 + \text{P}_4 \text{O}_{10}$$

75. (b) CH₄ + 2O₂ \longrightarrow CO₂ + 2H₂O ; $\Delta H = 890$ kJ/mol ^{16 g} $_{64 \text{ g}}$ $_{64 \text{ g}}$ $_{36 \text{ g}}$

Heat liberated on combustion of 16 g CH₄ is 890 kJ.

∴ Heat liberation from 3.2 g methans
$$= \frac{3.2}{16} \times 890 = \frac{890}{5}$$
= 178 H

76. (a) According to gas equation,

$$pV = nRT$$

$$V = \frac{nRT}{p}$$

As both p and T are double, V remains constant i.e., 4 dm^3 .

 (d) Copper on reacting with conc. HNO₃ gives copper nitrate

$$\text{Cu+HNO}_3 \text{ (conc.)} \longrightarrow \\ \mathfrak{C} \mathfrak{A} \text{(NO}_3)_2 + 2 \text{H}_2 \text{O} + 2 \text{NO}_2 \\ \text{Copper nitrate}$$

On strongly heating with copper nitrate, copper oxide is obtained.

$$2\mathrm{Cu}(\mathrm{NO_3})_2 \longrightarrow 2\mathrm{CuO}_{\begin{subarray}{c}\mathrm{Copper \ oxide}\\(5\ \mathrm{g})\end{subarray}} + 4\mathrm{NO_2} + \mathrm{O_2}$$

- .: Equivalent weight of Cu
 - = Weight of copper × Equivalent weight of oxygen = 4 × 8 = 32

78. (c) For the following reaction,

$$N_2 + 3H_2 \implies 2NH_3 + 92.3 \text{ kJ}$$

- Reducing temperature is favourable as it is an exothermic process and shift equilibrium towards right.
- (ii) Also on removing NH₃ equilibrium shift towards right according to Le-Chatelier's principle.
- (iii) Δn_g is negative for the process. Increase in pressure, equilibrium towards right. For an exothermic reaction, increasing temperature shifts the reaction to reactant side.
- 79. (d) The chemical equilibrium of a reversible reaction is not influenced by catalyst as it only increase the rate of reaction to achieve the equilibrium faster. The increase in rate of forward direction is equal to increase in rate of backward direction at equilibrium.
 - .. Equilibrium point is not shifted.
- 80. (c) The structure of cumene is

The IUPAC name is 1-methyl ethyl benzene.

81. (d) Moles of HCl =
$$\frac{1.2046 \times 10^{24}}{6.023 \times 10^{23}} = 2$$

∴ Normality =
$$\frac{6.023 \times 10^{23}}{\text{moles of HCl}}$$

$$\frac{\text{moles of HCl}}{\text{volume of solution (L or dm}^3)}$$

$$= \frac{2}{1} = 2 \text{ N}$$

- 82. (c) Nuclear theory of atom was put forward by Rutherford. He discovered α and β-rays and projected the law of radioactive decay.
- 83. (c) In acetylene or ethyne molecule, the two carbon atoms are linked by one σ and two π -bonds.

84. (c)
$$H_2(g) + \frac{1}{2}O_2(g) \longrightarrow H_2O(g)$$
; $\Delta H_1 = + ve$
 $H_2O(g) \longrightarrow H_2O(l)$; $\Delta H_3 = + ve$
 $H_2(g) + \frac{1}{2}O_2(g) \longrightarrow H_2O(l)$; $\Delta H_2 = \Delta H_1 + \Delta H_3$
 $\therefore \Delta H_2 > \Delta H_1$

85. (d) For radioactive decay

$$t_{1/2} = \frac{0.693}{k}$$

For concentration to reduce to $\frac{1}{16}$ of original amount

$$t = t_{1/2} \times 4$$

$$\therefore t_{1/2} = \frac{192}{4} = 48 \min$$

86. (d) The reagent, Cl₂ does not give acid chloride on heating with carboxylic acids, while other reagents give acid chloride.

$$R$$
—COOH $\xrightarrow{PCl_3}$ R —COCl+ $POCl_3$ + HCl
 R —COOH $\xrightarrow{PCl_3}$ $3R$ —COCl + H_3PO_3
 $\xrightarrow{SOCl_2}$ R —COCl + $SO_2\uparrow$ + $HCl\uparrow$

87. (d) Reducing property of halogens increases from F to I.
∴ I get oxidised by nitric acid.

$$\begin{array}{c} 0 \\ I_2 + 10 \text{ HNO}_3 \longrightarrow 2 \\ \text{HIO}_3 + 10 \text{ NO}_2 + 4 \\ \text{H}_2 \\ \text{Odine} \\ \text{acid} \\ \text{odic} \\ \text{acid} \\ \end{array}$$

 (a) Lead form nitric oxide with dil. HNO₃. It does not form ammonium nitrate by reaction with dil. nitric acid.

$$3\text{Pb} + 8\text{HNO}_3 \longrightarrow 3\text{Pb}(\text{NO}_3)_2 + 2\text{NO} + 4\text{H}_2\text{O}$$
Nitric oxide

- 89. (d) The elements with atomic number 9, 17, 35, 53 and 85 are all halogens, they have electronic configuration of ns²np⁵.
- 90. (b) In the electrolytic method of obtaining aluminium from purified bauxite, cryolite is added to the charge in order to lower the melting point of bauxite and brings conductivity.
- 91. (c) HNO₃ is not an amphoteric substance as, it behave only as acid. It can only donate H⁺ ions. While, substance like HCO₃, H₂O, and NH₃ can act as both donor and acceptor to H⁺ ions, so they are amphoteric in nature.
- (b) Equivalent moles of H₂SO₄ and KOH undergoing neutralisation

$$=50 \times 0.2 \times 10^{-3} = 0.01$$

∴ Heat of neutralisation = 0.01 × 57.3 kJ = 573 J

93. (c)
$$\begin{array}{c} {}^{14}X_5 \longrightarrow {}^{14}X_6 + {}^{0}_{-1}e \\ {}^{Parent} & \downarrow \\ {}^{14}N_7 + {}^{0}_{-e}e \end{array}$$

- \therefore The number of neutrons in parent nucleus = 14-5 = 9
- (d) Stainless steel does not rust because chromium forms an oxide layer and protects iron from rusting.
- 95. (b) Ethanol can be synthesised as follows:

$$CH_3MgI + HCHO \xrightarrow{H_2O} \xrightarrow{H_2O}$$

96. (b) The rate law expression is, r = k[SO₂]²[O₂]
As, volume increase 2 times, concentration reduces by

 \[
 \frac{1}{2} \text{ times i.e., [SO₂]₁ = [2SO₂] and [O₂]₁ = [2O₂]

:. New rate,
$$r_1 = k[2SO_2]^2[2O_2]$$

$$r_1 = 8r$$

$$\frac{r_1}{r_1} = \frac{8}{r_1}$$

 $\therefore pH_2 = pH_1 + 1$

$$pH_1 = pK_a + log \frac{[CH_3COONa]}{[CH_3COOH]} \qquad ...(i)$$

$$\begin{aligned} & \text{Given,} [\text{CH}_3\text{COONa}]_2 / [\text{CH}_3\text{COOH}]_2 \\ & = 10[\text{CH}_3\text{COONa}] / [\text{CH}_3\text{COOH}] \\ & \text{pH}_2 = \text{p}K_a + \log 10[\text{CH}_3\text{COONa}] / [\text{CH}_3\text{COOH}] \\ & \text{pH}_2 = \text{p}K_a + \log[\text{CH}_3\text{COONa}] / [\text{CH}_3\text{COOH}] + \log 10 \end{aligned}$$

98. (b) When mixture of methane and oxygen is passed through heated molybdenum oxide, the main product formed is methanal.

$$CH_4 + O_2 \xrightarrow{Mo\text{-axide}} HCHO + H_2O$$
Methane

99. (d) Benzene can be obtained by heating benzoic acid with soda lime and phenol with zinc dust as follows:

$$\begin{split} & C_6H_5COOH + \underset{Soda lime}{2NaOH} \xrightarrow{\Delta} C_6H_6 + Na_2CO_3 \\ & C_6H_5 \longrightarrow OH + \underset{Zinc dust}{Zinc} \xrightarrow{\Delta} C_6H_6 + ZnO \end{split}$$

100. (c) Ethyl benzoate is boiled with alc. potash to give ethyl alcohol and potassium benzoate.

$$C_6H_5COOCH_2CH_3 \xrightarrow{Alc. potash} C_6H_5COOK$$

Ethyl benzosate

+ CH₃CH₃OH

[From Eq. (i)]

Potassium benzoate is converted into benzoic acid, a white solid which separates out.

$$C_6H_5COOK + HCl \longrightarrow C_6H_5COOH + KCl$$

101. (a) On passing H,S gas in presence of dil. HCl for qualitative analysis of second group due to common ion effect, lower concentration of sulphide ions is obtained. It is sufficient for the precipitation of second group cations in forms of their sulphides and hence their dissociation decreases.

102. (b)
$$E^{\circ} = E^{\circ}_{(Ag^{+}/Ag)} - E^{\circ}_{(Al^{3+}/Al)}$$

 $2.46 = 0.80 - E^{\circ}_{(Al^{3+}/Al)}$
 $\therefore E^{\circ}_{(Al^{3+}/Al)} = -1.66 \text{ V}$

∴ Reduction potential = - 1.66 V.

- 103. (c) The first fraction obtained during the fractionation of petroleum is hydrocarbon gases.
- 104. (a) Ethanol gives trichloromethane on distilling with bleaching powder.

(I)Cl₂ + H₂O
$$\longrightarrow$$
 2HCl+ [O]
CH₃CH₂OH+ [O] \longrightarrow CH₃CHO+ H₂O

(III)
$$CCl_3CHO + Ca(OH)_2 \longrightarrow$$

 $2CHCl_3 + (HCOO)_2Ca$
Tricklore methane

105. (b) Benzoin is a α-hydroxy ketone.

- 106. (b) For every 10K rise in temperature, rate of reaction double.
 - ∴ From 298 K to 310 K, the reaction rate became (2)² times i.e., 4 times.

$$k = 3.2 \times 10^{-3} \text{ s}^{-1} \times 4 = 1.28 \times 10^{-2} \text{ s}^{-1}$$

107. (c) The acidic strength of an acid increase with ionisation.

The value of pK_a is inversely proportional to ionisation constant (Ka).

- ∴ The acid with pK_a value 1.0 is strongest.
- 108. (a) Unsaturated fatty acids contains one or more double bond in their carbon chains.

Their general formula is $C_n H_{2n-2r} O_2$.

- :. Oleic acid $(C_{18}H_{34}O_2)$ is unsaturated fatty acid with one double bond.
- 109. (b) Nylon is not a homopolymer. It is a polymer of hexamethylenediamine and adipic acid.
- 110. (c) The coaltar fraction which contains phenol is called middle oil.

111. (b)
$$A + B \rightleftharpoons C + D$$
Initially 1 1 0 0
at equilibrium $\frac{2}{3}$ $\frac{2}{3}$ $\frac{1}{3}$ $\frac{1}{3}$

$$\therefore \text{ Equilibrium constant } (K) = \frac{[C][D]}{[A][B]}$$

$$= \frac{\frac{1}{3} \cdot \frac{1}{3}}{\frac{2}{3} \cdot \frac{2}{3}} = \frac{1}{4} = 0.25$$

- 112. (c) The particles of ore float because their surface is not easily wetted by water.
- 113. (d) Amorphous solids are isotropic in nature i.e., they shows same properties in all the directions.

114. (c) Rate of diffusion
$$\approx \frac{1}{\sqrt{\text{Molar mass}}}$$

$$\therefore \frac{r_{\text{H}}}{r_{\text{A}}} = \sqrt{\frac{M_{\text{A}}}{M_{\text{H}}}}$$

$$\therefore r_{\text{H}} = 6r_{\text{A}}$$

$$\therefore 6 = \sqrt{\frac{M_{\text{A}}}{2}}$$

- 115. (b) Dulong and Petit's law is valid only for solid elements. According to this law, the product of atomic mass and specific heat of a solid element is approximately equal to 6.4 cal/mol.
- 116. (d) The gas which has greater critical temperature is readily adsorbed by activated charcoal.

The order of critical temperature is

- :. SO, gas is readily adsorbed by chorcoal.
- 117. (b) In fcc unit cell of NaCl, Na⁺ ion is present at edge centre and Cl⁻ ion is present at corner.

$$\therefore$$
 Edge length, $a = 2r^+ + 2r^-$

$$a = 2(r^+ + r^-)$$

$$= 2x \qquad [\because x = r^+ + r^-]$$

118. (d) In K₃[Fe(CN)₆], the ligand has satisfied both primary and secondary valencies of ferric ion. The + 3 charge of ferric ion is satisfied by negative charge on cyanide ion. The coordination sphere's secondary valency is satisfied by six cyanide ligands.

- 119. (b) 2-acetoxy benzoic acid is aspirin. It is used as an antipyretic to reduce body temperature.
- 120. (a) Nucleoside on hydrolysis gives an aldopentose and a heterocyclic base i.e. purine and pyrimidine.

Mathematics

121. (d) Given that, $A = \{a, b, c\}, B = \{b, c, d\}$

and
$$c = \{a, d, c\}$$

Now,
$$A - B = \{a, b, c\} - \{b, c, d\} = \{a\}$$

and
$$B \cap C = \{b, c, d\} \cap \{a, d, c\} = \{c, d\}$$

$$(A-B)\times(B\cap C) = \{a\}\times\{c,d\} = \{(a,c),(a,d)\}$$

122. (b) We have,

$$f: X \to Y$$

X: domain and Y: codomain

In one-one function,

$$x_1 \neq x_2$$

$$f(x_1) \neq f(x_2)$$

In onto function,

Range = domain

$$f(x) = \sin x$$

So, if
$$X = \left[0, \frac{\pi}{2}\right]$$
 and $Y = [-1, 1]$

For each value of $x \in X$ and range = [0, 1], there exists a unique value for $y \in Y$

Hence, function is one-one but not onto.

123. (a) We have,

$$\log_4 2 + \log_4 4 + \log_4 16 + \log_4 x = 6$$

$$\log_4 (2 \times 4 \times x \times 16) = 6$$

$$\log_4(128x) = 6$$

$$128x = 4^6$$

$$\Rightarrow$$
 128x = 64 × 4³

$$\Rightarrow$$
 $2x = 4^3$

$$\Rightarrow x = \frac{64}{2} = 32$$

124. (c) We have,

$$S_n = \frac{1}{6 \cdot 11} + \frac{1}{11 \cdot 16} + \frac{1}{16 \cdot 21} + \dots + n \text{ terms}$$

$$=\frac{1}{5}\left(\frac{1}{6}-\frac{1}{11}+\frac{1}{11}-\frac{1}{16}+\dots\frac{1}{5n-1}-\frac{1}{5n+6}\right)$$

$$=\frac{1}{5}\left(\frac{1}{6}-\frac{1}{5n+6}\right)$$

$$=\frac{1}{5}\left[\frac{5n+6-6}{6(5n+6)}\right]$$

$$= \frac{1}{5} \left[\frac{5n}{6(5n+6)} \right]$$

So,
$$6S_n = \frac{n}{(5n+6)}$$

125. (b) Here, terms greater than 5!, i.e.

.. For terms

Now, consider $(1!)^2 + (2!)^2 + (3!)^2 + (4!)^2$

$$= 1 + 4 + 36 + 576$$

When, 617 is divided by 100, its remainder is 17. So, required remainder is 17.

126. (d) Given that, $(p \land \sim r) \rightarrow (\sim p \lor q)$ is false

$$\Rightarrow$$
 $(p \land \sim r)$ is true and $(\sim p \lor q)$ is false

$$\Rightarrow$$
 (p is true and $\sim r$ is true)

and ($\sim p$ is false and q is false)

 $\Rightarrow p$ is true, r is false and q is false.

127. (a) Since, α , β and γ are the roots of the equation

$$x^3 - 8x + 8 = 0$$
, then

$$\alpha + \beta + \gamma = 0, \alpha\beta + \beta\gamma + \gamma\alpha = -8,$$

 $\alpha\beta\gamma = -8$...(i)

Therefore, $(\alpha + \beta + \gamma)^2 = 0$

$$\Rightarrow \alpha^2 + \beta^2 + \gamma^2 + 2(\alpha\beta + \beta\gamma + \gamma\alpha) = 0$$

$$\Rightarrow \alpha^{2} + \beta^{2} + \gamma^{2} = -2(-8) = 16$$

$$\Sigma \alpha^{2} = 16$$
and
$$\frac{1}{\alpha \beta} + \frac{1}{\beta \gamma} + \frac{1}{\gamma \alpha} = \frac{\alpha + \beta + \gamma}{\alpha \beta \gamma} = \frac{0}{-8} = 0$$

$$\Sigma \frac{1}{\alpha \beta} = 0$$

128. (c) $1080 = 2^3 \times 3^3 \times 5$ (prime factorization) $675 = 3^3 \times 5^2$

So, Greatest Common divisor = $3^3 \times 5 = 27 \times 5 = 135$

129. (d) $b \equiv c \pmod{a}$

So,
$$\frac{b+c}{a}$$
 and $\frac{b-c}{a} = \frac{(b+c)(b-c)}{a^2}$
= $\frac{b^2-c^2}{a^2}$ or $\frac{a^2}{b^2-c^2}$

Here, $b^2 \equiv c^2 \pmod{a^2}$

130. (c) By taking option (c), $a|(b+c) \Rightarrow a|b \text{ and } a|c$ e.g. 6|18 ≠ 6|1 and 6|17

131. (c) We have,
$$2A + 3B = \begin{bmatrix} 2 & -1 & 4 \\ 3 & 2 & 5 \end{bmatrix}$$
 ... (i

and
$$A + 2B = \begin{bmatrix} 5 & 0 & 3 \\ 1 & 6 & 2 \end{bmatrix}$$
 ... (ii)

Multiply Eq. (ii) by 2, we get

$$2A + 4B = \begin{bmatrix} 10 & 0 & 6 \\ 2 & 12 & 4 \end{bmatrix} \qquad \dots \text{ (iii)}$$

Now, subtracting Eq. (i) from Eq. (iii), we get

$$B = \begin{bmatrix} 10 & 0 & 6 \\ 2 & 12 & 4 \end{bmatrix} - \begin{bmatrix} 2 & -1 & 4 \\ 3 & 2 & 5 \end{bmatrix} = \begin{bmatrix} 8 & 1 & 2 \\ -1 & 10 & -1 \end{bmatrix}$$

132. (a) Given that,

$$O(A) = 2 \times 3, O(B) = 3 \times 2,$$

 $O(C) = 3 \times 3$
 $\Rightarrow O(A') = 3 \times 2, O(B') = 2 \times 3$
 $(a) C(A + B')$
Now, $O(A + B') = 2 \times 3$
and $O(C) = 3 \times 3$

So, matrix C(A + B') cannot be determined.

(b) C(A + B')' $O(A + B') = 2 \times 3$

$$\Rightarrow O(A + B')' = 3 \times 2$$
 and $O(C) = 3 \times 3$

Therefore, matrix C(A + B')' can be determined.

(c) $O(BA) = 3 \times 3$ and $O(C) = 3 \times 3$

Therefore, matrix BAC can be determined.

(d)CB + A'

Now, order of CB = (order of C) (order of B)= (order of C is 3×3) (order of B is 3×2) = order of CB is 3×2

Since, $O(A') = 3 \times 2$

Therefore, matrix CB + A' can be determined.

133. (a) We have,
$$A = \begin{bmatrix} 1 & -3 \\ 2 & k \end{bmatrix}$$

Now, $A = \begin{bmatrix} 1 & -3 \\ 2 & k \end{bmatrix} \begin{bmatrix} 1 & -3 \\ 2 & k \end{bmatrix}$

$$= \begin{bmatrix} 1-6 & -3-3k \\ 2+2k & -6+k^2 \end{bmatrix} = \begin{bmatrix} -5 & -3-3k \\ 2+2k & k^2-6 \end{bmatrix}$$

Now, $A^2 - 4A + 10I =$

$$\Rightarrow \begin{bmatrix} -5 & -3 - 3k \\ 2 + 2k & k^2 - 6 \end{bmatrix} - 4 \begin{bmatrix} 1 & -3 \\ 2 & k \end{bmatrix}$$

$$+ 10 \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & -3 \\ 2 & k \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} -5 - 4 + 10 & -3 - 3k + 12 + 0 \\ 2 + 2k - 8 + 0 & k^2 - 6 - 4k + 10 \end{bmatrix} = \begin{bmatrix} 1 & -3 \\ 2 & k \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} -1 & -3k + 9 \\ 2k - 6 & k^2 - 4k + 4 \end{bmatrix} = \begin{bmatrix} 1 & -3 \\ 2 & k \end{bmatrix}$$

$$k^{2} - 4k + 4 = k$$

$$k^{2} - 5k + 4 = 0$$

$$k^{2} - 4k - k + 4 = 0$$

$$k^{2} - 4k - k + 4 = 0$$

$$k^{2} - 4k - k + 4 = 0$$

$$k(k - 4) - 1(k - 4) = 0$$

$$k(k - 4) (k - 1) = 0$$

$$k = 4, 1$$

$$k + y \quad y + z \quad z + x \quad x \quad y \quad z \quad x + y \quad y - z \quad z - x$$

$$k - 4 - 1(k - 4) = 0$$

$$k = 4, 1$$

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$$k - 4 - 1(k - 4) = 0$$

$$k = 4, 1$$

$$k - 4 - 1(k - 4) = 0$$

$$k = 4, 1$$

$$k - 4$$

134. (a)
$$\begin{vmatrix} x+y & y+z & z+x \\ x & y & z \\ x-y & y-z & z-x \end{vmatrix}$$

$$= \begin{vmatrix} (x+y+z) & y & z \\ 0 & y-z & z-x \end{vmatrix}$$

$$= (x+y+z) \begin{vmatrix} 2 & y+z & z+x \\ 1 & y & z \\ 0 & y-z & z-x \end{vmatrix}$$

$$= (x+y+z) \begin{vmatrix} 2 & y+z & z+x \\ 0 & y-z & z-x \end{vmatrix}$$

$$= (x+y+z) \begin{vmatrix} 2 & y+z & z+x \\ 0 & y-z & z-x \\ 0 & y-z & z-x \end{vmatrix}$$

$$= (x+y+z) \times 0 = 0$$

$$= (x+y+z) \times 0 = 0$$

$$= (x+y+z) \times 0 = 0$$

[: R2 and R3 are identical]

135. (d) If a * b = b * a, then the operation is commutative. If (a*b)*c = a*(b*c), then the operation is associative.

By option (d),

a * b = a + b + ab

b * a = b + a + ba = a + b + ab

Here, a * b = b * a, so the operation is commutative.

$$(a * b) * c = (a + b + ab) * c$$

 $= (a + b + ab) + c + (a + b + ab)c$
 $= a + b + ab + c + ac + bc + abc$
 $= a + b + c + ab + ac + bc + abc$
 $a * (b * c) = a * (b + c + bc)$
 $= a + b + c + bc + a(b + c + bc)$
 $= a + b + c + bc + ab + ac + abc$

Here, (a * b) * c = a * (b * c).

So, the operation is associative.

136. (c) Given that, $G = \{1, 5, 7, 11\}$ is a group under multiplication module 12.

∴
$$7^{-1} = 7$$
 [∴ $7^{-1} \otimes_{12} 7 = 1$]
Now, $7^{-1} \otimes_{12} (x \otimes_{12} 11) = 5$
⇒ $7 \otimes_{12} (11 \otimes_{12} x) = 5$
⇒ $(7 \otimes_{12} 11) \otimes_{12} x = 5$
 $\{7 \otimes_{12} 11 = \text{remainder after dividing 77 from 12}\}$
⇒ $5 \otimes_{12} x = 5$
⇒ $x = 1$

137. (b) In additive subgroup 'o' is the identity.

So, required set (N, +) which is not a subgroup.

138. (d) We have, $p = \hat{i} + \hat{j}$, $q = 4\hat{k} - \hat{j}$ and $r = \hat{i} + \hat{k}$ So, $3p + q - 2r = 3\hat{i} + 3\hat{j} + 4\hat{k} - \hat{j} - 2\hat{i} - 2\hat{k}$

Now, required unit vector =
$$\frac{\hat{\mathbf{i}} + 2\hat{\mathbf{j}} + 2\hat{\mathbf{k}}}{\sqrt{1 + 4 + 4}}$$
$$= \frac{1}{2}(\hat{\mathbf{i}} + 2\hat{\mathbf{j}} + 2\hat{\mathbf{k}})$$

139. (a) We have, $|\mathbf{a}| = 3\sqrt{3}$, $|\mathbf{b}| = 4$ and $|\mathbf{a} + \mathbf{b}| = \sqrt{7}$

Now,
$$|\mathbf{a} + \mathbf{b}|^2 = |\mathbf{a}|^2 + |\mathbf{b}|^2 + 2|\mathbf{a}||\mathbf{b}|\cos\theta$$

$$\Rightarrow \qquad (\sqrt{7})^2 = (3\sqrt{3})^2 + 16 + 2(3\sqrt{3})(4)\cos\theta$$

$$\Rightarrow \qquad 7 = 27 + 16 + 24\sqrt{3}\cos\theta$$

$$\Rightarrow \qquad 24\sqrt{3}\cos\theta = -36$$

$$\Rightarrow \qquad \cos\theta = -\frac{36}{24\sqrt{3}}$$

$$\Rightarrow \qquad \cos\theta = -\frac{\sqrt{3}}{2}$$

140. (b) Given, a is perpendicular to b and c.

Thus, a is perpendicular to the plane of b and c.

Now, cross product of b and c will give a vector perpendicular to plane of b and c. This vector will be parallel to a.

Now, cross product of two parallel is zero vector.

Thus, $\mathbf{a} \times (\mathbf{b} \times \mathbf{c}) = 0$

141. (c) We know that, if a and b are two adjacent sides of a parallelogram, then

Area =
$$|\mathbf{a} \times \mathbf{b}| = 15$$
 (given) ... (i)
If the sides are $(3\mathbf{a} + 2\mathbf{b})$ and $(\mathbf{a} + 3\mathbf{b})$

Then, area of parallelogram

=
$$3|(3a + 2b) \times (a + 3b)|$$

= $|3a \times a + 9a \times b + 2b \times a + 6b \times a|$
= $|0 + 9a \times b - 2a \times b + 0|$
= $|7(a \times b)|$
= $7|a \times b|$
= $7 \times 15 = 105$ sq units

- 142. (c) The locus of the point which such that the ratio of its distance from two fixed point in the plane is always a constant k(k < 1) is an ellipse.
- 143. (d) Given lines are concurrent, then there coefficient determinant is zero.

So,
$$\begin{vmatrix} 1 & 3 & -9 \\ 4 & b & -2 \\ 2 & -1 & -4 \end{vmatrix} = 0$$

$$\Rightarrow 1(-4b-2) - 3(-16+4) - 9(-4-2b) = 0$$

$$\Rightarrow -4b - 2 + 36 + 36 + 18b = 0$$

$$\Rightarrow 14b + 70 = 0$$

$$\Rightarrow b = -5$$

144. (c) We know that the angle between the two lines $ax^2 + 2hxy + by^2 = 0$ is given by

$$\tan \theta = \frac{2\sqrt{h^2 - ab}}{a + b}$$

$$\theta = 90^{\circ}$$

$$a + b = 0$$

145. (b) Since, the equation of tangents x - y - 2 = 0 and x - y + 2 = 0 are parallel.

> Therefore, distance between them = Diameter of the circle

$$= \frac{2 - (-2)}{\sqrt{1^2 + 1^2}}$$
$$= \frac{4}{\sqrt{2}} = 2\sqrt{2}$$

Radius =
$$\frac{1}{2}(2\sqrt{2}) = \sqrt{2}$$

2.

Now, required equation of circle is

$$(x-0)^2 + (y-0)^2 = (\sqrt{2})^2$$

$$x^2 + y^2 = 2$$

146. (*) Let point $P(x_1, y_1)$ be any point on the circle, therefore it satisfy the circle

$$(x_1 - 3)^2 + (y_1 + 2)^2 = 5r^2$$
 ... (i)

The length of the tangent drawn from point $p(x_1, y_1)$ to the circle $(x-3)^2 + (y+2)^2 = r^2$ is

$$x_1, y_1$$
) to the circle $(x-3) + (y+2) = r$
 $\sqrt{(x_1-3)^2 + (y_1+2)^2 - r^2} = \sqrt{5r^2 - r^2}$
 $= \sqrt{4r^2} = 2r$

$$\Rightarrow 2r = 16$$

$$\Rightarrow r = 8$$

So, area between two circles

=
$$\pi(5r^2) - \pi r^2$$

= $5\pi r^2 - \pi r^2$
= $4\pi r^2 = 4\pi \times 64$
= 256π sq units

147. (*) Given equation of circles are

$$ax^2 + ay^2 + 2g_1x + 2f_1y + c_1 = 0$$

and $bx^2 + by^2 + 2g_2x + 2f_2y + c_2 = 0$

It can be rewritten as,

$$x^{2} + y^{2} + \frac{2g_{1}}{a}x + \frac{2f_{1}}{a}y + \frac{c_{1}}{a} = 0$$
and
$$x^{2} + y^{2} + \frac{2g_{2}}{b}x + \frac{2f_{2}}{b}y + \frac{c_{2}}{b} = 0$$

So, centres of circle
$$\left(-\frac{g_1}{a}, -\frac{f_1}{a}\right)$$

and
$$\left(-\frac{g_2}{b}, -\frac{f_2}{b}\right)$$
 respectively.

We know that, if two circles cut orthogonally, then

$$2(g_1g_2 + f_1f_2) = c_1 + c_2$$

 $\Rightarrow 2\left(\frac{g_1g_2}{ab} + \frac{f_1f_2}{ab}\right) = \frac{c_1}{a} + \frac{c_2}{b}$
 $2(g_1g_2 + f_1f_2) = bc_1 + ac_2$

148. (d) Let

$$S_1 \equiv x^2 + y^2 - 6x - 12y + 37 = 0$$

and $S_2 \equiv x^2 + y^2 - 6y + 7 = 0$

The equation of common tangent of the two circles is

$$\Rightarrow x^2 + y^2 - 6x - 12y + 37 - (x^2 + y^2 - 6y + 7) = 0$$

\Rightarrow - 6x + 6y + 30 = 0
\Rightarrow x - y - 5 = 0

149. (d) Given, vertex of the parabola (h, k) = (-1, 1) and its

$$(a + h, k) = (2, 1)$$
 or $a + h = 2 \Rightarrow a = 3$

We know that as the y-coordinate of vertex and focus are same, therefore axis of parabola is parallel to X-axis.

Thus, equation of parabola is

$$(y-k)^{2} = 4a(x-h)$$

$$(y-1)^{2} = 4 \times 3(x+1)$$

$$(y-1)^{2} = 12x + 12$$

$$y^{2} + 1 - 2y = 12x + 12$$

$$y^{2} - 12x - 2y - 11 = 0$$

150. (a) Let the equation of line by y = mx + C

Since, this is the tangent to the circle $x^2 + y^2 = 5$

So,
$$C = \pm a\sqrt{1 + m^2}$$

= $\pm \sqrt{5}\sqrt{1 + m^2}$...(i)

Also, the above line is tangent to the parabola

$$y^2 = 40x$$

So, $c = \frac{a}{m} = \frac{10}{m}$... (ii)

By Eqs. (i) and (ii), we get
$$\frac{10}{m} = \pm \sqrt{5} \sqrt{1 + m^2}$$
$$m^4 + m^2 - 20 = 0$$
$$(m^2 + 5) (m^2 - 4) = 0$$
$$m^2 = 4 (m^2 \neq -5)$$

$$m = \pm 2 \Rightarrow c = \pm 5$$

Here. $y = \pm 2x \pm 5$

151. (a) Given,
$$x = 4(1 + \cos \theta)$$

and $y = 3(1 + \sin \theta)$
 $\Rightarrow \cos \theta = \frac{x}{4} - 1 = \frac{x - 4}{4}$
and $\sin \theta = \frac{y}{3} - 1 = \frac{y - 3}{3}$

$$\sin^2\theta + \cos^2\theta = 1$$

$$\therefore \frac{(x-4)^2}{16} + \frac{(y-3)^2}{9} = 1$$

152. (d) Equation of hyperbola is

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

Distance between foci = 2ae

and distance between directrices = $\frac{2a}{}$

According to question, we have

$$\frac{2ae}{2a/e} = \frac{3}{2}$$

$$\Rightarrow \qquad e^2 = \frac{3}{2}$$

$$\therefore \qquad b^2 = a^2(e^2 - 1)$$

$$\Rightarrow \qquad \frac{b^2}{a^2} = \frac{3}{2} - 1 = \frac{1}{2}$$

$$\Rightarrow \qquad \frac{b}{a} = \frac{1}{\sqrt{2}}$$

153. (a) Equation of ellipse is

$$\frac{x^2}{25} + \frac{y^2}{16} = 1, \, a > b$$

and equation of hyperbola is
$$\frac{x^2}{25} - \frac{y^2}{16} = 1, a > b$$

Let e and e' be the eccentricities of the ellipse and hyperbola.

So,
$$e = \sqrt{\frac{a^2 - b^2}{a^2}} = \sqrt{\frac{25 - 16}{25}} = \frac{3}{5}$$

and

$$e' = \sqrt{\frac{a^2 + b^2}{a^2}} = \sqrt{\frac{25 + 16}{25}} = \frac{\sqrt{41}}{5}$$

- (i) Centre of ellipse (0, 0) and centre of hyperbola is (0, 0)
- (ii) Foci of ellipse are (± ae, 0) or (± 3, 0). Foci of hyperbola are (± ae', o) or (±√41, 0).
- (iii) Direction of ellipse are

$$x = \pm \frac{a}{e} \Rightarrow x = \pm \frac{25}{3}$$

and directrices of hyperbola are $x = \pm \frac{a}{a}$

$$\Rightarrow x = \pm \frac{25}{\sqrt{41}}$$

(iv) Vertices of ellipse are (± a, 0) or (± 5, 0). Vertices of hyperbola are (± a, 0) or (±5, 0).
From the above discussions, their are common is

centre and vertices. 154. (d) We have, $\sec \theta = m$ and $\tan \theta = n$

Now,
$$\frac{1}{m} \left[(m+n) + \frac{1}{(m+n)} \right]$$

$$= \frac{1}{\sec \theta} \left[(\sec \theta + \tan \theta) + \frac{1}{(\sec \theta + \tan \theta)} \right]$$

$$= \frac{1}{\sec \theta} \left[\frac{(\sec \theta + \tan \theta)^2 + 1}{(\sec \theta + \tan \theta)} \right]$$

$$= \frac{1}{\sec \theta} \left[\frac{\sec^2 \theta + \tan^2 \theta + 2\sec \theta \tan \theta + 1}{(\sec \theta + \tan \theta)} \right]$$

$$= \frac{1}{\sec \theta} \left[\frac{\sec^2 \theta + \sec^2 \theta - 1 + 2\sec \theta + \tan \theta + 1}{\sec \theta + \tan \theta} \right]$$

$$= \frac{1}{\sec \theta} \left[\frac{2\sec^2 \theta + 2\sec \theta \tan \theta}{\sec \theta + \tan \theta} \right]$$

$$= \frac{1}{\sec \theta} \left[\frac{2\sec \theta (\sec \theta + \tan \theta)}{(\sec \theta + \tan \theta)} \right]$$

$$= \frac{1}{\sec \theta} \left[\frac{2\sec \theta (\sec \theta + \tan \theta)}{(\sec \theta + \tan \theta)} \right]$$

$$= \frac{1}{\sec \theta} \left[(2\sec \theta) = 2 \right]$$

155. (b)
$$\frac{\sin 85^{\circ} - \sin 35^{\circ}}{\cos 65^{\circ}}$$

$$= \frac{2 \cos \left(\frac{85^{\circ} + 35^{\circ}}{2}\right) \sin \left(\frac{85^{\circ}}{2}\right) \sin \left(\frac{85^{\circ}}{2}\right) \sin \left(\frac{85^{\circ}}{2}\right) \sin \left(\frac{85^{\circ}}{2}\right) \sin \left(\frac{85^{\circ}}{2}\right) \cos 65^{\circ}$$

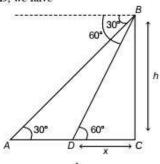
$$= \frac{2 \cos 60^{\circ} \sin 25^{\circ}}{\cos 65^{\circ}}$$

$$= \frac{2 \times \frac{1}{2} \times \sin 25^{\circ}}{\cos (90^{\circ} - 25^{\circ})}$$

$$= \frac{\sin 25^{\circ}}{\sin 25^{\circ}} = 1$$

156. (c) Let the distance of two consecutive stones are (x, x + 1).

In ΔBCD , we have



$$\tan 60^{\circ} = \frac{h}{x}$$

 $\Rightarrow x = \frac{h}{\sqrt{3}}$... (i)

In $\triangle ABC$, we have

$$\tan 30^{\circ} = \frac{h}{x+1}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{h}{x+1}$$

$$\Rightarrow \frac{h}{\sqrt{3}} + 1 = \sqrt{3}h \qquad \text{[by Eq. (i)]}$$

$$\Rightarrow h\left(\sqrt{3} - \frac{1}{\sqrt{3}}\right) = 1$$

$$\Rightarrow h \cdot \left(\frac{2}{\sqrt{3}}\right) = 1 \Rightarrow h = \frac{\sqrt{3}}{2}$$

157. (d) Let the angles of triangle are 30, 40, 50.

As we know that,

$$\angle A + \angle B + \angle C = 180^{\circ}$$

 $\Rightarrow 3\theta + 4\theta + 5\theta = 180^{\circ}$
 $\Rightarrow 12\theta = 180^{\circ} \Rightarrow \theta = 15^{\circ}$
So, angle are 45°, 60°, 75°.

Now, sin $A = \sin 45^{\circ} = \frac{1}{\sqrt{2}}$ $\sin B = \sin 60^{\circ} = \frac{\sqrt{3}}{2}$ $\sin C = \sin 75^{\circ} = \frac{\sqrt{3} + 1}{2\sqrt{2}}$

So,
$$a:b:c = \sin A: \sin B: \sin C$$

= $\frac{1}{\sqrt{2}}: \frac{\sqrt{3}}{2}: \frac{\sqrt{3}+1}{2\sqrt{2}}$
= $2:\sqrt{6}:\sqrt{3}+1$

158. (b) Given that,
$$\cos^{-1} x = \alpha$$
, $(0 < x < 1)$... (i)

$$\Rightarrow x = \cos \alpha$$
Thus, $\sin^{-1}(2x\sqrt{1-x^2}) + \sec^{-1}\left(\frac{1}{2x^2-1}\right) = \frac{2\pi}{3}$

$$\Rightarrow \sin^{-1}(2\cos\alpha\sqrt{1-\cos^{2}\alpha})$$

$$+ \sec^{-1}\left(\frac{1}{2\cos^{2}\alpha-1}\right) = \frac{2\pi}{3}$$

$$\Rightarrow \sin^{-1}(\sin 2\alpha) + \sec^{-1}(\sec 2\alpha) = \frac{2\pi}{3}$$

$$\Rightarrow 2\alpha + 2\alpha = \frac{2\pi}{3} \Rightarrow \alpha = \frac{\pi}{6}$$
Now, $x = \cos\frac{\pi}{6} = \frac{\sqrt{3}}{2} \Rightarrow 2x = \sqrt{3}$
Therefore, $\tan^{-1}(2x) = \tan^{-1}\sqrt{3} = \frac{\pi}{3}$

159. (a) We have,

$$\tan^{-1}\left(\frac{a}{b}\right) + \tan^{-1}\left(\frac{a+b}{a-b}\right)$$

$$= \tan^{-1}\left[\frac{\frac{a}{b} + \frac{a+b}{a-b}}{1 - \left(\frac{a}{b}\right)\left(\frac{a+b}{a-b}\right)}\right]$$

$$= \tan^{-1}\left[\frac{\frac{a^2 - ab + ab + b^2}{b(a-b)}}{\frac{b(a-b)}{b(a-b)}}\right]$$

$$= \tan^{-1}\left[\frac{a^2 + b^2}{ab - b^2 - a^2 - ab}\right]$$

$$= \tan^{-1}\left[\frac{a^2 + b^2}{-(a^2 + b^2)}\right] = \tan^{-1}(-1)$$

It does not depends neither a nor b.

160. (c) By option (c),

 $\csc \theta \cdot \sec \theta = 1$

 $\sin \theta \cos \theta = 1$

 $2\sin\theta\cos\theta = 2$

 $\sin 2\theta = 2$

As we know that range of $\sin x$ is [-1, 1].

Hence, this equation has no solution.

161. (b) Let
$$z = \frac{(-\sqrt{3} + 3i)(1 - i)}{(3 + \sqrt{3}i)(i)(\sqrt{3} + \sqrt{3}i)}$$

$$= \frac{\sqrt{3}(-1 + \sqrt{3}i)(1 - i)}{(\sqrt{3})^2(\sqrt{3} + i)(1 + i)(i)}$$

$$= \frac{(-1 + \sqrt{3}i)(1 - i)}{\sqrt{3}(\sqrt{3}i + i^2)(1 + i)} = \frac{(-1 + \sqrt{3}i)(1 - i)}{\sqrt{3}(-1 + \sqrt{3}i)(1 + i)}$$

$$= \frac{1 - i}{(\sqrt{3})1 + i} \times \frac{(1 - i)}{(1 - i)} = \frac{(1 - i)^2}{(\sqrt{3})(1 + 1)}$$

$$= \frac{1 + i^2 - 2i}{2\sqrt{3}} = \frac{-2i}{2\sqrt{3}} = -\frac{i}{\sqrt{3}}$$
= Purely imaginary

162. (a) We have,

$$2x = -1 + \sqrt{3} i \implies x = \frac{-1 + \sqrt{3}i}{2} = \omega$$

$$So, (1 - x^2 + x)^6 - (1 - x + x^2)^6$$

$$= (1 - \omega^2 + \omega)^6 - (1 - \omega - \omega^2)^6$$

$$= (-2\omega^2)^6 - (-\omega - \omega)^6 = 2^6\omega^{12} - 2^6\omega^6$$

$$= 2^6 - 2^6 = 0 \qquad [\because \omega^3 = 1]$$

163. (c) Let
$$z = (1 + i\sqrt{3})^8$$

$$= \left(2\left(\frac{1}{2} + \frac{\sqrt{3}}{2}i\right)\right)^8$$

$$= \left[2(\cos 60^\circ + i\sin 60^\circ)\right]^8 = (2^8 e^{i\pi/3})^8$$

$$= 2^8 \cdot e^{\frac{8\pi}{3}i} = 2^8 \cdot e^{\left(2\pi + \frac{2\pi}{3}\right)i} = 2^8 \cdot e^{\frac{2\pi}{3}i}$$

So, modulus = $2^8 = 256$

and amplitude = $\frac{2\pi}{2}$

164. (d)
$$\lim_{x \to 0} \frac{5^x - 5^{-x}}{2x} = \lim_{x \to 0} \frac{5^x \log 5 + 5^{-x} \log 5}{2}$$
(Applying L' Hospital rule)
$$= \frac{\log 5 + \log 5}{2} = \log 5$$

165. (c) If a function f(x is continuous at x = a).

Then, it may or may not be differentiable at x = a.

166. (a) Given,
$$y = \frac{1}{x} + \frac{1}{x^2} + \frac{1}{x^3} + \dots \infty$$

This is an infinite GP with a = 1

and
$$r = \frac{1}{x}$$

$$\therefore S_{\infty} = \frac{a}{1-r}$$

$$y = \frac{1}{1-\frac{1}{x}}$$

$$y = \frac{x}{x-1}$$
Now,
$$\frac{dy}{dx} = \frac{(x-1)-x}{(x-1)^2} = \frac{x-1-x}{(x-1)^2} = \frac{-1}{(x-1)^2}$$

$$= -\frac{1}{\left(\frac{x^2}{y^2}\right)} = -\frac{y^2}{x^2}$$

167. (*)
$$f\{g(x)\} = x^3 - \frac{1}{x^3}$$

$$f\left(x - \frac{1}{x}\right) = \left(x - \frac{1}{x}\right)\left(x^2 + \frac{1}{x^2} + 1\right)$$

$$= \left(x - \frac{1}{x}\right)\left\{\left(x - \frac{1}{x}\right)^2 + 2 + 1\right\}$$

$$f\left(x - \frac{1}{x}\right) = \left(x - \frac{1}{x}\right) \left\{ \left(x - \frac{1}{x}\right)^2 + 3 \right\}$$

Replace $x - \frac{1}{r}$ by x,

$$f(x) = (x)(x^2 + 3) = x^3 + 3x$$

$$f'(x) = 3x^2 + 3$$

168. (b) Let $u = a^{\sec x} \implies v = a^{\tan x}$

 $\log u = \sec x \log a$

$$\frac{du}{dx} = u \log a \sec x \tan x$$
$$= a^{\tan x} \log a \sec x \tan x$$

and

$$\frac{dv}{dx} = \tan x \log a$$

$$\frac{dv}{dx} = v \log a \sec^2 x$$

$$= a^{\tan x} \log a \sec^2 x$$

$$= a^{\tan x} \log a \sec^2 x$$

$$\frac{dx}{du} = a^{\tan x} \log a \sec^2 x$$

$$\frac{du}{dv} = \frac{\left(\frac{du}{dx}\right)}{\frac{dv}{dx}} = \frac{a^{\sec x} \log a \sec x \tan x}{a^{\tan x} \log a \sec^2 x}$$

$$= \frac{a^{\sec x} \sin x}{a^{\tan x}} = \sin x \ a^{\sec x - \tan x}$$

169. (c) Given that, $\sin(x + y) + \cos(x + y) = \log(x + y)$

On differentiating w.r.t. x,

$$\cos(x+y) \cdot \left(1 + \frac{dy}{dx}\right) - \sin(x+y) \left(1 + \frac{dy}{dx}\right)$$

$$= \frac{1}{(x+y)} \left(1 + \frac{dy}{dx}\right)$$

$$\Rightarrow \left(1 + \frac{dy}{dx}\right) \left\{\cos(x+y) - \sin(x+y) - \frac{1}{(x+y)}\right\} = 0$$

$$\Rightarrow 1 + \frac{dy}{dx} = 0$$

Again differentiating w.r.t. 'x'

$$0 + \frac{d^2y}{dx^2} = 0 \implies \frac{d^2y}{dx^2} = 0$$

170. (a) We have,

$$g(x) = [f(x)]^2 + [f'(x)]^2$$

Differentiate the function g(x)

$$g'(x) = 2f(x) f'(x) + 2f'(x)f''(x)$$

Use chain rule,

$$2f'(x)[f(x)+f''(x)]=2f'(x)(0)=0$$

Hence, g(x) is a constant function

$$\Rightarrow$$
 $g(x) = c$, constant

But, g(3) = 8, so g(x) = 8

For all real x.

Hence, g(8) = 8

171. (c)
$$y = 2x^3 + ax^2 + bx + c$$
 ... (i)

Since, it passes through (0, 0),

$$0 = 2(0) + a(0) + b(0) + c$$

$$c = 0 \qquad \dots (ii)$$

$$\frac{dy}{dx} = 6x^2 + 2ax + b$$

Since, tangents at x = -1 and x = 2 are parallel to X-axis.

$$\therefore \frac{dy}{dx} = 0$$

$$6(-1)^2 + 2a(-1) + b = 0$$

 $6 - 2a + b = 0$... (iii)

At x = -2

So,
$$6(2)^2 + 2a(2) + b = 0$$

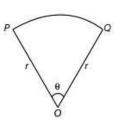
$$24 + 4a + b = 0$$
 ... (iv)

By solving Eqs. (iii) and (iv), we get

$$a = -3, b = -12$$

Hence,
$$a = -3$$
, $b = -12$, $c = 0$

172. (b)



Perimeter of sector = $2r + r\theta$

$$\Rightarrow 60 = 2r + r\theta \text{ (given)}$$

$$\Rightarrow$$
 $\theta = \frac{60 - 2r}{r}$

Now, area of sector,

$$(A) = \frac{\pi r^2 \theta}{360^{\circ}} = \frac{\pi r^2 (60 - 2r)}{360 r}$$
$$= \frac{\pi r}{180} (30 - r)$$
$$\frac{dA}{dr} = \frac{\pi}{180} (30 - 2r)$$

For maximum area $\frac{dA}{dr} = 0$

$$\Rightarrow 30 - 2r = 0$$

$$\Rightarrow 2r = 30 \Rightarrow r = 15$$

and
$$\frac{d^2A}{dr^2} = \frac{\pi}{180^{\circ}}(-2) = -\frac{\pi}{90} < 0$$

173. (a) Given, equation of curve is

$$y = x^2 - x + 4$$

Slope of tangent at P(1, 4) is

$$\frac{dy}{dx} = 2x - 1 \implies \left(\frac{dy}{dx}\right)_{(1,4)} = 2 - 1 = 1$$

So, equation of tangent is

$$y-4=1(x-1)$$

$$\Rightarrow y-x=3 \qquad ...(i)$$

and equation of normal at point P(1, 4) is

$$y - 4 = -1(x - 1)$$

 $x + y = 5$... (ii)

Since, the tangent cuts X-axis at A.

Therefore, coordinates of A are (-3, 0)

and the normal cuts X-axis at B and coordinates of B are

Therefore, area of ΔPAB

$$= \frac{1}{2} \begin{vmatrix} 1 & 4 & 1 \\ -3 & 0 & 1 \\ 5 & 0 & 1 \end{vmatrix}$$

$$= \frac{1}{2} [1(0) - 4(-3 - 5) + 1(0)]$$

$$= \frac{1}{2} |32| = 16 \text{ sq. units}$$

174. (d)
$$\int \frac{x^3 + 3x^2 + 3x + 1}{(x+1)^5} dx$$
$$= \int \frac{(x+1)^3}{(x+1)^5} dx = \int \frac{dx}{(x+1)^2}$$
$$= -\frac{1}{x+1} + c$$

175. (c) Let
$$I = \int \frac{\csc x}{\cos^2 \left(1 + \log \tan \frac{x}{2}\right)} dx$$

Put
$$1 + \log \tan \frac{x}{2} = t$$

$$\Rightarrow \frac{1}{\tan \frac{x}{2}} \cdot \sec^2 \frac{x}{2} \cdot \frac{dx}{2} = dt$$

$$\Rightarrow \frac{dx}{2\sin\frac{x}{2}\cos\frac{x}{2}} = dt \Rightarrow \frac{dx}{\sin x} = dt$$

$$\csc x dx = dt$$

$$\Rightarrow \cos c x \, dx = dt$$
So, $I = \int \frac{dt}{\cos^2 t} = \int \sec^2 t \, dt = \tan t + c$

$$= \tan \left(1 + \log \tan \frac{x}{2} \right) + c$$

176. (b) Let
$$I = \int \frac{dx}{x\sqrt{(x^3)^2 - 16}}$$

Put
$$x^3 = t \Rightarrow 3x^2 dx = dt$$

So,
$$I = \frac{1}{3} \int \frac{dt}{x^3 \sqrt{(x^3)^2 - 16}}$$

 $= \frac{1}{3} \int \frac{dt}{t(\sqrt{t^2 - 16})}$
 $= \frac{1}{3 \times 4} \sec^{-1} \left(\frac{t}{4}\right) + c$
 $= \frac{1}{12} \sec^{-1} \left(\frac{x^3}{4}\right) + c$

177. (d)
$$I_1 = \int_0^{\pi/2} x \sin x \, dx$$

$$= [-x \cos x + \int \cos x]_0^{\pi/2}$$

$$= [-x \cos x + \sin x]_0^{\pi/2}$$

$$= 0 + \sin \frac{\pi}{2} - 0 = 1$$

Similarly,
$$I_2 = \int_0^{\pi/2} x \cos x \, dx$$

$$= [x \sin x - \int \sin x]_0^{\pi/2}$$

$$= [x \sin x + \cos x]_0^{\pi/2}$$

$$= \frac{\pi}{2} \sin \frac{\pi}{2} - 1 = \frac{\pi}{2} - 1$$

Hence,
$$I_1 + I_2 = 1 + \frac{\pi}{2} - 1 = \frac{\pi}{2}$$

178. (b) Given that,
$$f(x) = 4x^2 - 3x + 1$$

$$g(x) = \frac{f(-x) - f(x)}{x^2 + 3}$$

$$g(x) = \frac{(4x^2 + 3x + 1) - (4x^2 - 3x + 1)}{x^2 + 3} = \frac{6x}{x^2 + 3}$$

Now,
$$g(-x) = -\frac{6x}{x^2 + 3} = g(x)$$

which is an odd function.

Thus,
$$\int_{-a}^{2} g(x) dx = 0$$

$$= \int_0^2 (x+2) - (x^2 - x + 2) dx$$

$$= \int_0^2 (x+2) - (x^2 - x + 2) dx = \int_0^2 (-x^2 + 2x) dx$$

$$= \left[-\frac{x^3}{3} + x^2 \right]_0^2$$

$$= -\frac{8}{3} + 4 - (0) = \frac{-8 + 12}{3} = \frac{4}{3}$$

180. (d) Given, differential equation is

$$e^{-x}(y+1) dy + (\cos^{2} x - \sin 2x)y dx = 0$$

$$\Rightarrow \left(\frac{y+1}{y}\right) dy + e^{x}(\cos^{2} x - \sin 2x) dx = 0$$

$$\Rightarrow \left(1 + \frac{1}{y}\right) dy + (e^{x} \cos^{2} x - e^{x} \sin 2x) dx = 0$$

$$\Rightarrow d(y + \log y) + d(e^{x} \cos^{2} x) = 0$$

On integrating above equation, we get

$$y + \log y + e^x \cos^2 x = c$$

At
$$y(0) = 1$$

$$\Rightarrow 1 + 0 + e^0 \cdot 1 = c \Rightarrow c = 2$$

Hence, required solution is

$$y + \log y + e^x \cos^2 x = 2$$